



**COMILLAS**

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MITEI-IAP24

Computational modeling for clean, reliable, and affordable electricity

Massachusetts Institute of Technology (MIT)

# *Transmission Expansion Planning*

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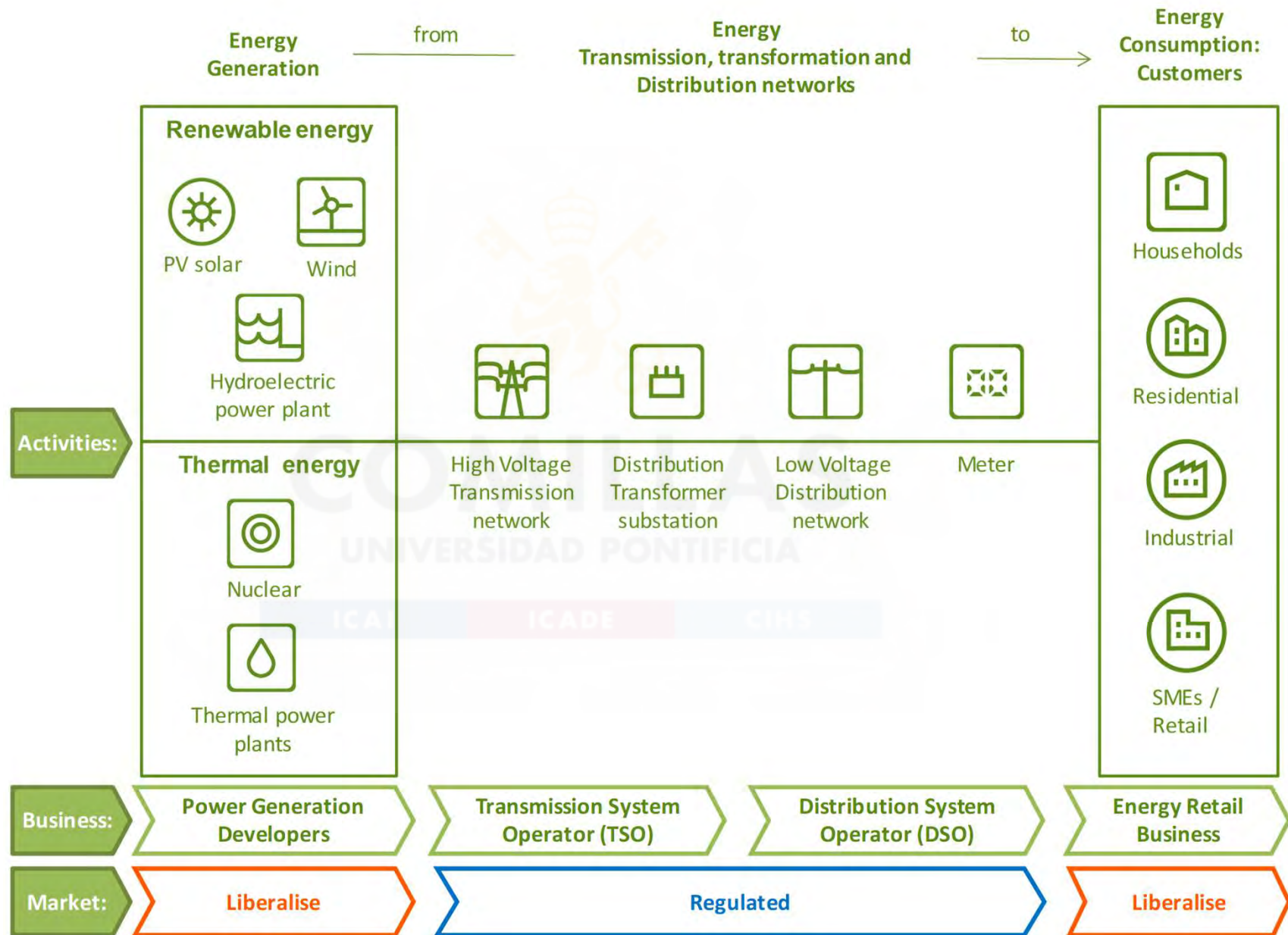
[arght@mit.edu](mailto:arght@mit.edu)

January 2024

# Motivation

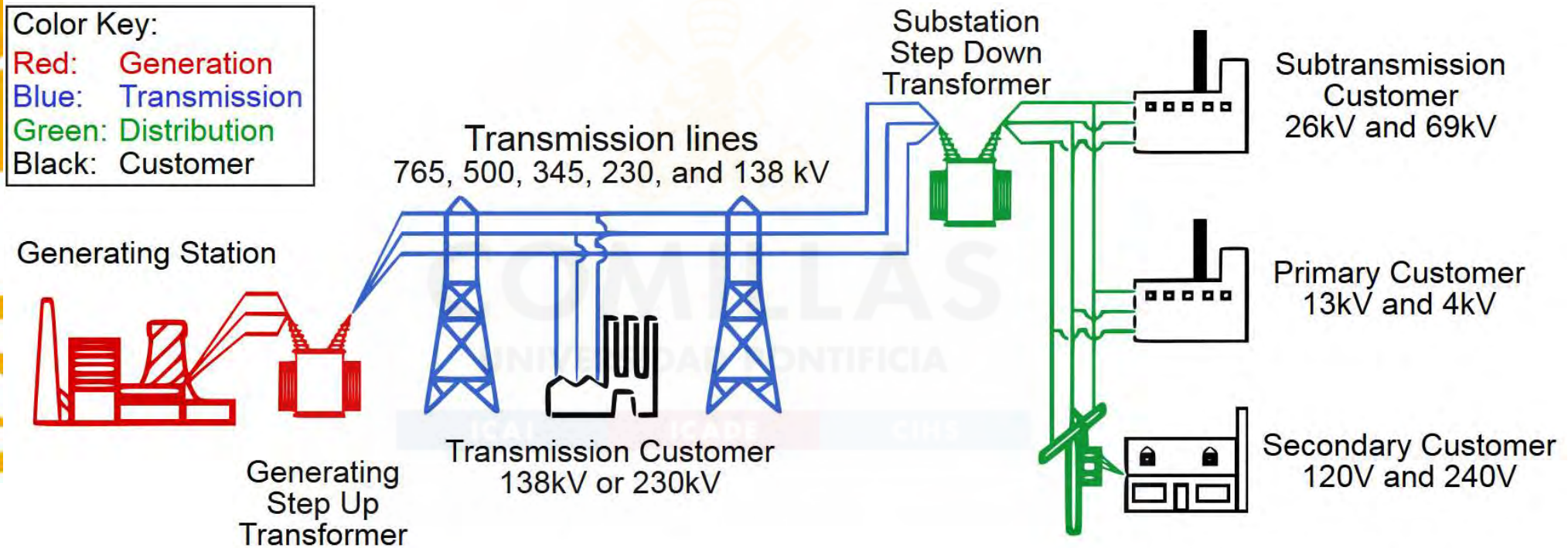
- To understand why the transmission plays a vital role in renewable integration
- To indicate what it is possible to state with a decision tool
  - Capabilities and limitations
- To become familiar with transmission network expansion modeling techniques
- To give the mathematical foundation

# Electric System. Activities, businesses and markets





# Electric System. Physical layout



[https://upload.wikimedia.org/wikipedia/commons/4/41/Electricity\\_grid\\_simple- North America.svg](https://upload.wikimedia.org/wikipedia/commons/4/41/Electricity_grid_simple- North America.svg)



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# Content

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- 2. Simple TEP models
- 3. Modeling issues
- 4. Prototype TEP. Mathematical formulation
- 5. Prototype TEP. Computer implementation
- 6. Takeaways

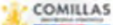
Transmission Expansion Planning



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- 1. Transmission Expansion Planning
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Simple TEP models



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Modeling issues



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Prototype TEP.  
Mathematical formulation



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Prototype TEP.  
Computer implementation



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Takeaways





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# Transmission Expansion Planning

# The future of system operations: The new 50Hertz Transmission Control Center



<http://www.youtube.com/watch?v=uE49sQMWekg>

## TenneT network planning - to guarantee system stability



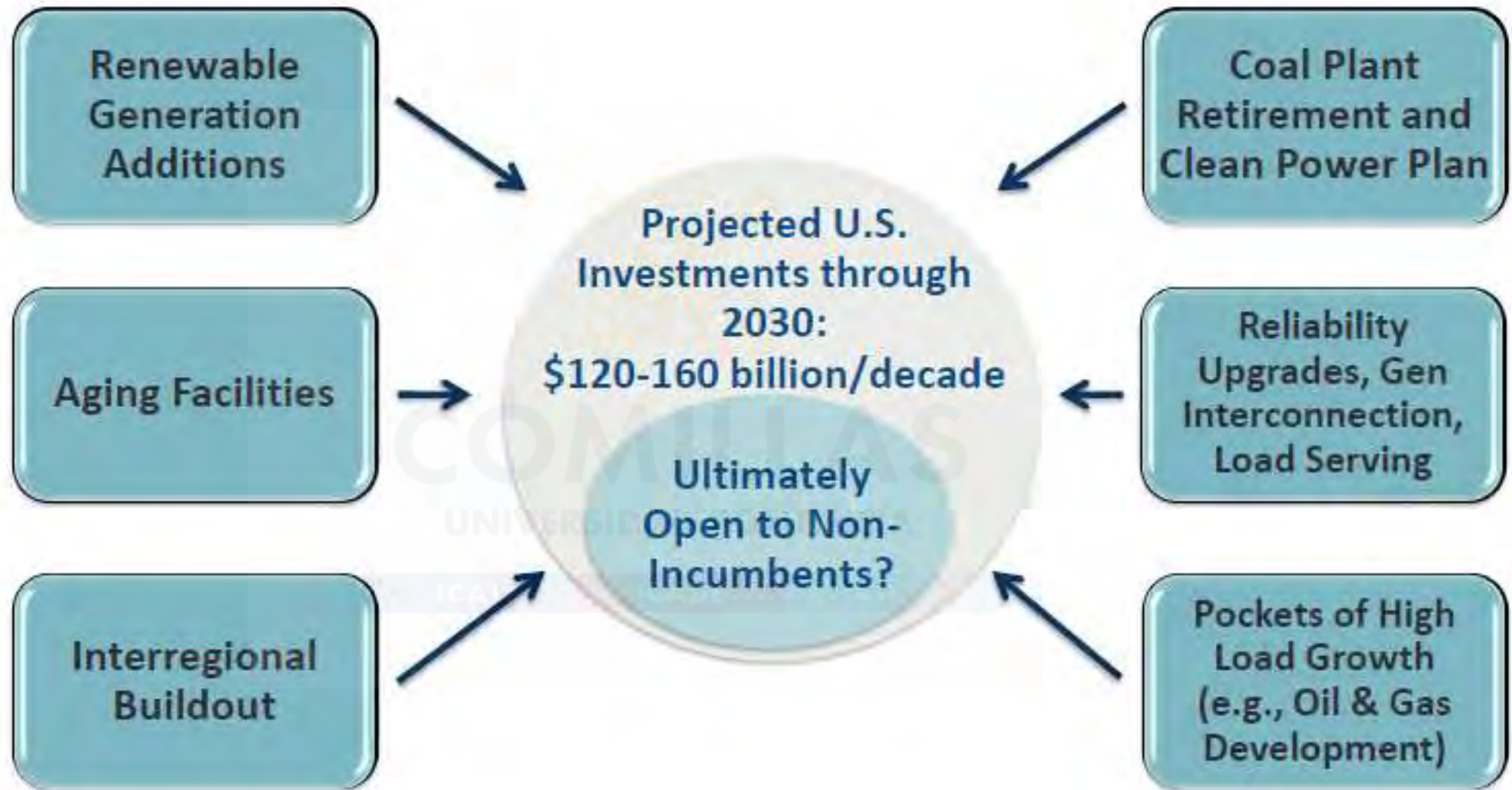
<https://youtu.be/P5Nol6dyJN4>

# Drivers for investing

- Reliability
- Economic efficiency
  - Reduce network losses
  - Mitigate capacity constraints (congestion), expand electricity markets, or mitigate market power
  - Avoidance/postponement of generation investments
- Generation connection of new (conventional) power plants
- Meet RES policy targets (solar and wind generation)
  - **European Green Deal**: 55% emission reductions by 2030 (Fit for 55)  
<https://www.consilium.europa.eu/en/policies/green-deal/>
  - **National Energy and Climate Plans (NCEP)**



# USA Projected Transmission Investment Opportunities



<http://www.brattle.co.uk/industry/electric-power/82-transmission>

# The White House. FACT SHEET: The American Jobs Plan

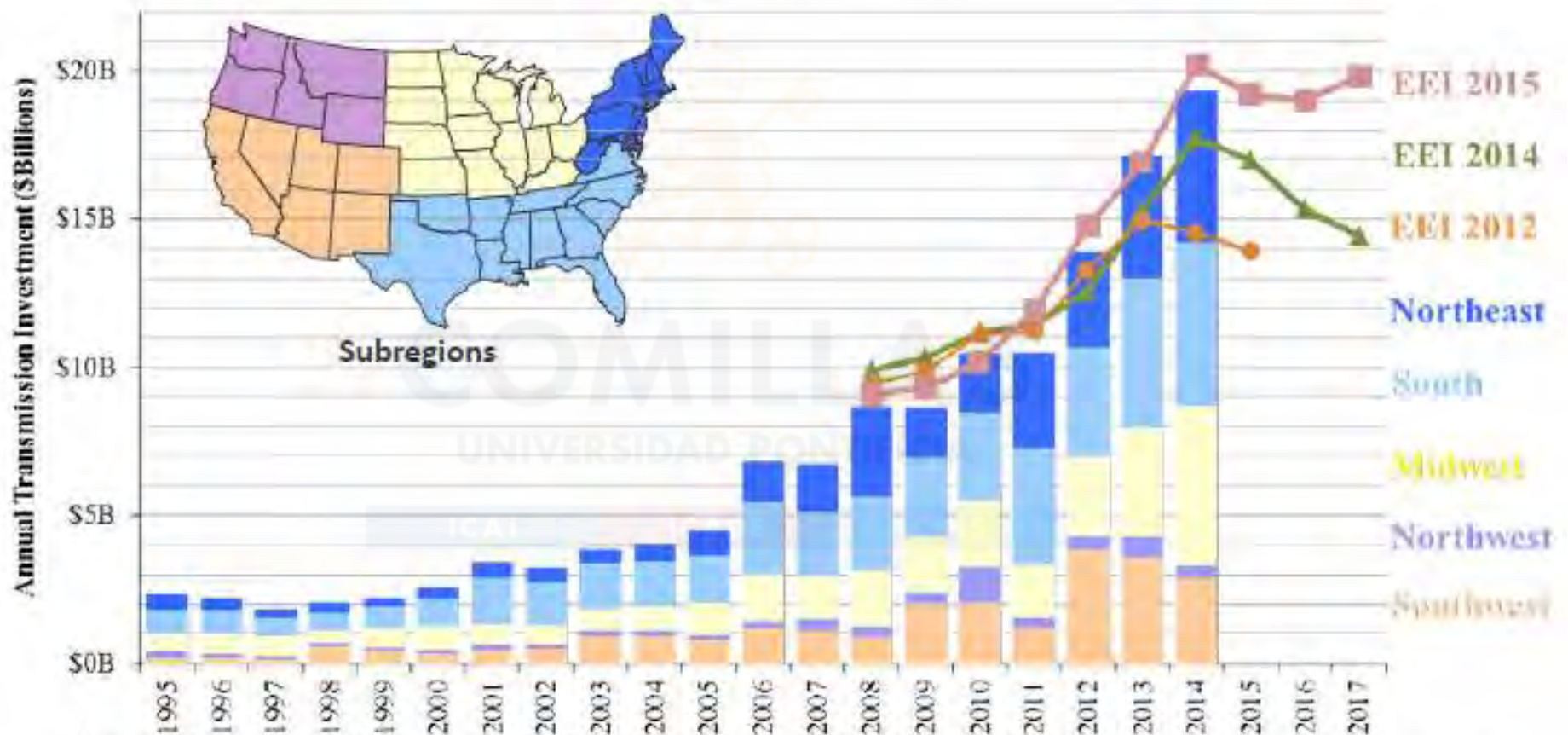
## Reenergize America's power infrastructure

- **Build a more resilient electric transmission system.** Through investments in the grid, we can move cheaper, cleaner electricity to where it is needed most. This starts with the creation of a targeted investment tax credit that incentivizes the buildout of at least 20 gigawatts of high-voltage capacity power lines and mobilizes tens of billions in private capital off the sidelines – right away. In addition, President Biden's plan will establish a new Grid Deployment Authority at the Department of Energy that allows for better leverage of existing rights-of-way – along roads and railways – and supports creative financing tools to spur additional high priority, high-voltage transmission lines. These efforts will create good-paying jobs for union laborers, line workers, and electricians, in addition to creating demand for American-made building materials and parts.



# USA Historical and Projected Transmission Investments

1995-2017 Annual Transmission Investment of Investor-Owned Utilities  
by FERC Subregion

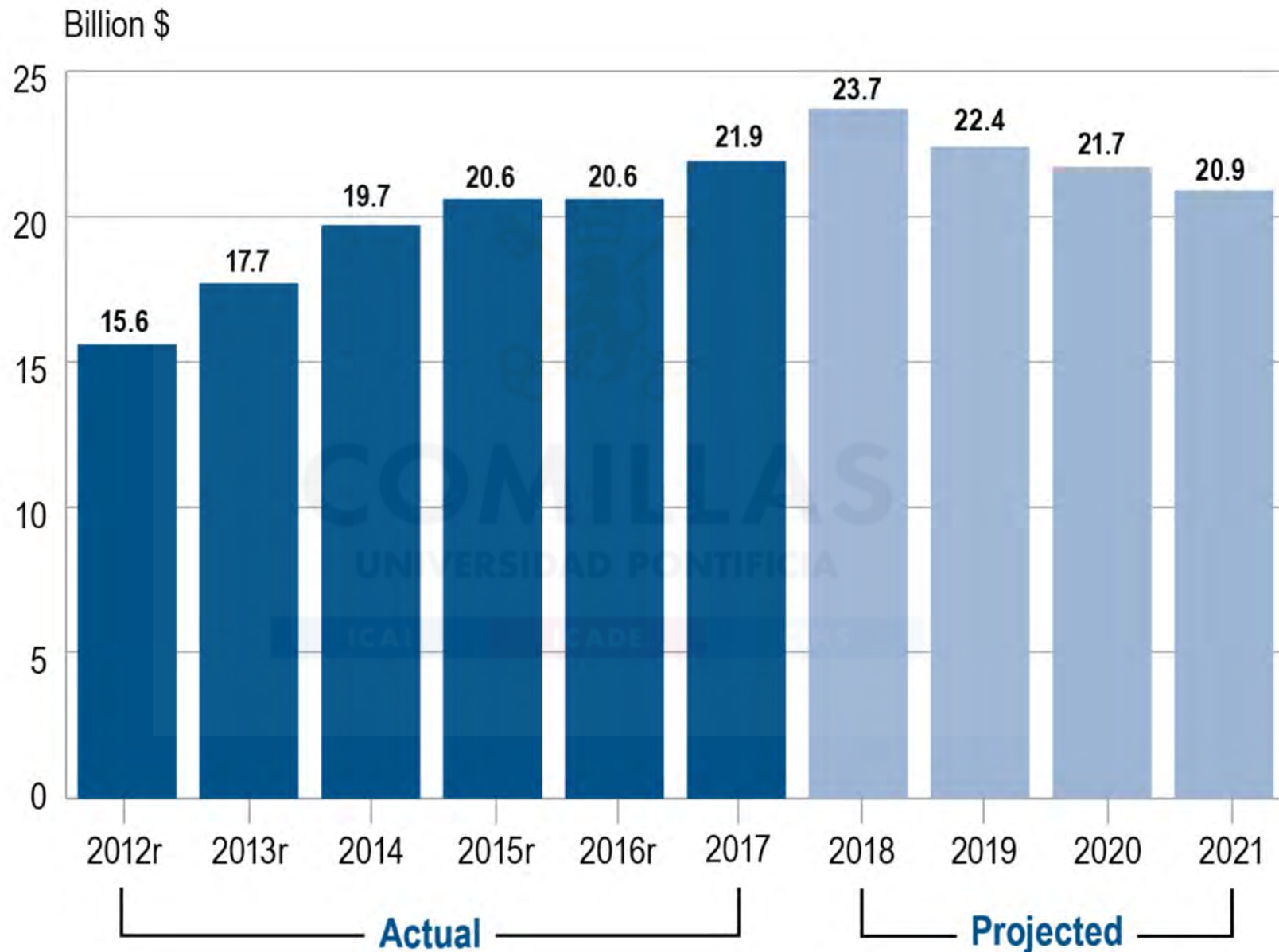


**Sources and Notes:** The Brattle Group's analysis of FERC Form 1 data compiled in Ventyx's Velocity Suite. Based on EIA data available through 2003, FERC-jurisdictional transmission owners estimated to account for 80% of transmission assets in the Eastern Interconnection, and 60% in WECC and ERCOT. Facilities >300kV estimated to account for 60-80% of shown investments. EEI annual transmission expenditures updated June 2015 shown (2008-2017) based on prior year's actual investment through 2013 and planned investment thereafter.

<http://www.brattle.co.uk/industry/electric-power/82-transmission>



# USA Historical and Projected Transmission Investments



# New England Clean Energy Connect (NECEC)

145 miles (233 km) of new HVDC line with 1200 MW at 345 kV, new DC/AC converter station, and multiple system upgrades



Started in January 2021

[https://youtu.be/TEdr\\_DfzUyE](https://youtu.be/TEdr_DfzUyE)



<https://www.necleanenergyconnect.org/>

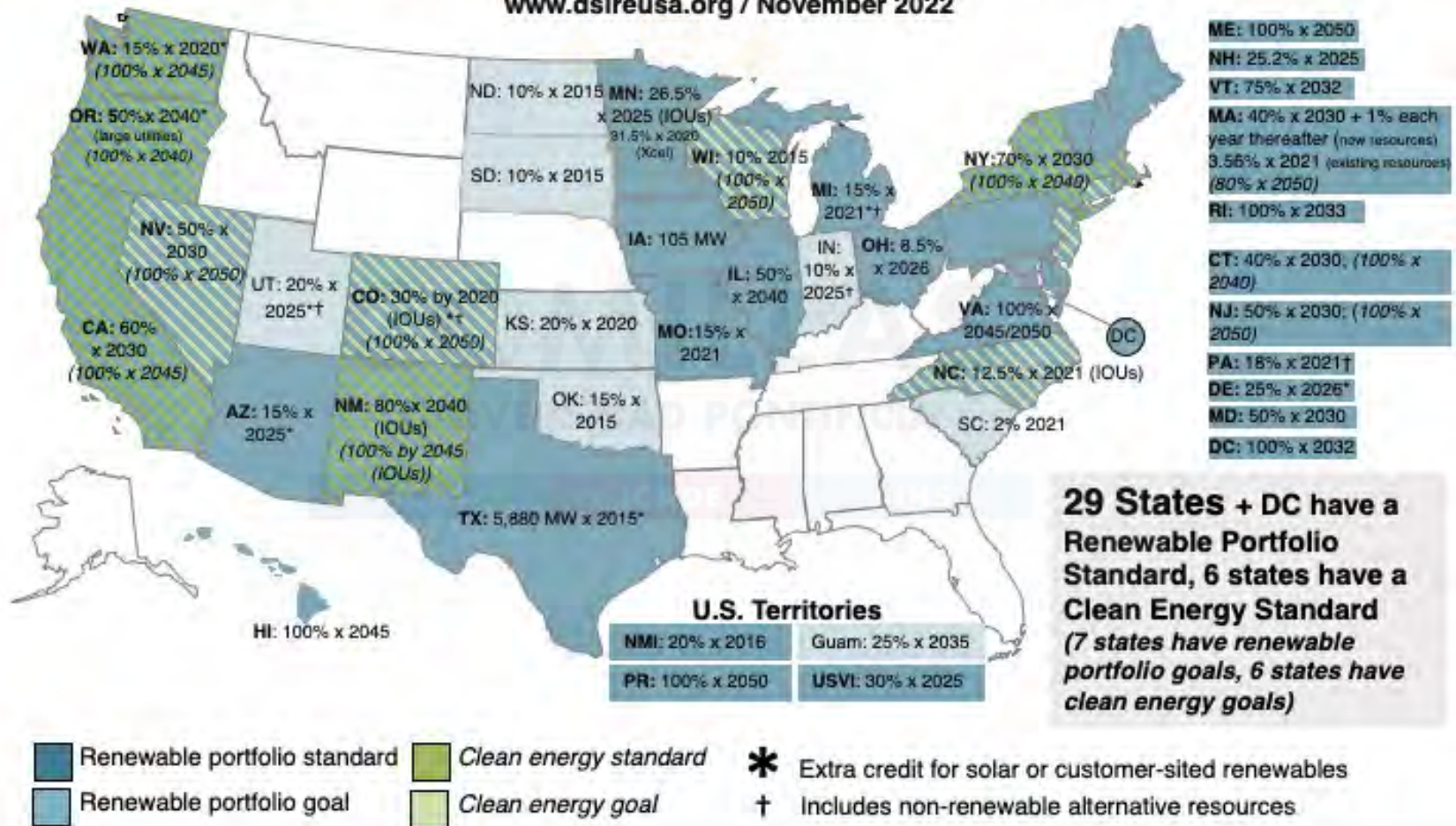


# USA Renewable Portfolio Standards (RPS)

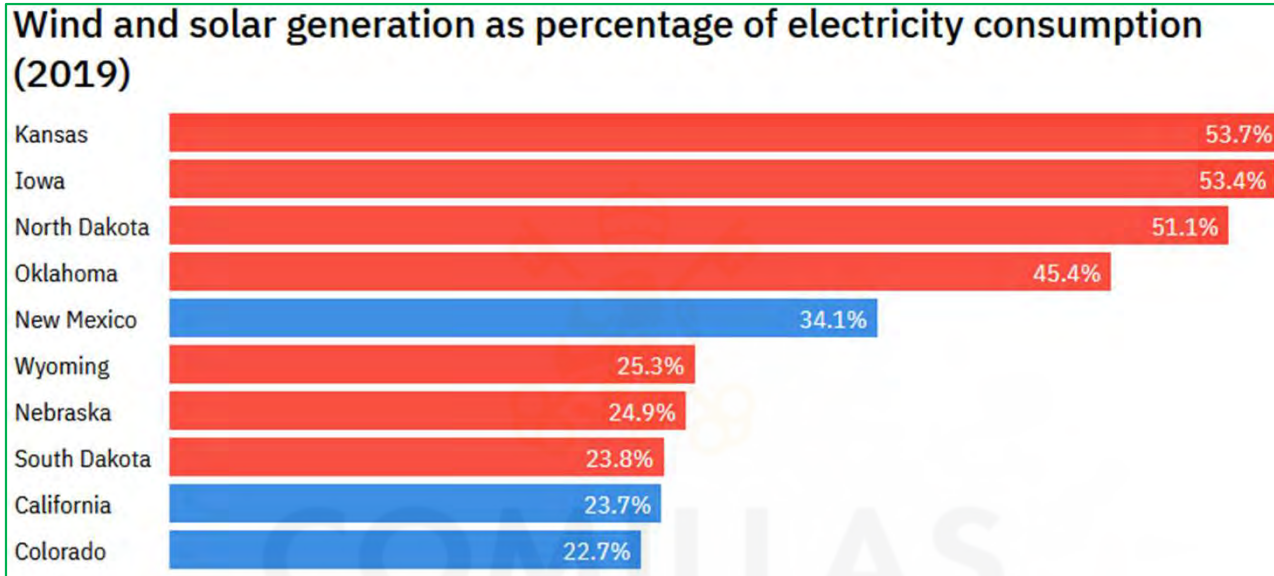


## Renewable & Clean Energy Standards

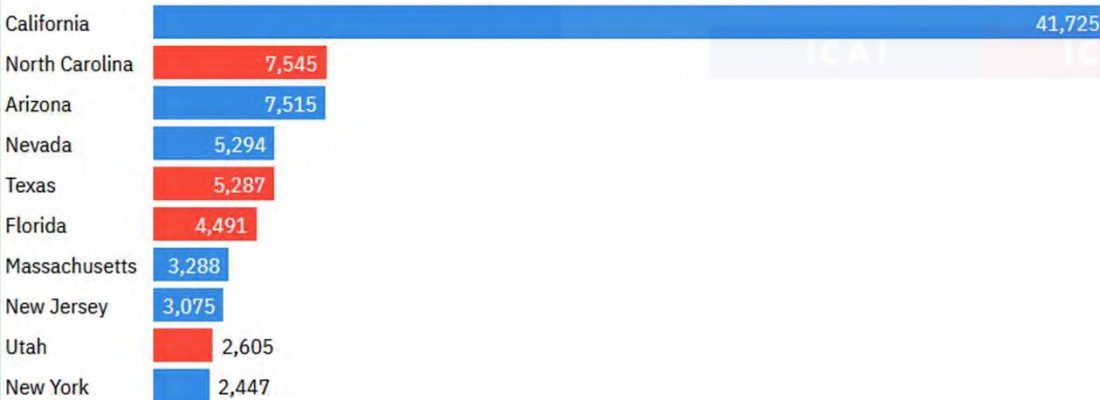
www.dsireusa.org / November 2022



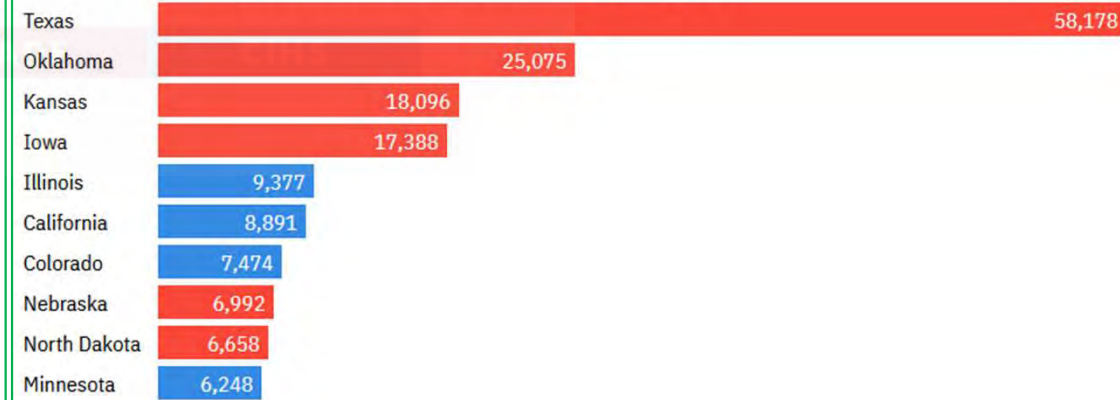
# US red states among wind and/or solar leaders



**Increase in solar electricity, 2010-2019 (GWh)**

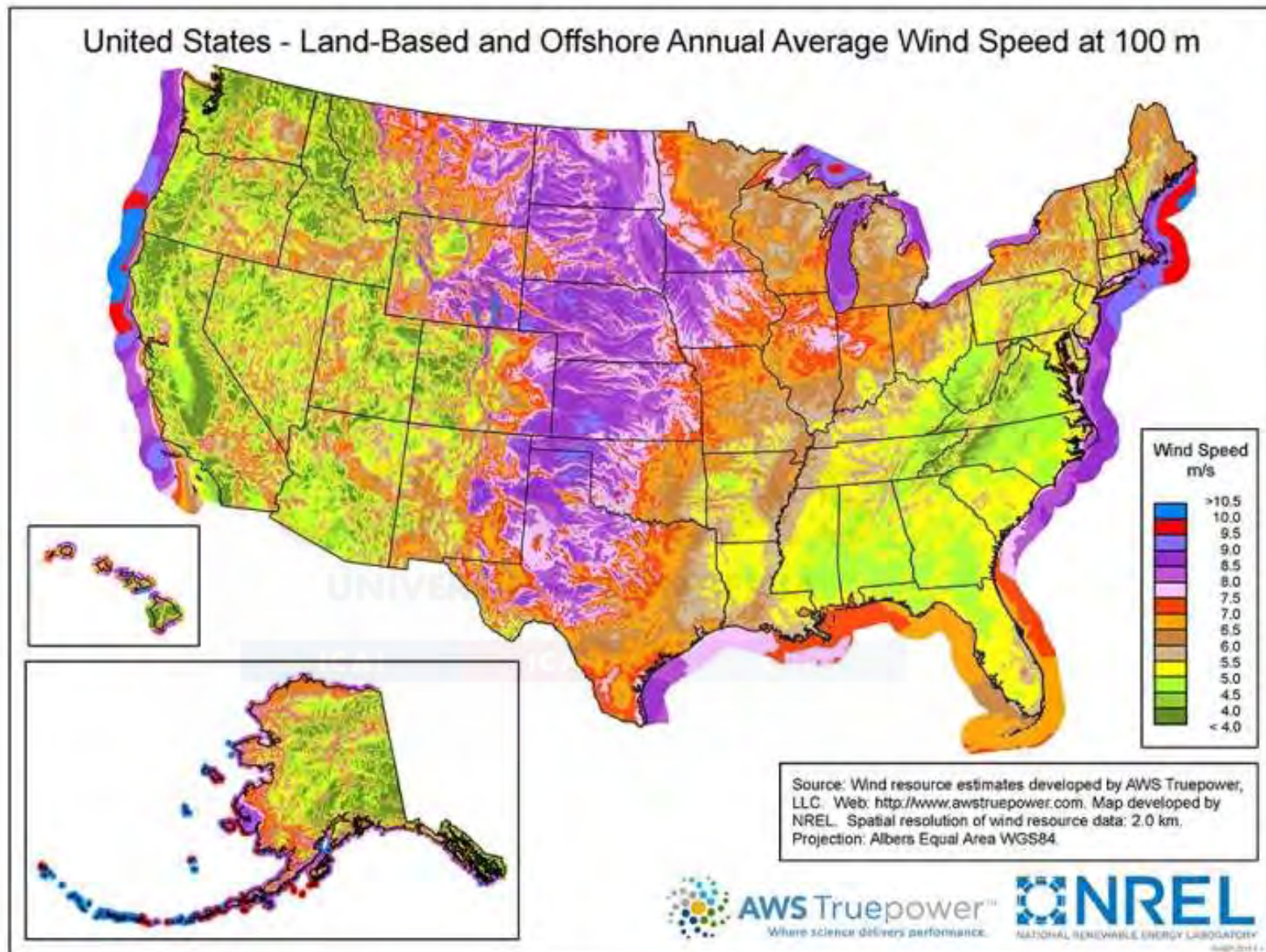


**Increase in wind electricity, 2010-2019 (GWh)**





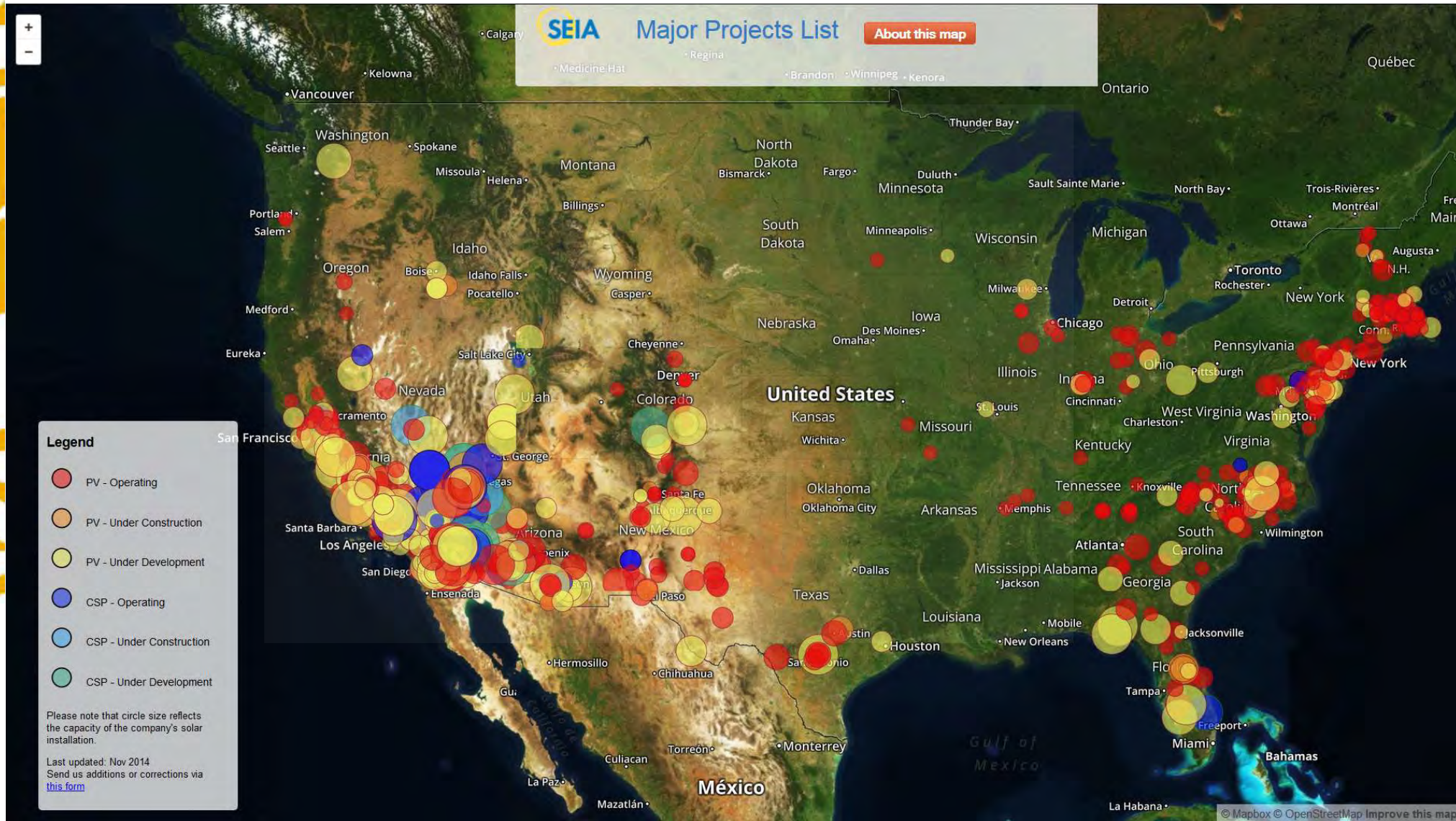
# Land Based and Offshore Annual Average Wind Speed at 100 Meters



<https://energy.gov/eere/wind/downloads/united-states-land-based-and-offshore-annual-average-wind-speed-100-meters>

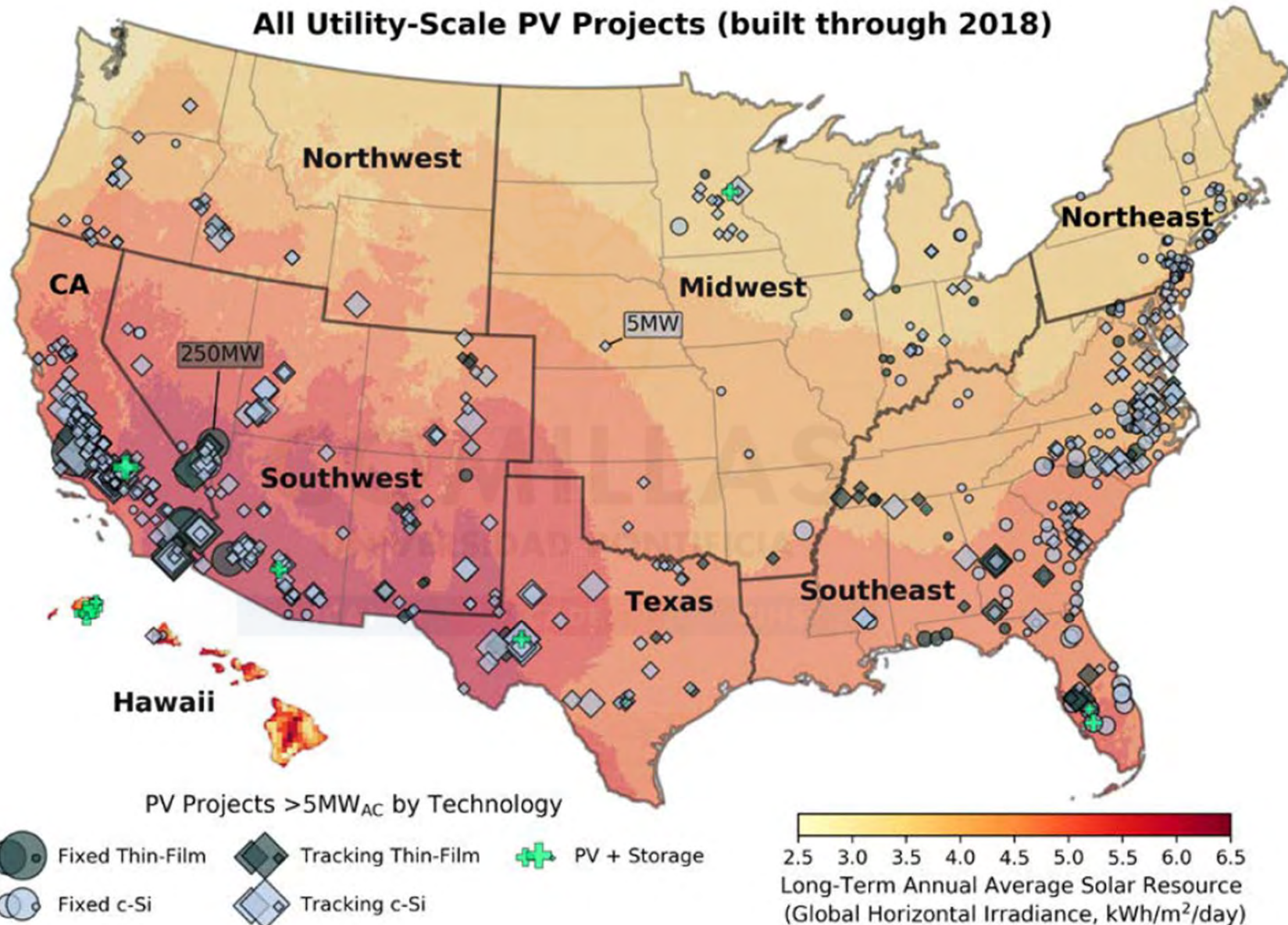


# Major PV and CSP projects in the US





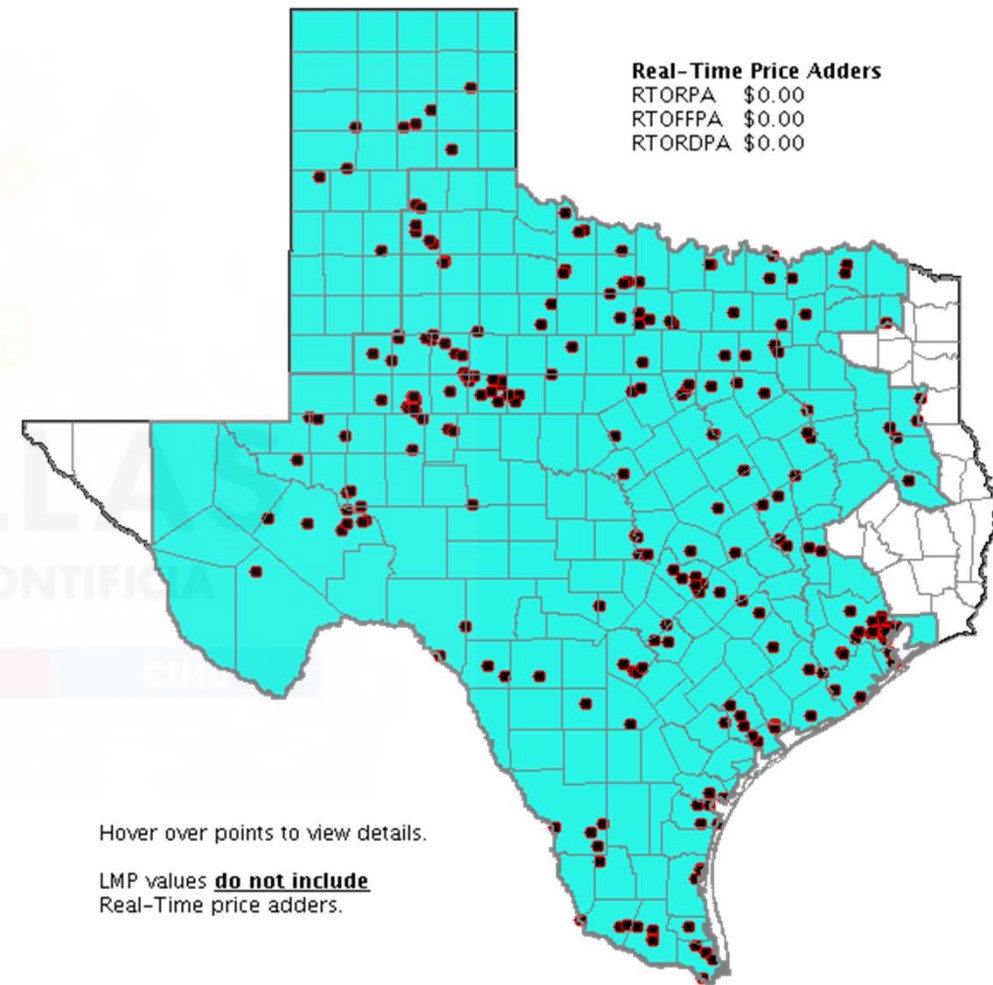
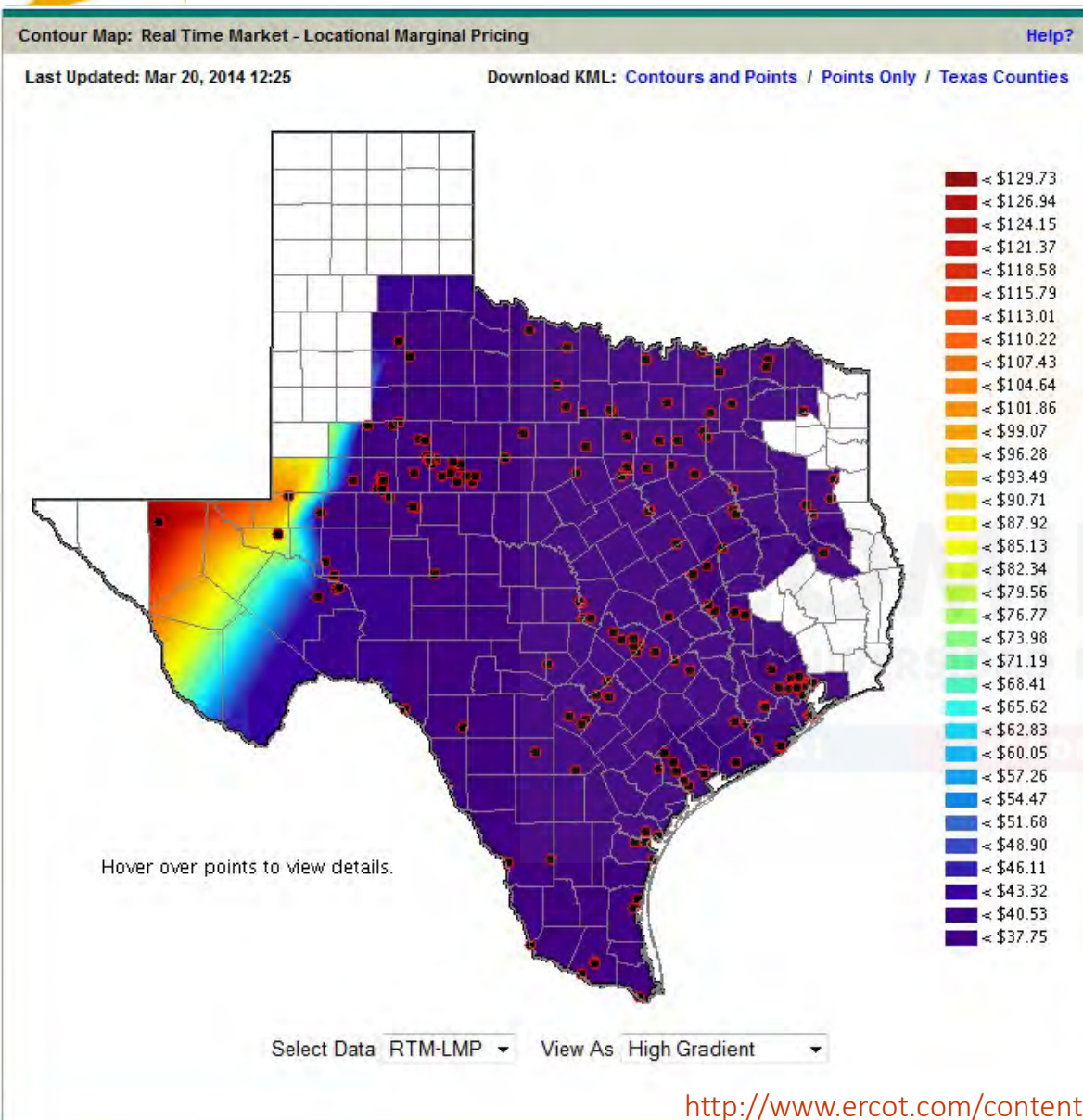
# Maps of Global Horizontal Irradiance (GHI) and Utility-Scale PV Projects



<https://emp.lbl.gov/utility-scale-solar/>

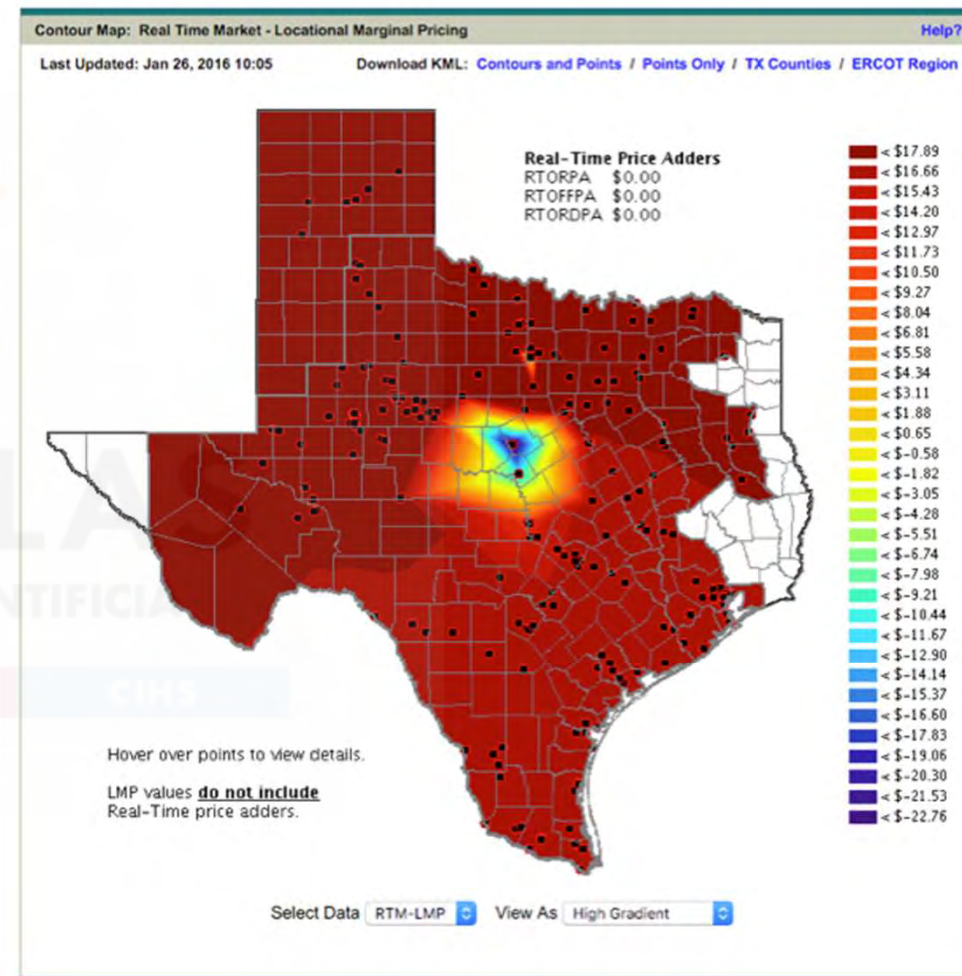
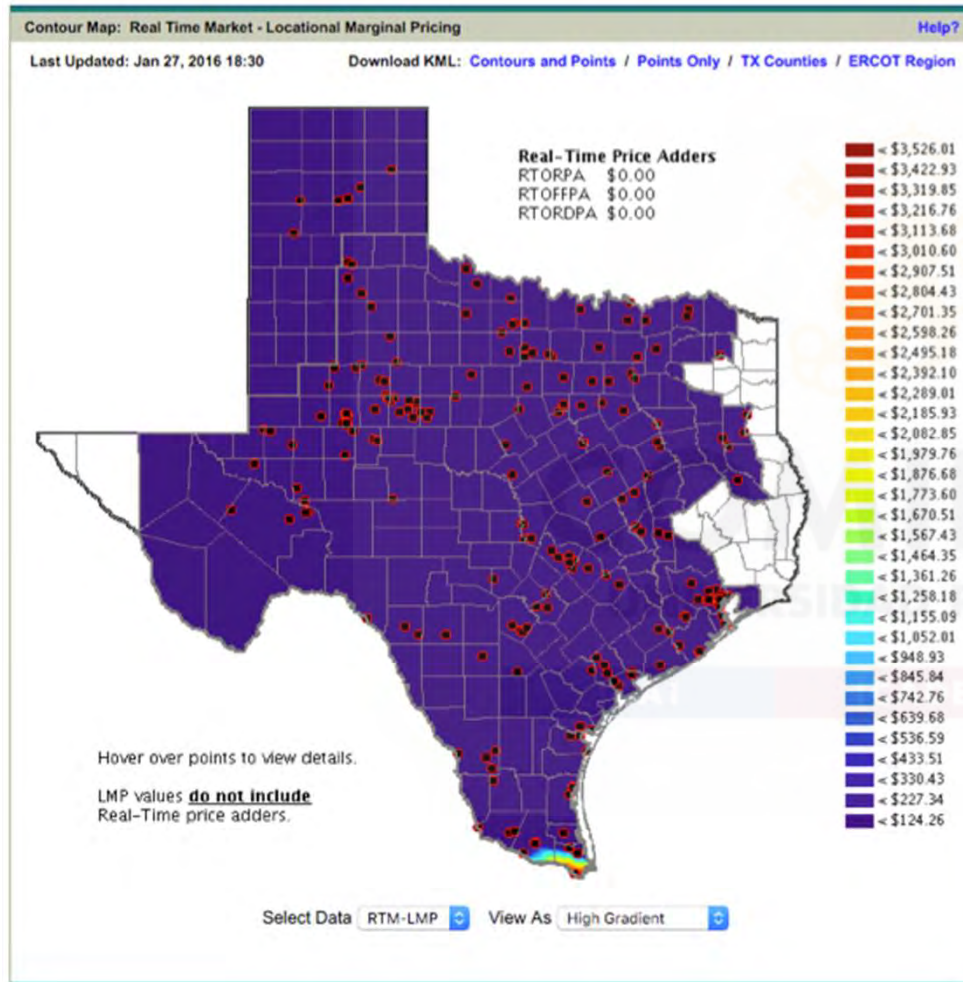


# ERCOT. Locational marginal prices



<http://www.ercot.com/content/cdr/contours/rtmLmpHg.html>

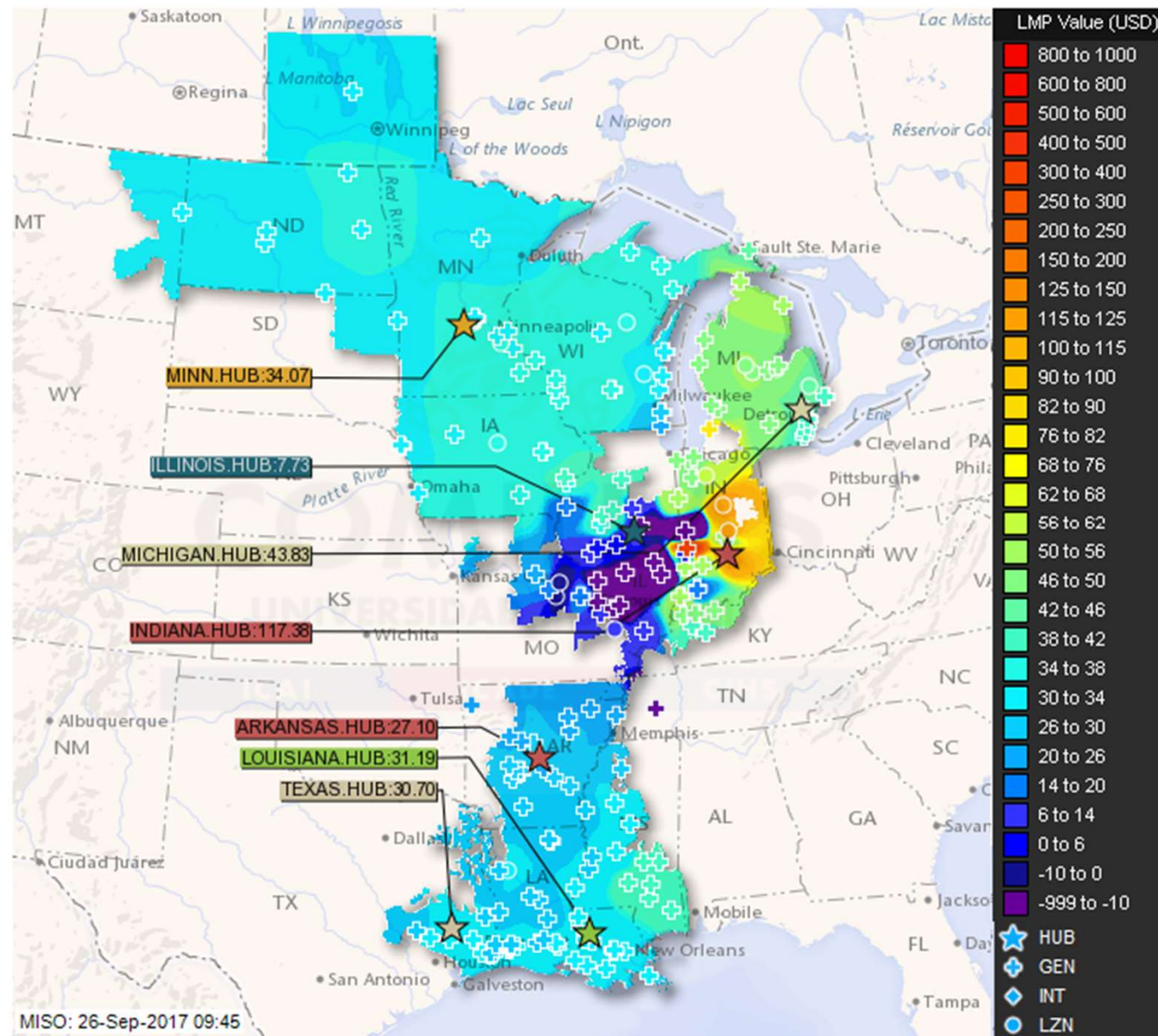
# ERCOT. Locational marginal prices



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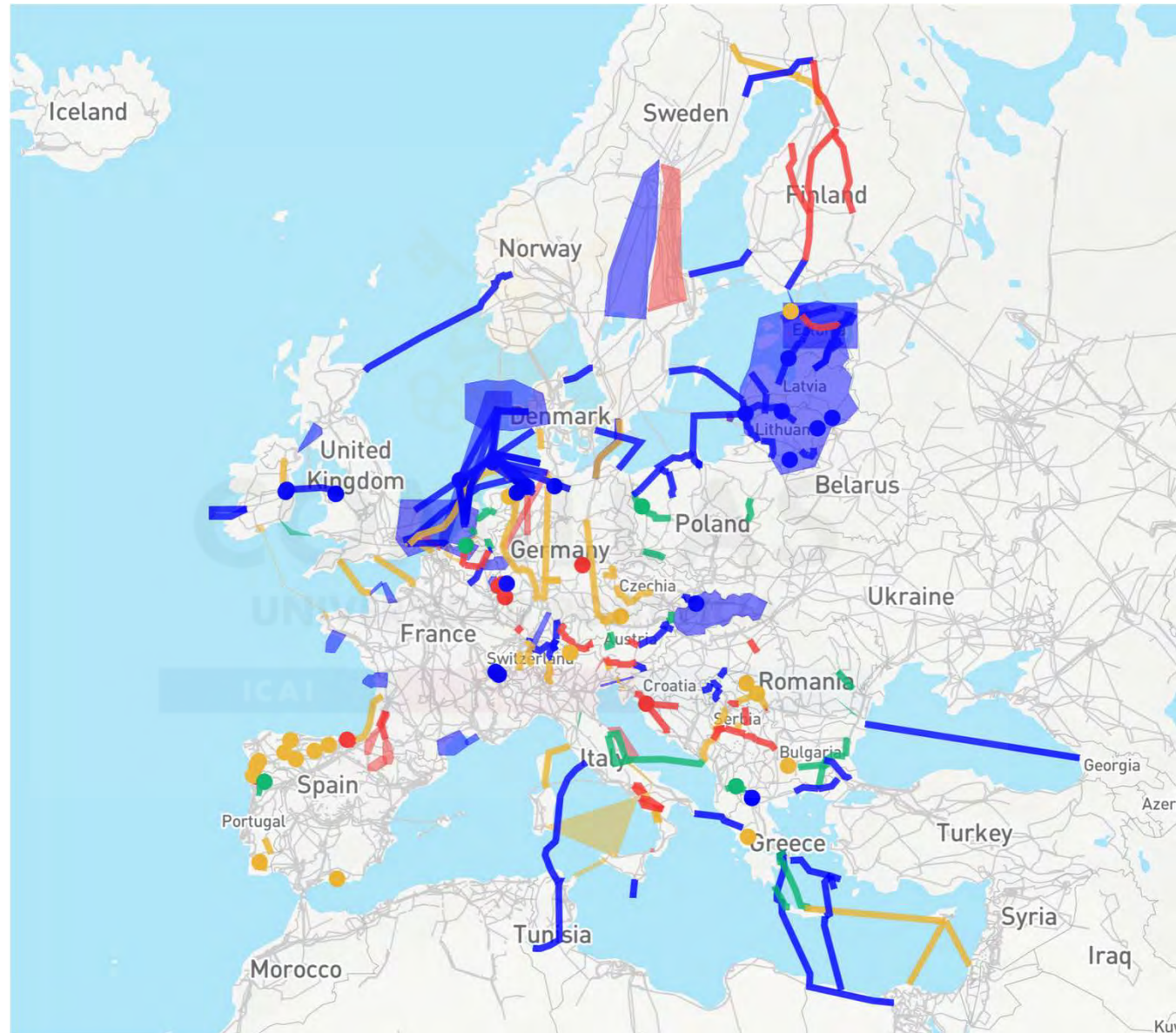


# MISO (Midcontinent Independent System Operator). Locational marginal prices





# (Ten-Year Network Development Plan) TYNDP 2022



# Projects of Common Interest (PCI)

Selected based on five criteria:

1. have a **significant impact on at least two EU countries**
2. **enhance market integration** and contribute to the integration of EU countries' networks
3. **increase competition in energy markets** by offering alternatives to consumers
4. **Improve the security of the supply**
5. **contribute to the EU's energy and climate goals.** They should facilitate the integration of an increasing share of energy from variable renewable energy sources.

[https://ec.europa.eu/energy/topics/infrastructure/projects-common-interest\\_en](https://ec.europa.eu/energy/topics/infrastructure/projects-common-interest_en)

Application of the ENTSO-e cost-benefit analysis method to Aguayo II pumped-hydro storage, developed for **Repsol**. June 2022. [A. Ramos](#), [L. Olmos](#), [L. Sigrist](#)

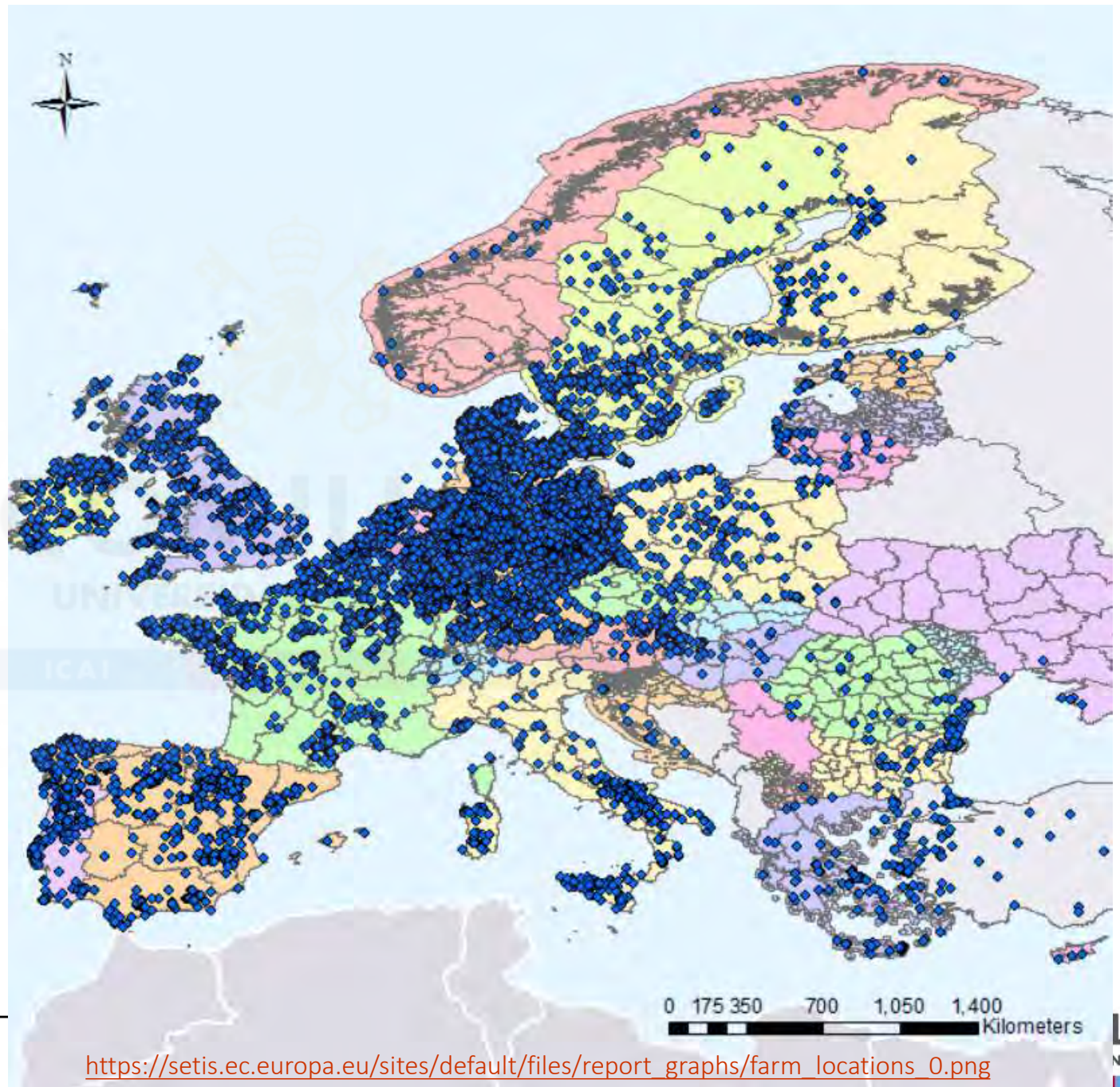
It aims to write a report on the application of the ENTSO-e cost-benefit analysis method to Aguayo II pumped-hydro storage.

Application of the ENTSO-e cost-benefit analysis method to Los Guájares pumped-hydro storage, developed for **VM Energía**. May 2022 - June 2022. [A. Ramos](#), [L. Olmos](#), [L. Sigrist](#)

It aims to write a report on the application of the ENTSO-e cost-benefit analysis method to Los Guájares pumped-hydro storage.

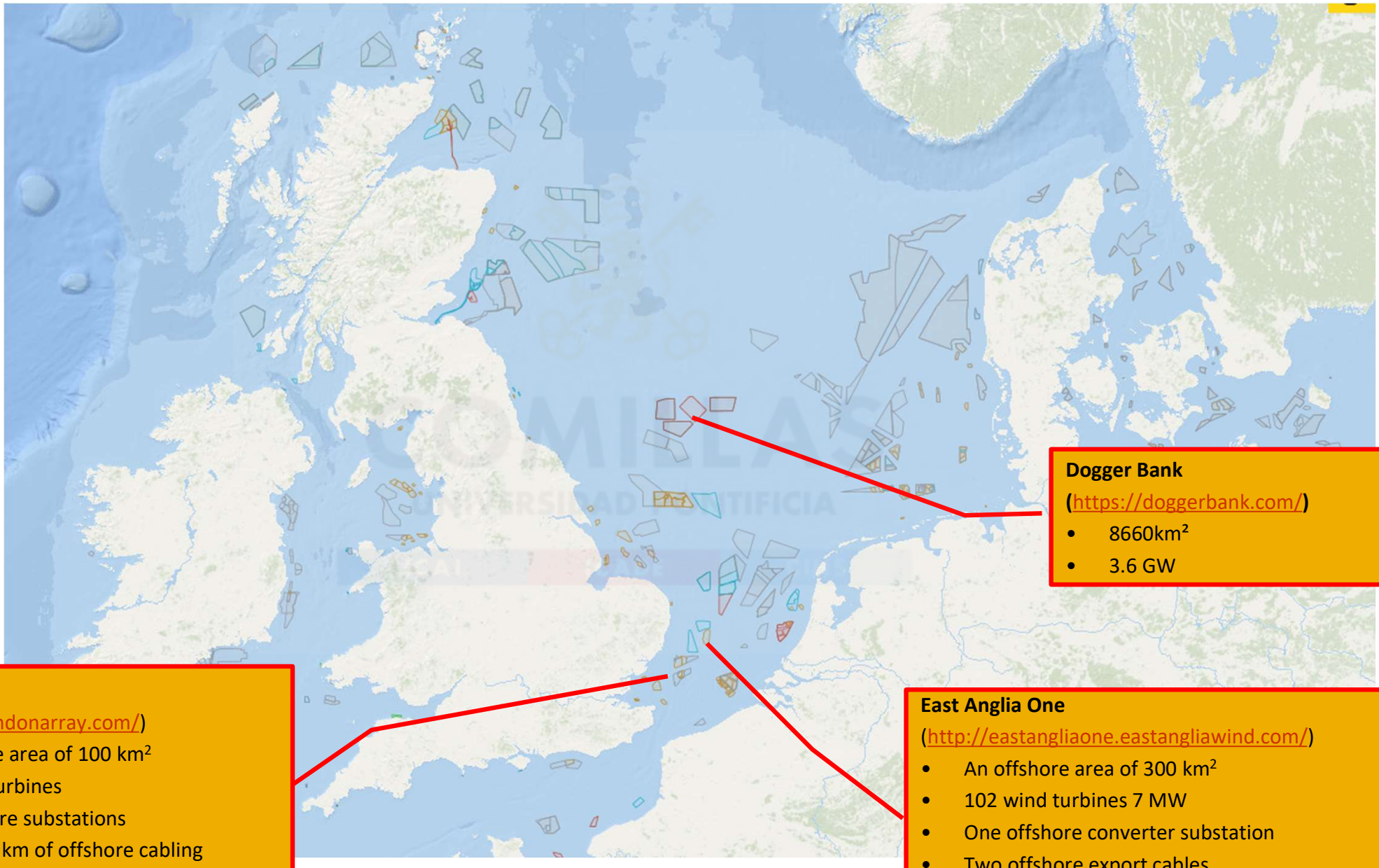


# Map of European wind farms





# Off-shore wind farms in the North Sea and Baltic Sea



**Dogger Bank**  
(<https://doggerbank.com/>)

- 8660km<sup>2</sup>
- 3.6 GW

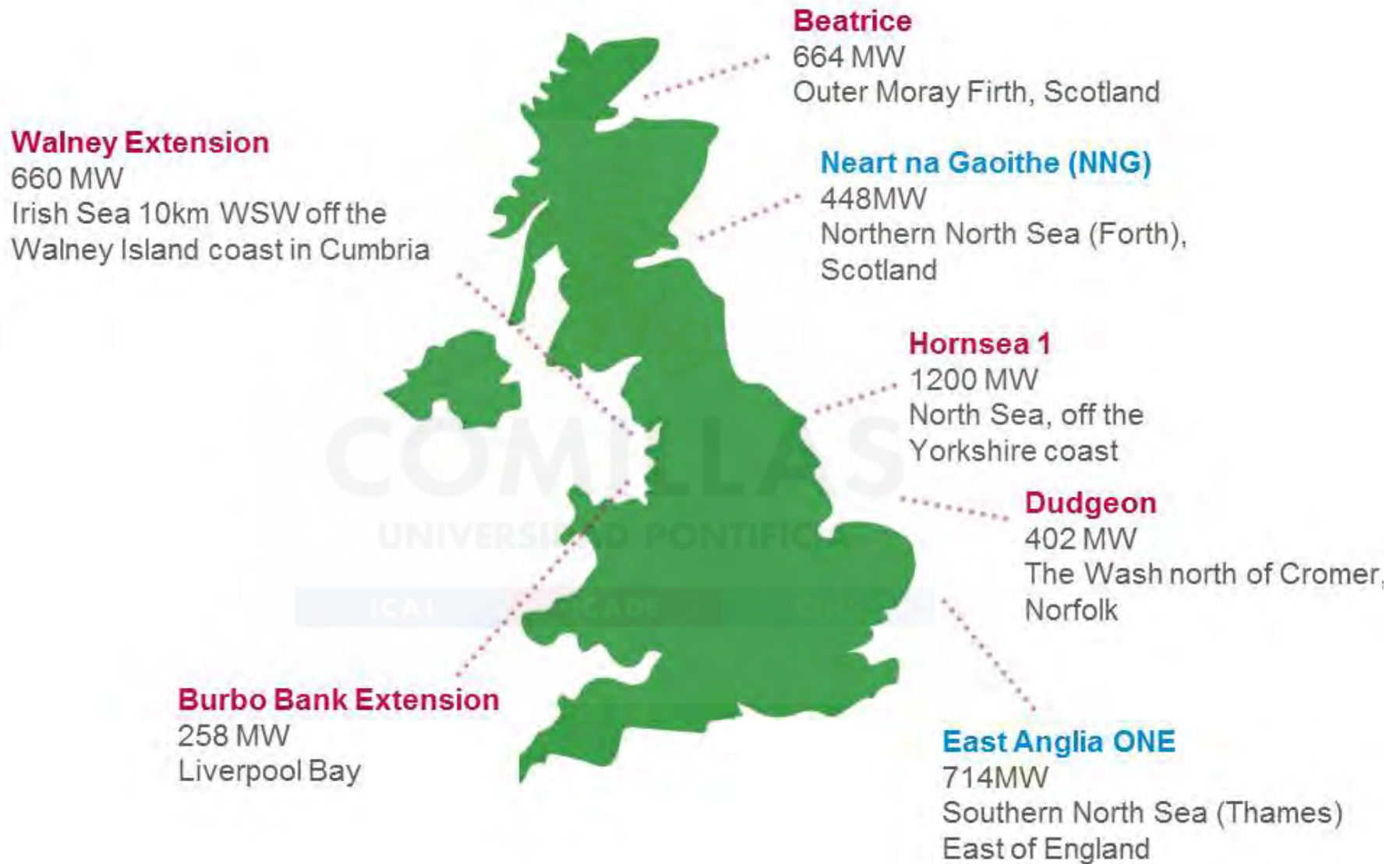
**London Array**  
(<http://www.londonarray.com/>)

- An offshore area of 100 km<sup>2</sup>
- 175 wind turbines
- Two offshore substations
- Nearly 450 km of offshore cabling
- One onshore substation
- 630 MW of capacity

**East Anglia One**  
(<http://eastangliaone.eastangliawind.com/>)

- An offshore area of 300 km<sup>2</sup>
- 102 wind turbines 7 MW
- One offshore converter substation
- Two offshore export cables
- 714 MW of capacity

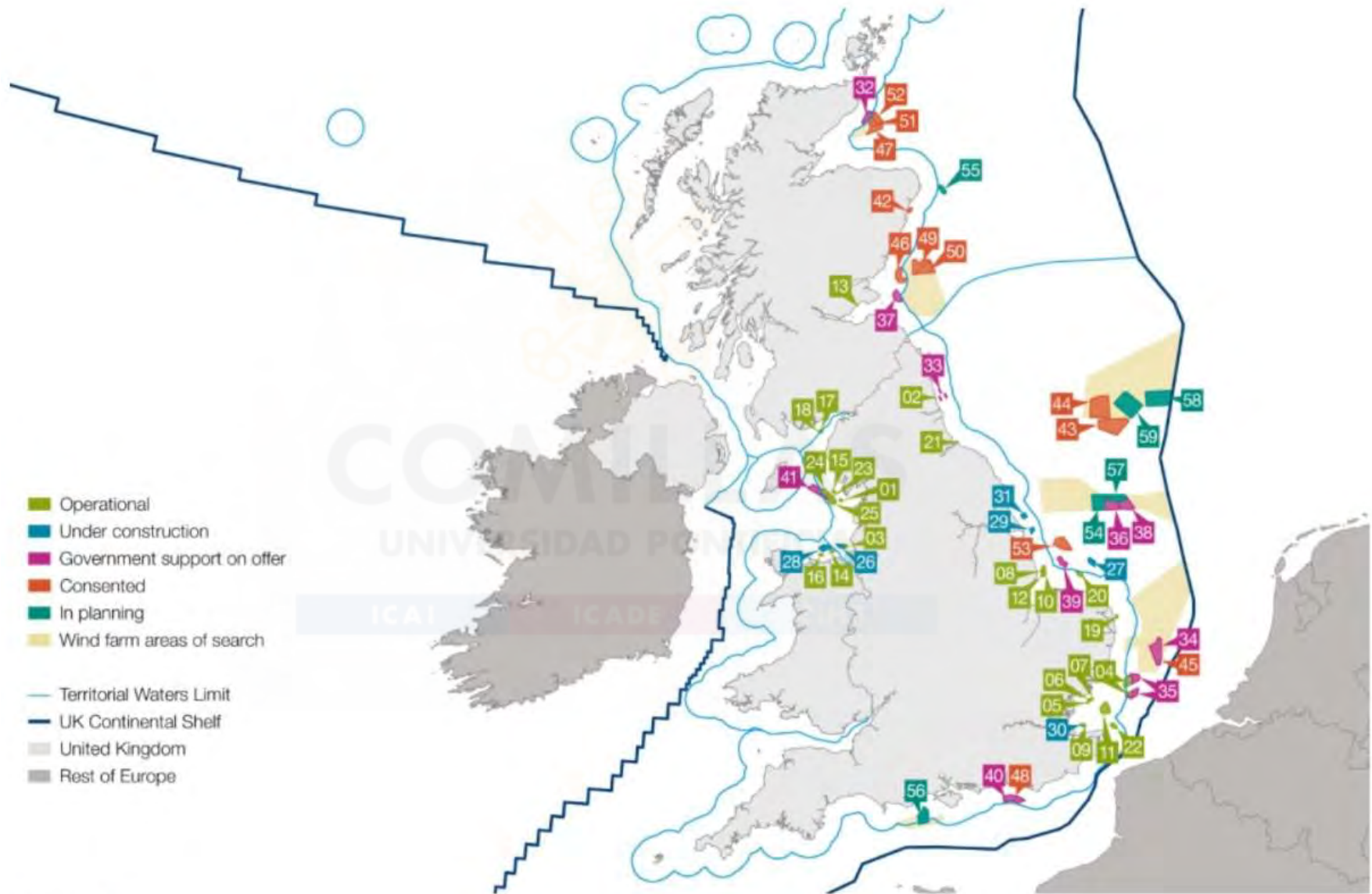
# Projects awarded Contracts for Difference in UK (2015)



<https://www.gov.uk/government/publications/uk-offshore-wind-opportunities-for-trade-and-investment/uk-offshore-wind-opportunities-for-trade-and-investment>



# Offshore wind (UK) map – May 2015

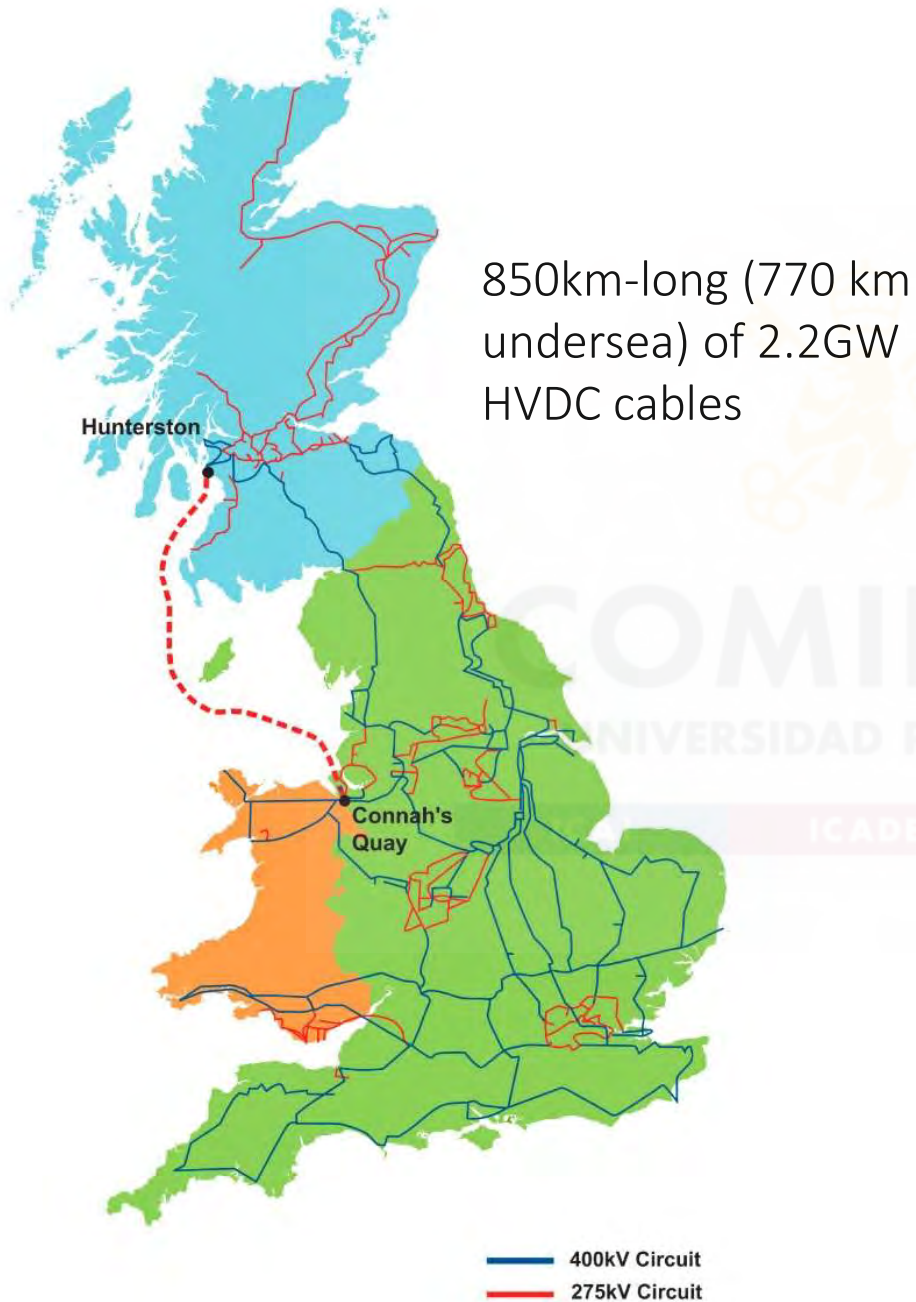


(c) Crown Estate

<https://www.gov.uk/government/publications/uk-offshore-wind-opportunities-for-trade-and-investment/uk-offshore-wind-opportunities-for-trade-and-investment>



# Western Link, UK



# Eastern Green Link 2, UK

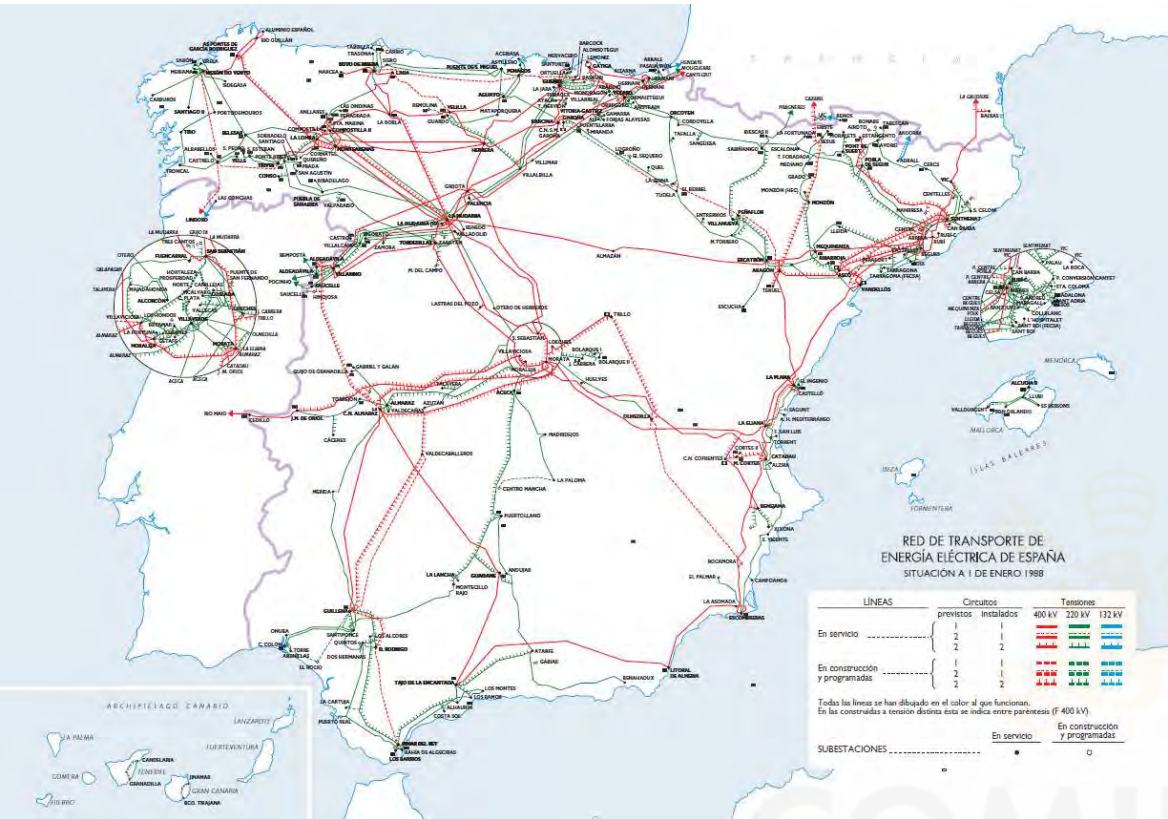
440km-long subsea of two 2GW HVDC cables



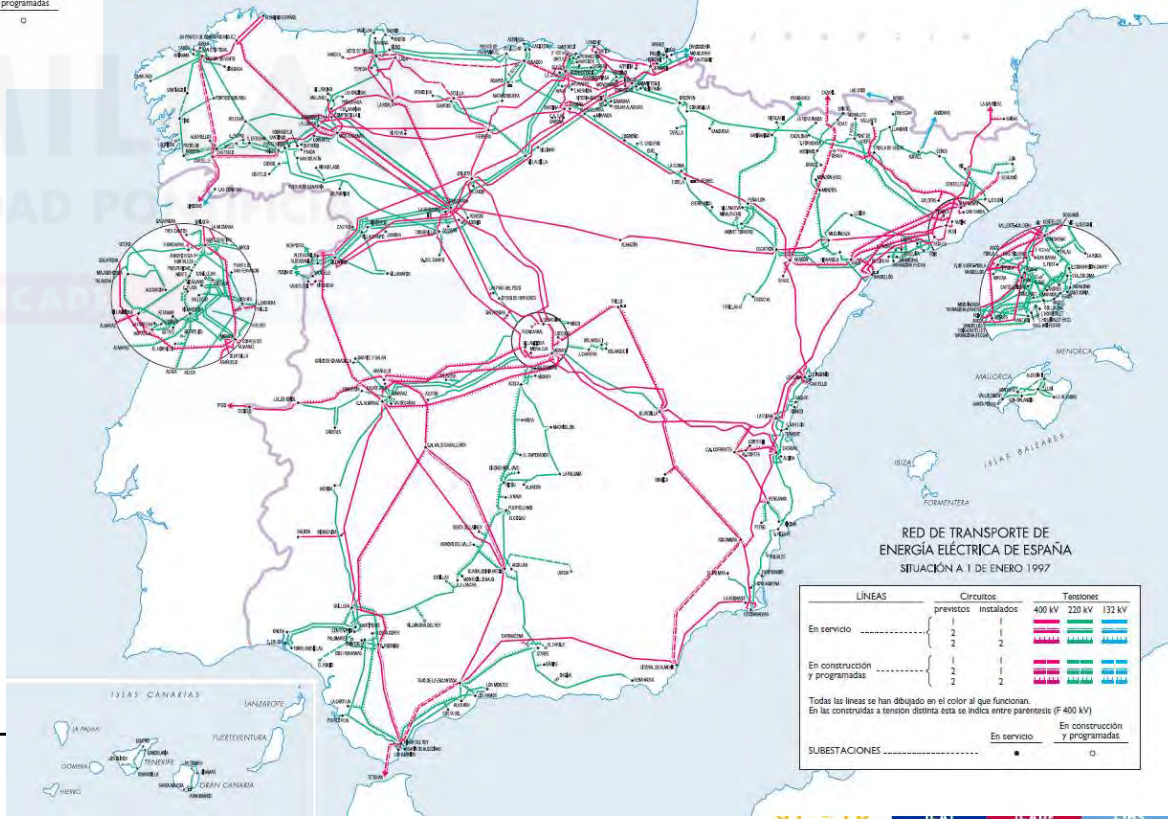
<https://www.iberdrola.com/about-us/lines-business/flagship-projects/eastern-link-electric-underwater-line>



## 1988



## 1997



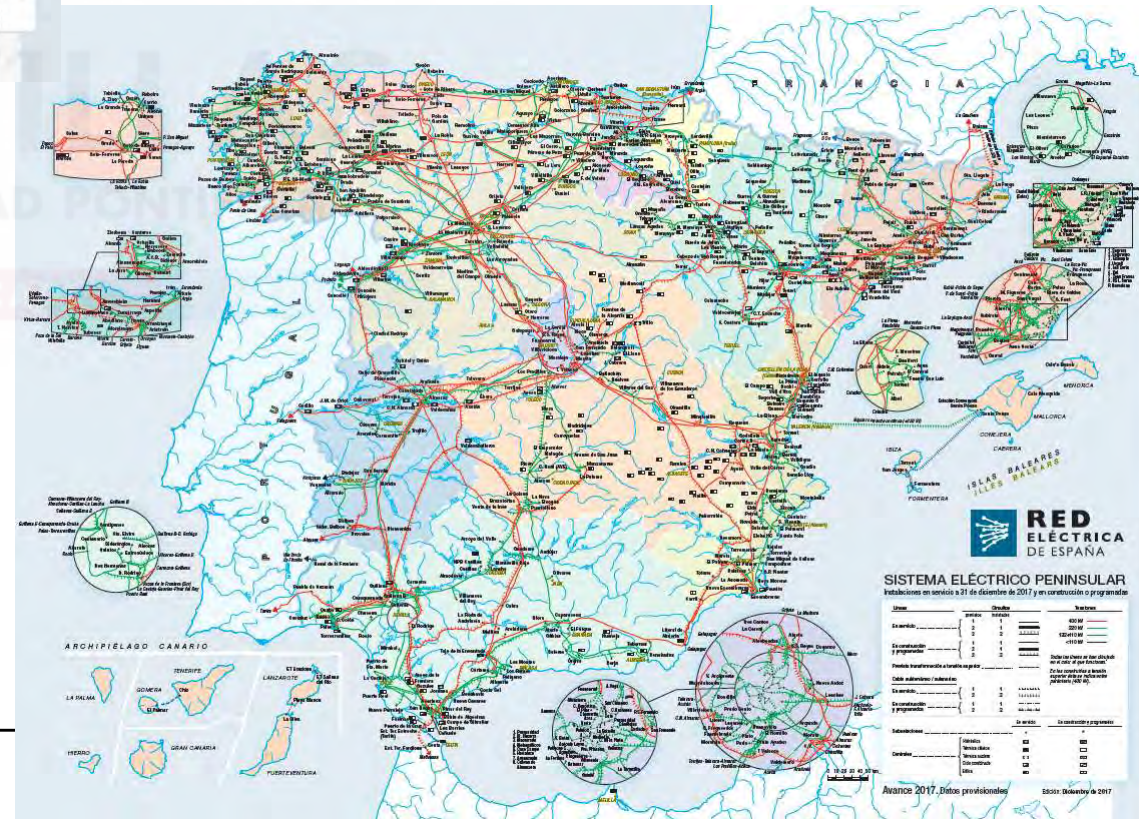


# Spanish Grid

2004

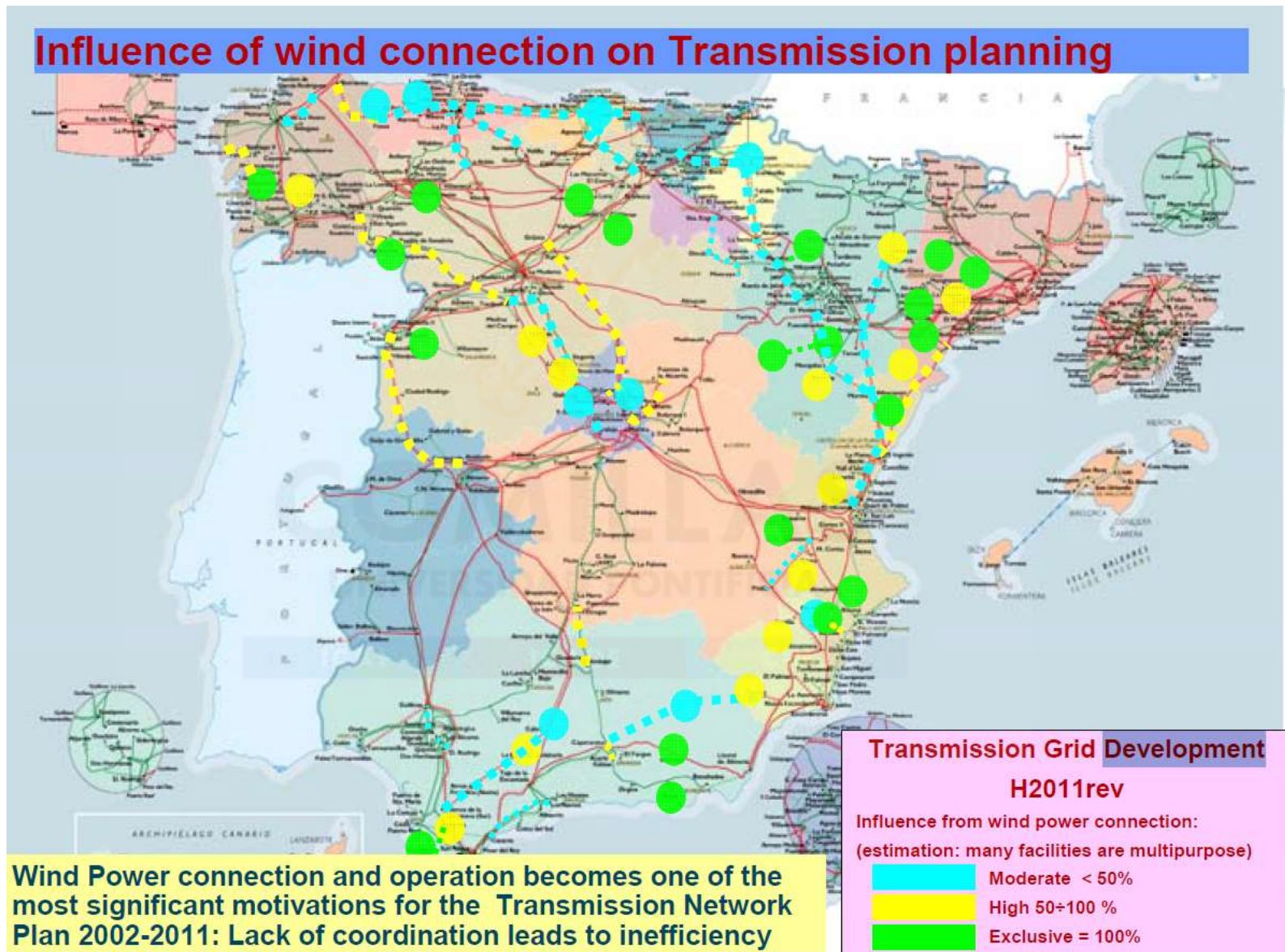


2017





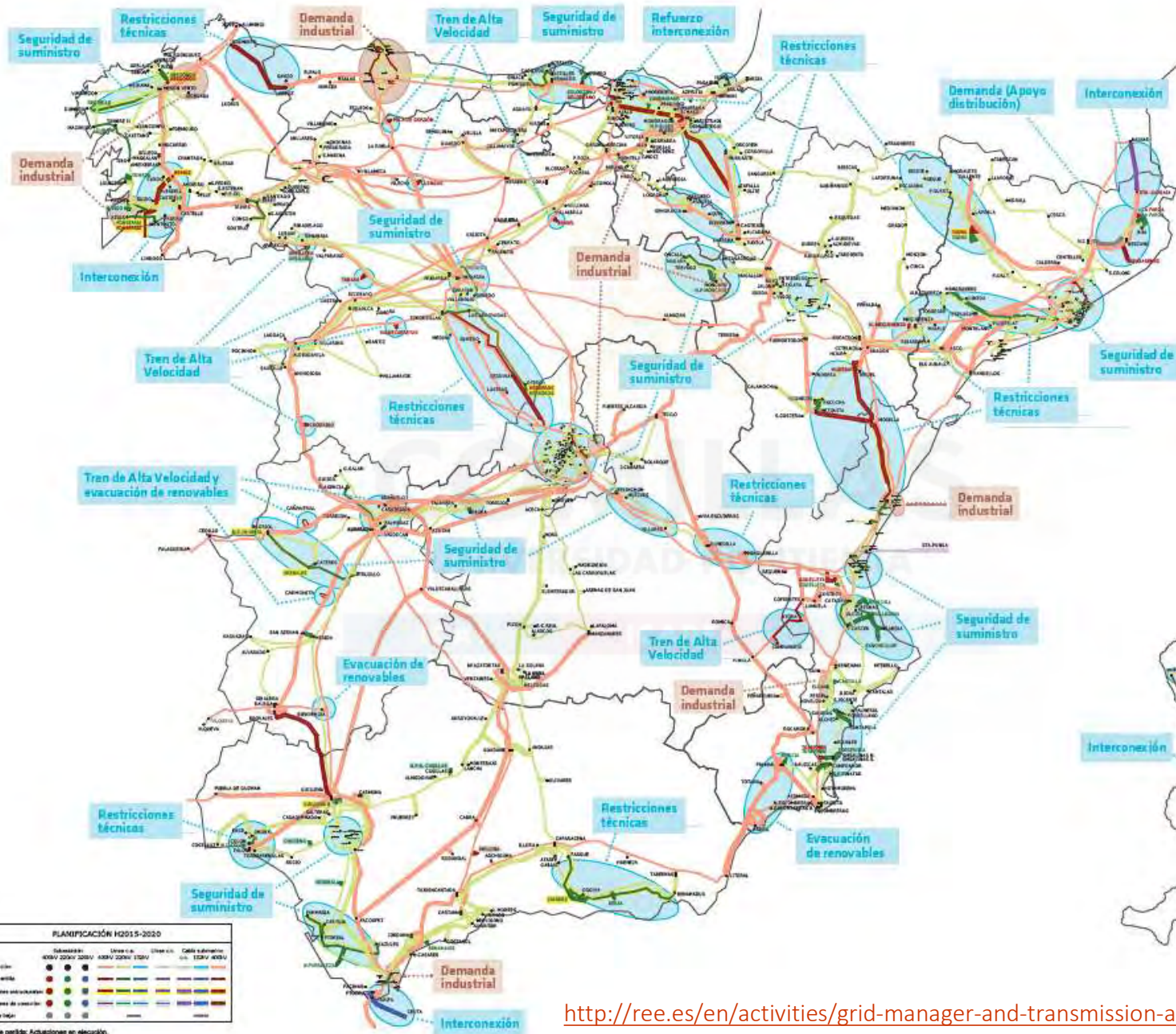
# Influence of wind connection on transmission planning



Source: J.F. Alonso, System Operation Perspective: Connection and Operation Aspects, REE, 2006



# REE Transmission Planning 2015-2020

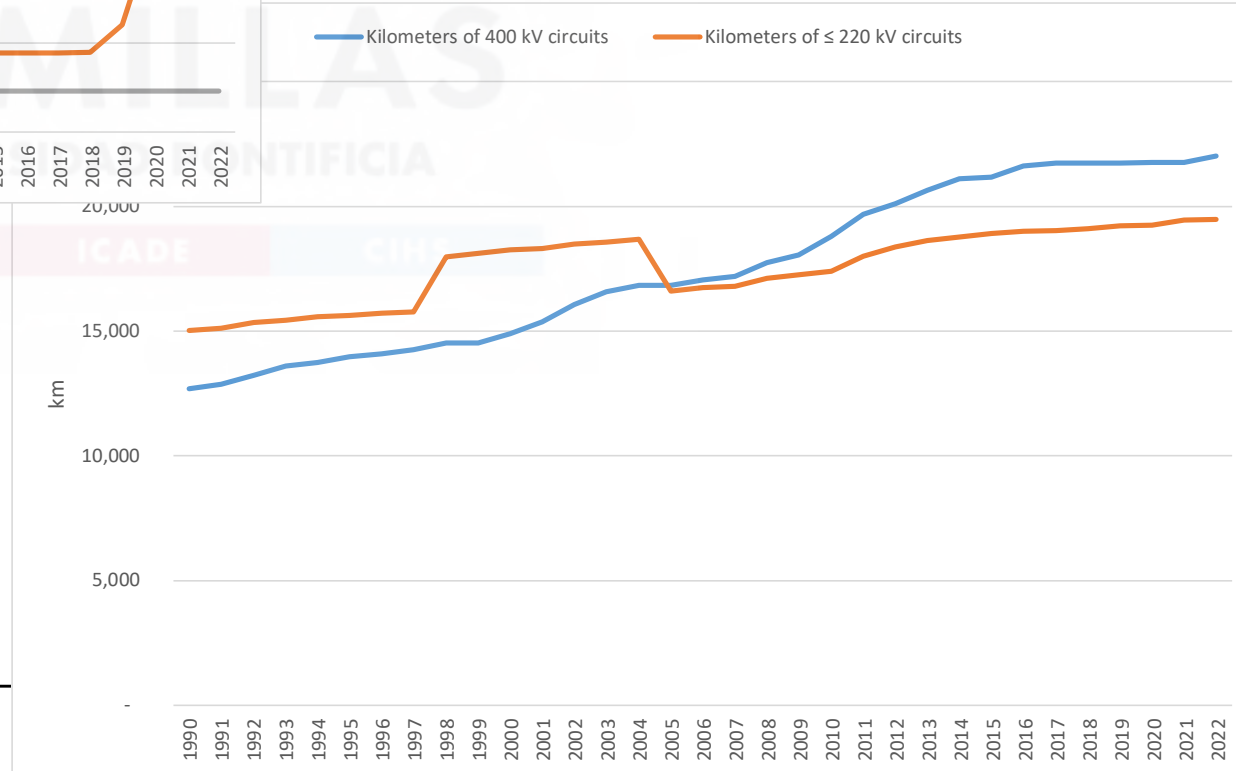
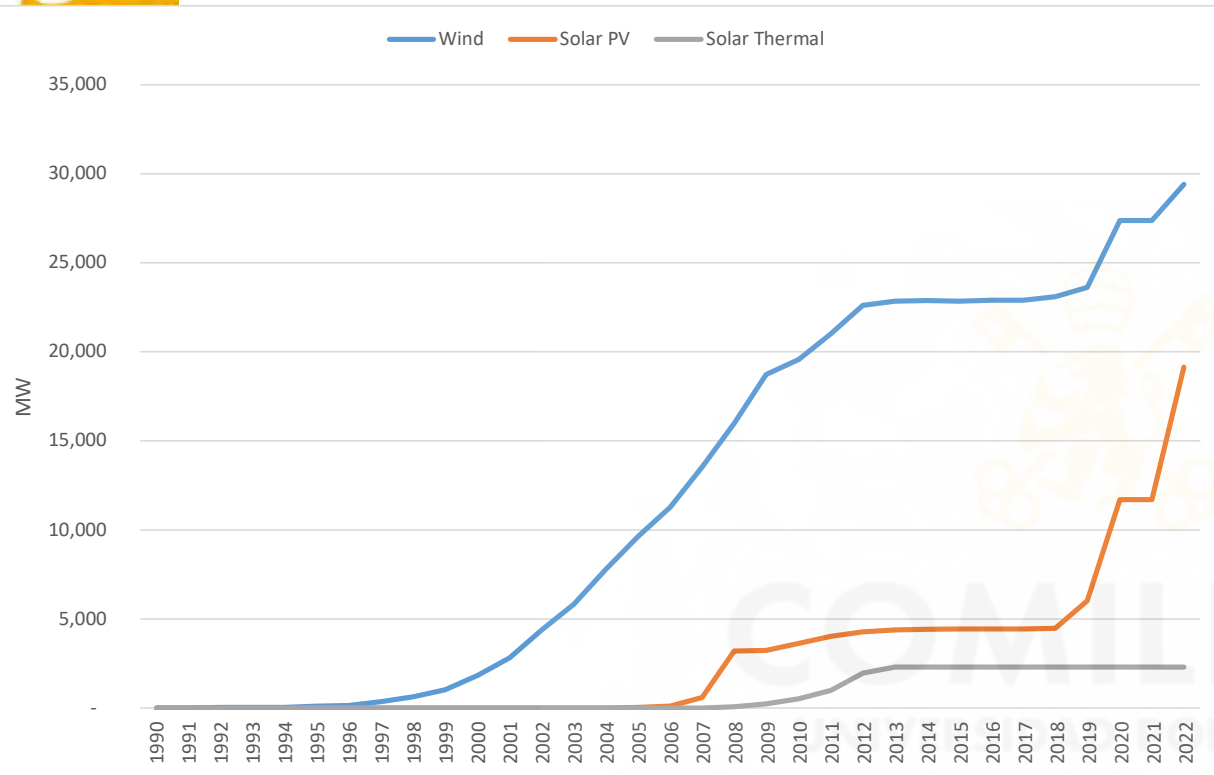


<http://ree.es/en/activities/grid-manager-and-transmission-agent/grid-planning-an-development>





# Spanish high voltage transmission network (1990-2022)



1. Transmission Expansion Planning
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## Simple TEP models



# Centralized TEP model

$$\min \sum_{ij} f'_{ij} IC_{ij} + \sum_t v_t P_t + \sum_i v' ENS_i$$

$$\sum_{t \in i} P_t + \sum_j F_{ji} - \sum_j F_{ij} + ENS_i = D_i \quad \forall i$$

$$F_{ij} - \frac{\theta_i - \theta_j}{X_{ij}} S_B = 0 \quad \forall ij$$

$$-\bar{F}'_{ij} (1 - IC_{ij}) \leq F_{ij} - \frac{\theta_i - \theta_j}{X_{ij}} S_B \leq \bar{F}'_{ij} (1 - IC_{ij}) \quad \forall ij$$

$$-\bar{F}_{ij} \leq F_{ij} \leq \bar{F}_{ij} \quad \forall ij$$

$$-\bar{F}_{ij} IC_{ij} \leq F_{ij} \leq \bar{F}_{ij} IC_{ij} \quad \forall ij$$

$$\theta_i \text{ free}, \theta_{i^*} = 0$$

$$0 \leq ENS_i \leq D_i \quad \forall i$$

$$0 \leq P_t \leq \bar{P}_t \quad \forall t$$

$$IC_{ij} \in \{0, 1\} \quad \forall ij$$

Transmission investment cost + thermal variable costs + ENS cost

Generation and load balance for each node

DC linearized load flow for existing and candidate lines

Flow limits for existing & candidate lines. Reference voltage angle

Thermal operating bounds

Investment decisions

## Market TEP model

- No longer exists coordination between generation operation and TEP
- Conceptual solution of the market equilibrium with network expansion decisions
  - TSO decides first: **Proactive** investment
    - **Stackelberg leader-multi-follower game** stated as a **bilevel optimization**
  - TSO reacts to generation investments: **Reactive** investment
- **Financial Transmission Rights (FTR)** can help in solving this dilemma

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# TSO (Transmission System Operator) optimization problem

- O.F.: Investment cost minimization and computation of nodal prices
- Constraints: load flow equations

$$\min \sum_{ij} f'_{ij} IC_{ij} + \sum_i v' ENS_i$$

$$\sum_{t \in i} P_t + \sum_j F_{ji} - \sum_j F_{ij} + ENS_i = D_i \quad \text{: } \pi_i \quad \forall i$$

$$F_{ij} - \frac{\theta_i - \theta_j}{X_{ij}} S_B = 0 \quad \forall ij$$

$$-\bar{F}'_{ij} (1 - IC_{ij}) \leq F_{ij} - \frac{\theta_i - \theta_j}{X_{ij}} S_B \leq \bar{F}'_{ij} (1 - IC_{ij}) \quad \forall ij$$

$$-\bar{F}_{ij} \leq F_{ij} \leq \bar{F}_{ij} \quad \forall ij$$

$$-\bar{F}_{ij} IC_{ij} \leq F_{ij} \leq \bar{F}_{ij} IC_{ij} \quad \forall ij$$

$$\theta_i \text{ free}, \theta_{i^*} = 0$$

$$0 \leq ENS_i \leq D_i$$

$$IC_{ij} \in \{0, 1\}$$

Transmission investment cost

Generation and load balance for each node

DC linearized load flow for existing and candidate lines

Flow limits for existing & candidate lines. Reference voltage angle

ENS bounds

Investment decisions

# GenCo profit maximization problem

- O.F.: Maximize its profit given nodal prices
- Constraints: generation operation

$$\begin{aligned} \max \quad & \sum_i \sum_{t \in i} \pi_i P_t - \sum_t v_t P_t \\ & 0 \leq P_t \leq \bar{P}_t \quad \forall t \end{aligned}$$

Thermal revenues - variable costs

Thermal operating bounds



# GenCos market equilibrium problem (MEP)

- Each company solves independently its own profit maximization problem

*Gen Company 1*

$$\begin{aligned} \max \quad & \sum_i \sum_{t \in i} \pi_i P_t - \sum_t v_t P_t \\ 0 \leq P_t \leq \bar{P}_t \quad & \forall t \end{aligned}$$

*Gen Company e*

$$\begin{aligned} \max \quad & \sum_i \sum_{t \in i} \pi_i P_t - \sum_t v_t P_t \\ 0 \leq P_t \leq \bar{P}_t \quad & \forall t \end{aligned}$$

*Gen Company E*

$$\begin{aligned} \max \quad & \sum_i \sum_{t \in i} \pi_i P_t - \sum_t v_t P_t \\ 0 \leq P_t \leq \bar{P}_t \quad & \forall t \end{aligned}$$

# Overall MEP + TEP

Bilevel  
optimization

*TSO*

$$\min \sum_{ij} f'_{ij} IC_{ij} + \sum_i v' ENS_i$$

$$\sum_{t \in i} P_t + \sum_j F_{ji} - \sum_j F_{ij} + ENS_i = D_i \quad : \pi_i \quad \forall i$$

$$F_{ij} - \frac{\theta_i - \theta_j}{X_{ij}} S_B = 0 \quad \forall ij$$

$$-\bar{F}'_{ij} (1 - IC_{ij}) \leq F_{ij} - \frac{\theta_i - \theta_j}{X_{ij}} S_B \leq \bar{F}'_{ij} (1 - IC_{ij}) \quad \forall ij$$

$$-\bar{F}_{ij} \leq F_{ij} \leq \bar{F}_{ij} \quad \forall ij$$

$$-\bar{F}_{ij} IC_{ij} \leq F_{ij} \leq \bar{F}_{ij} IC_{ij} \quad \forall ij$$

$$\theta_i \text{ free}, \theta_{i^*} = 0$$

$$0 \leq ENS_i \leq D_i \quad \forall i$$

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*Gen Company 1*

$$\max \sum_i \sum_{t \in i} \pi_i P_t - \sum_t v_t P_t$$

$$0 \leq P_t \leq \bar{P}_t \quad \forall t$$

*Gen Company e*

$$\max \sum_i \sum_{t \in i} \pi_i P_t - \sum_t v_t P_t$$

$$0 \leq P_t \leq \bar{P}_t \quad \forall t$$

*Gen Company E*

$$\max \sum_i \sum_{t \in i} \pi_i P_t - \sum_t v_t P_t$$

$$0 \leq P_t \leq \bar{P}_t \quad \forall t$$



1. Transmission Expansion Planning
2. Simple TEP models
3. **Modeling issues**
4. Prototype TEP. Mathematical formulation
5. Prototype TEP. Computer implementation
6. Takeaways

3

## Modeling issues

# Challenges for Transmission Expansion Planning (TEP)



*Spatial complexity: Europe to smart cities*



*Temporal complexity: msec. to decades*

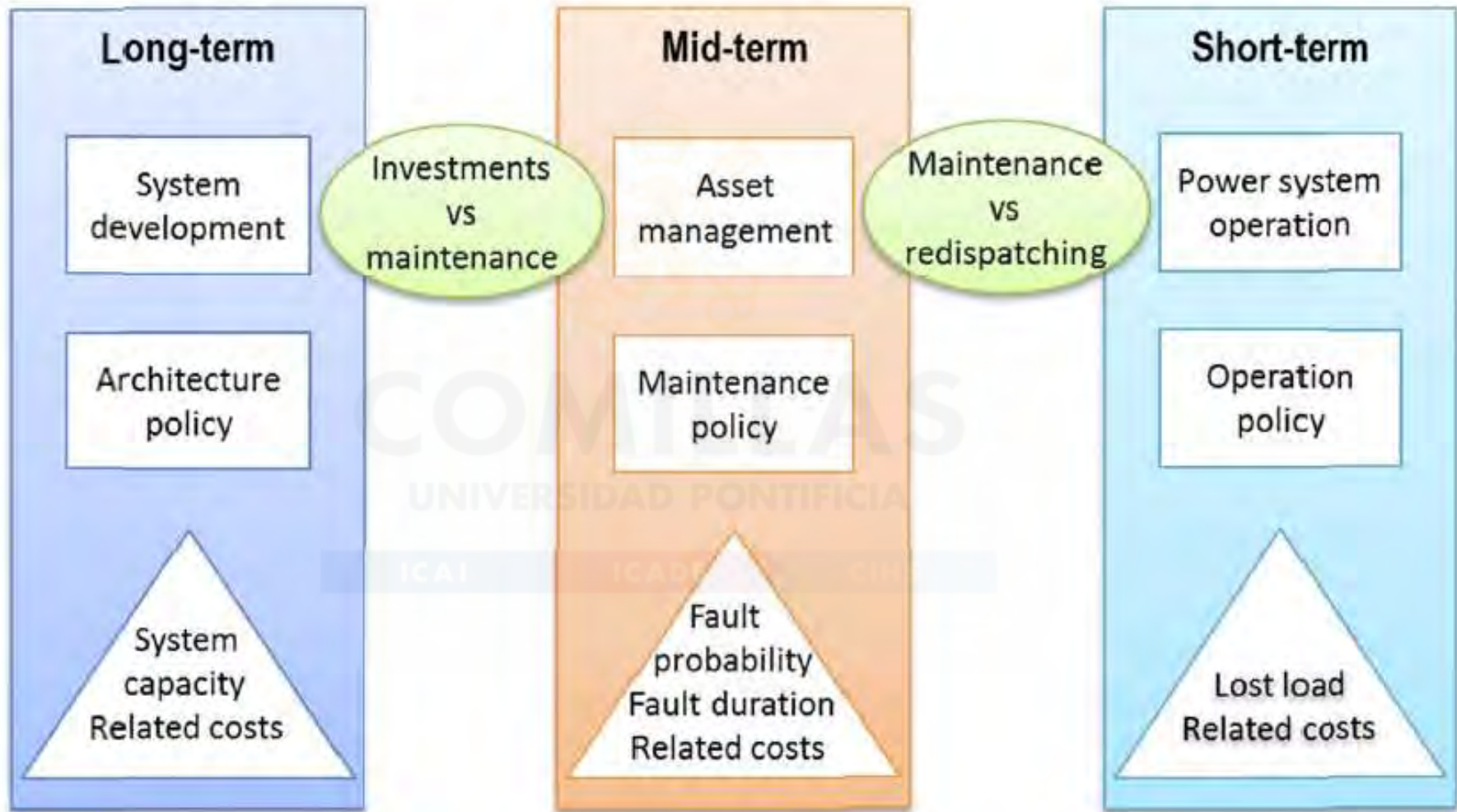


*Stochastic complexity: weather conditions and human behaviors*





# TSO (Transmission System Operator) activities



Source: GARPUR Project. D1.1 State of the art on reliability assessment in power systems <http://www.garpur-project.eu/deliverables>

# Time scopes

- Long-term (tactical) (5-10 years)
  - Specific decisions for network development
  - More detailed models are required
  - Analysis of proposed plans is the main objective
- Very long-term (strategic) (10-20 years)
  - Guidelines for network development
  - Simpler models are acceptable
  - New corridors are the main objective to determine





# Characteristics of the TEP

- Very complex decision problem with **multiple criteria**
- Important **strategic decision**. Decisions require **very long building periods** and have **long book life**
- **Generation planning decisions** strongly affect transmission planning decisions
  - Wind and solar far from load centers
- Generation operation decisions and constraints are a subset of the transmission expansion problem. A large-scale transmission planning problem
  - Large and **correlated variations of renewable sources** cause interdependency power flows in large regions
  - **Spatial correlation** in generation profiles (wind and solar)
  - **Sudden temporal changes** from one day to another



# Why coordination between generation and transmission expansion planning?

- **Independent entities make decisions**
  - Private generation companies
  - Publicly owned transmission system operators
- With **different periods in advance**
  - Several years for generation investment
  - A decade for transmission investment

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# Proactive and reactive investment game

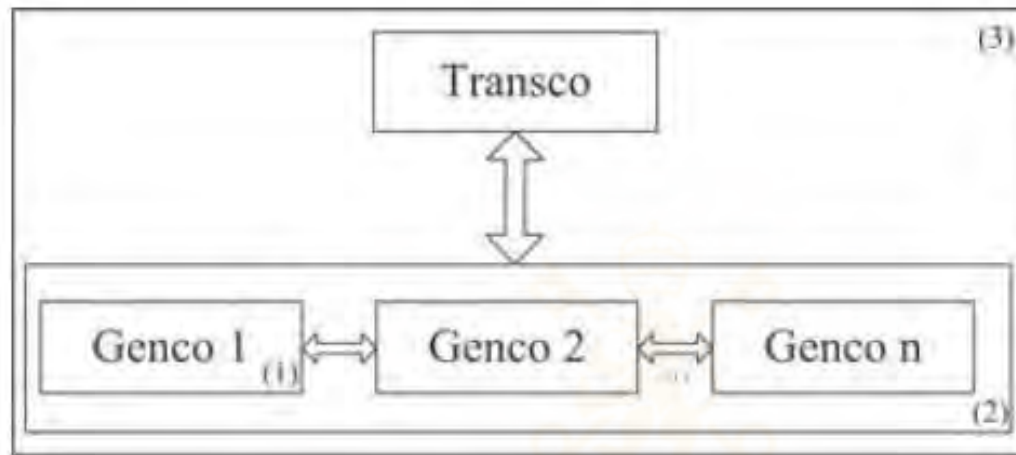


Figure 4.2: The proactive approach for generation-transmission investment game

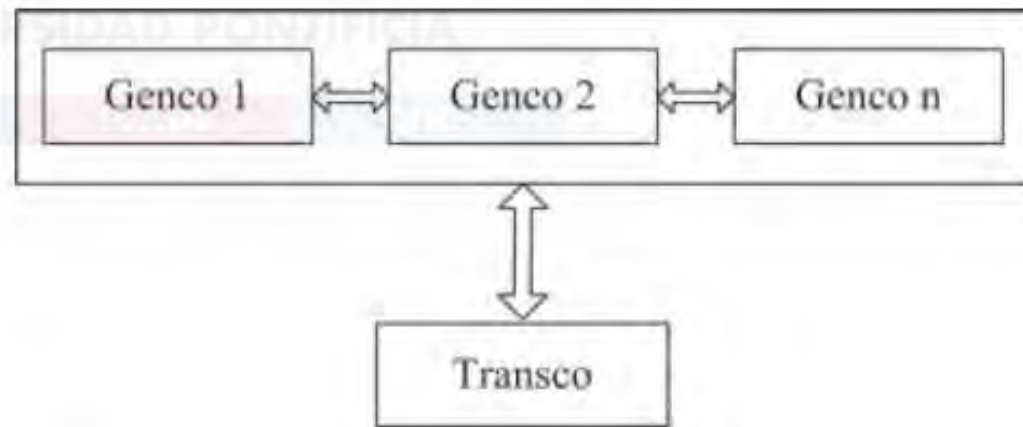


Figure 4.3: The reactive approach for generation-transmission investment game

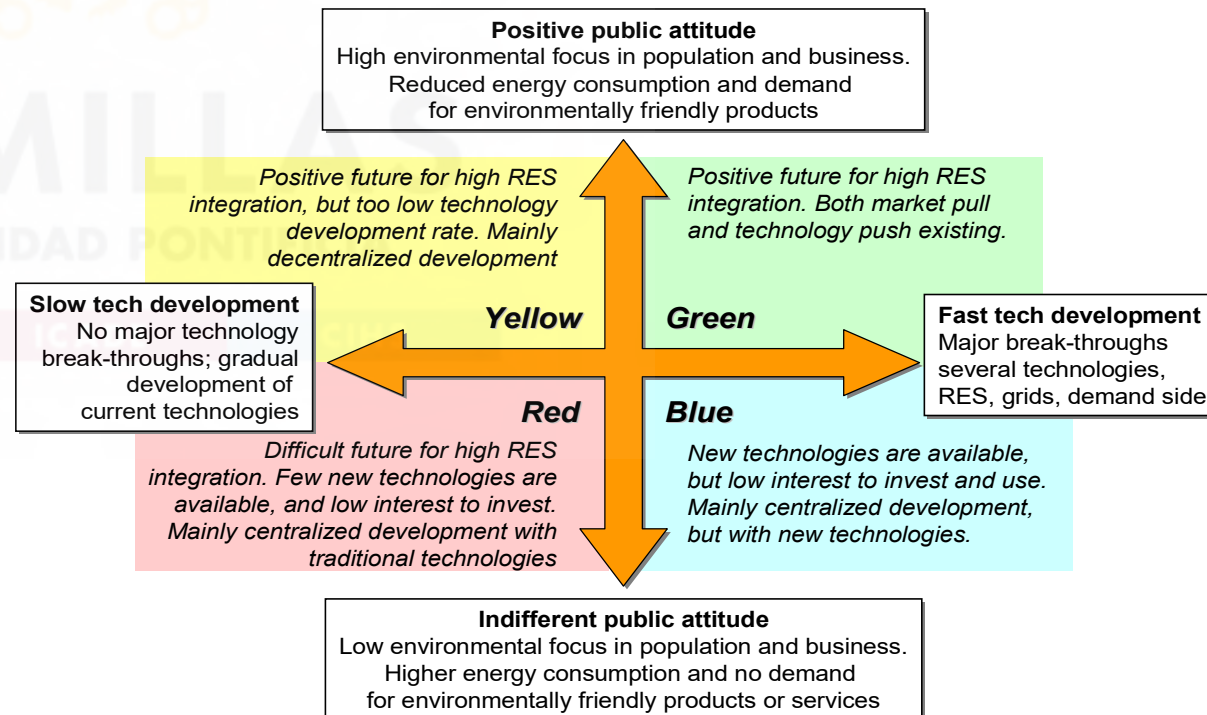
Y. Tohidi *Optimal Long-Term Generation-transmission Planning in the Context of Multiple TSOs*. PhD Thesis. KTH, 2016

# General Scope

## Generation Expansion Planning (GEP) or Integrated Resource Planning (IRP)

- GEP included in the optimization: GEP+TEP
- GEP as an external input
  - Single future scenario vs. uncertain GEP

Implies using methods to cope with non-random uncertainties (exogenous storylines/pathways/options)





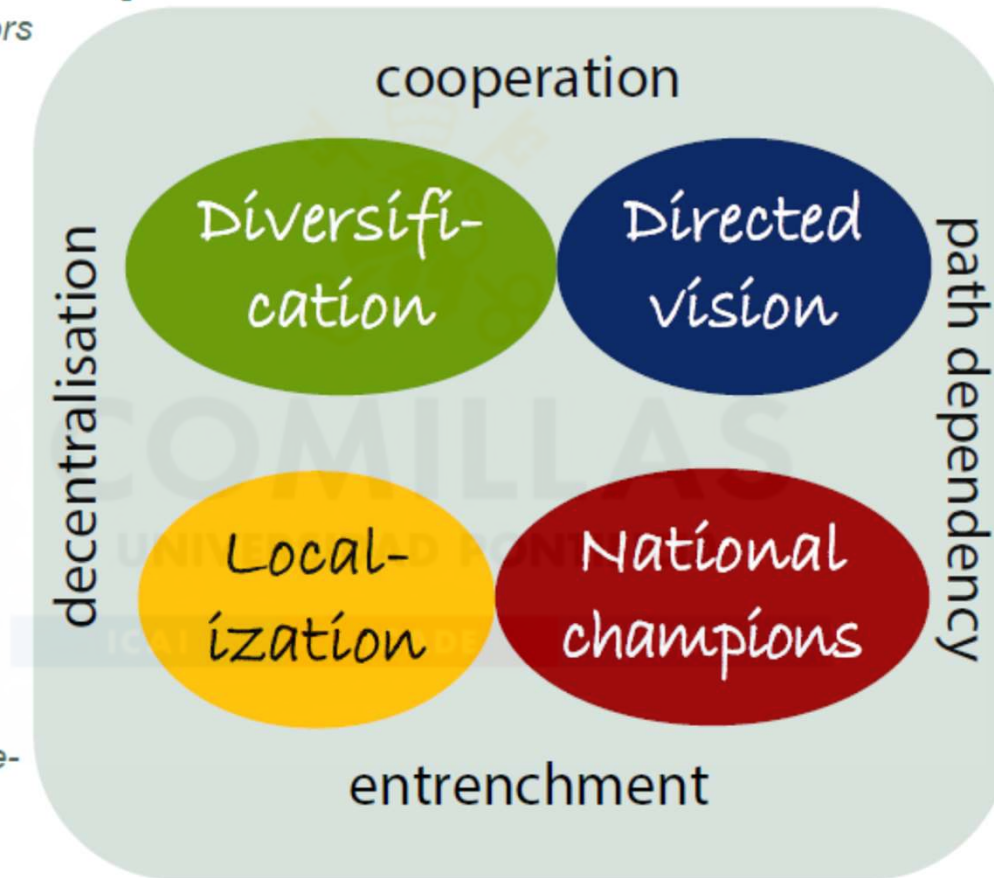
# Future storylines for SET-Nav project

(<http://www.set-nav.eu/>)

## Pathway analysis: **Pathway definition / Storylines**

- heterogeneous actors
- coordination (beyond markets)
- digitalization (open IP)
- regulatory change
- disrupt incumbents

- local resources
- resistance to big infrastructure
- experimentation & diversity (many niches)
- digital winners-take-all



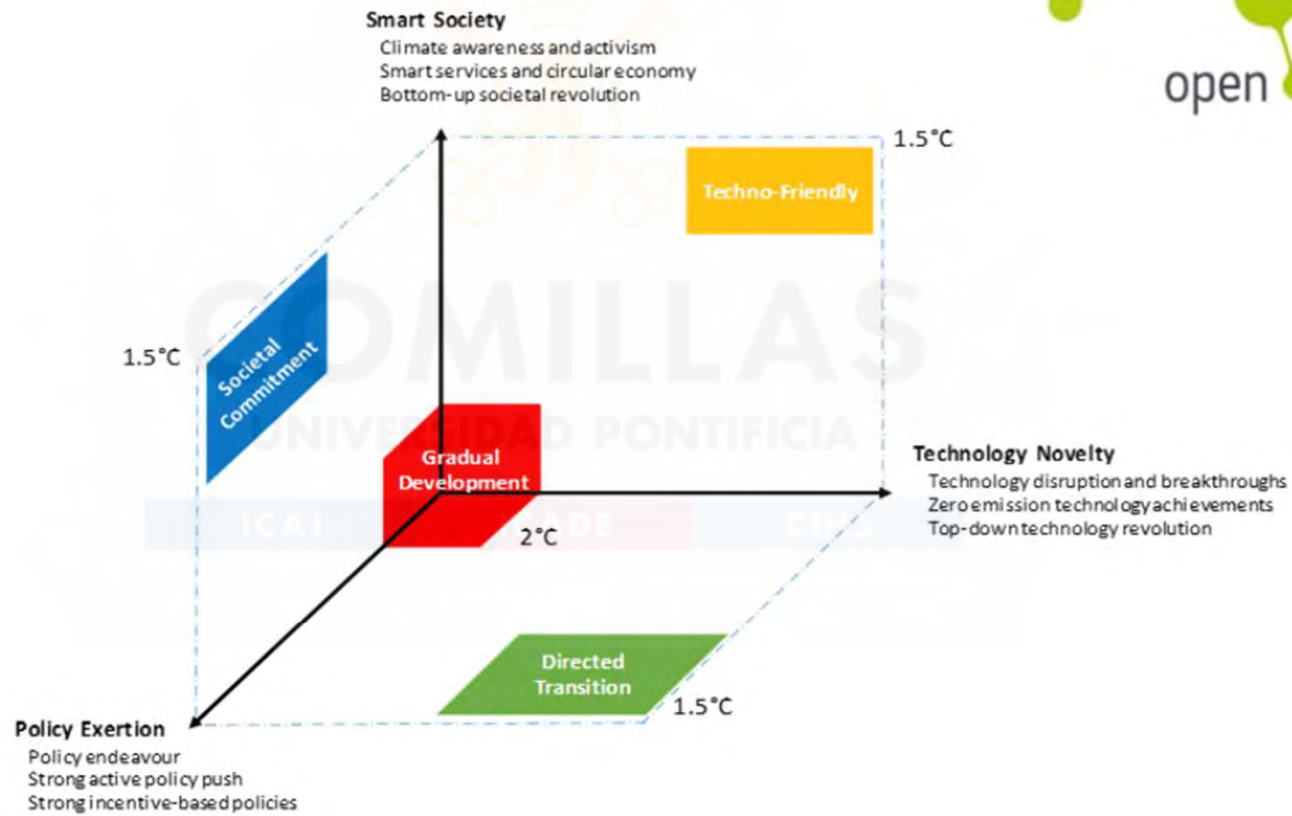
- EU/state-directed
- shared vision
- strong EU policy framework

- utilities & incumbents
- regulatory capture
- low transition costs

# Future storylines for openENTRANCE project

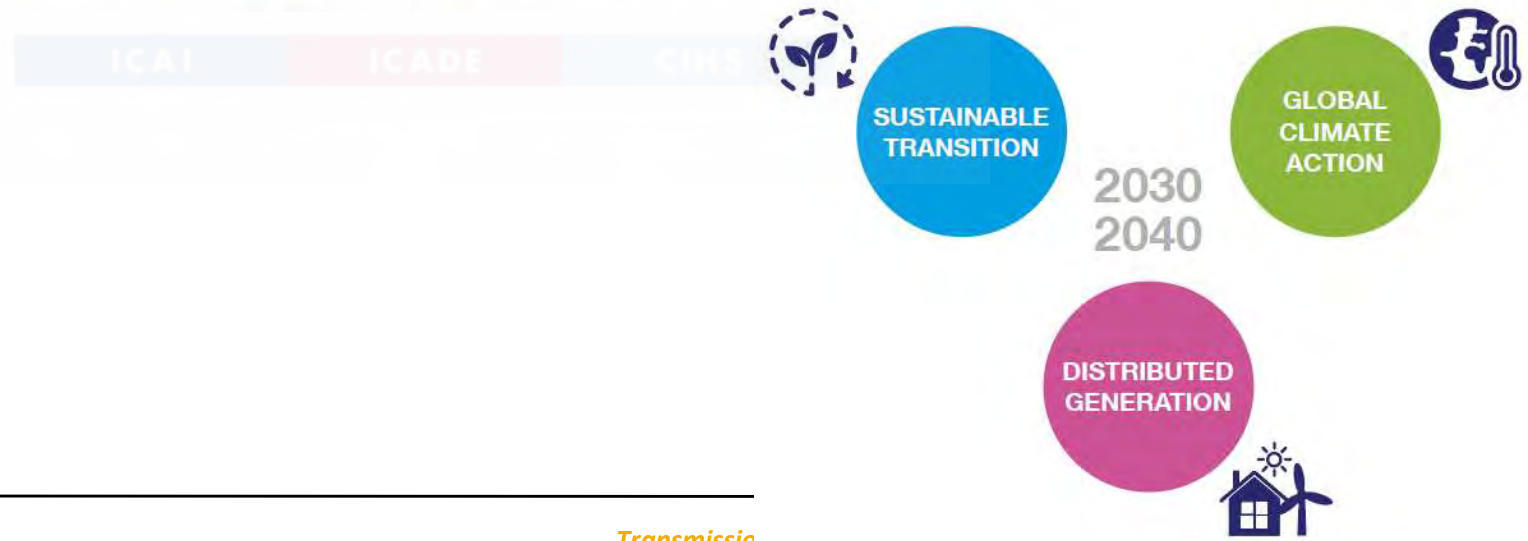
(<https://openentrance.eu/>)

## openENTRANCE Storylines

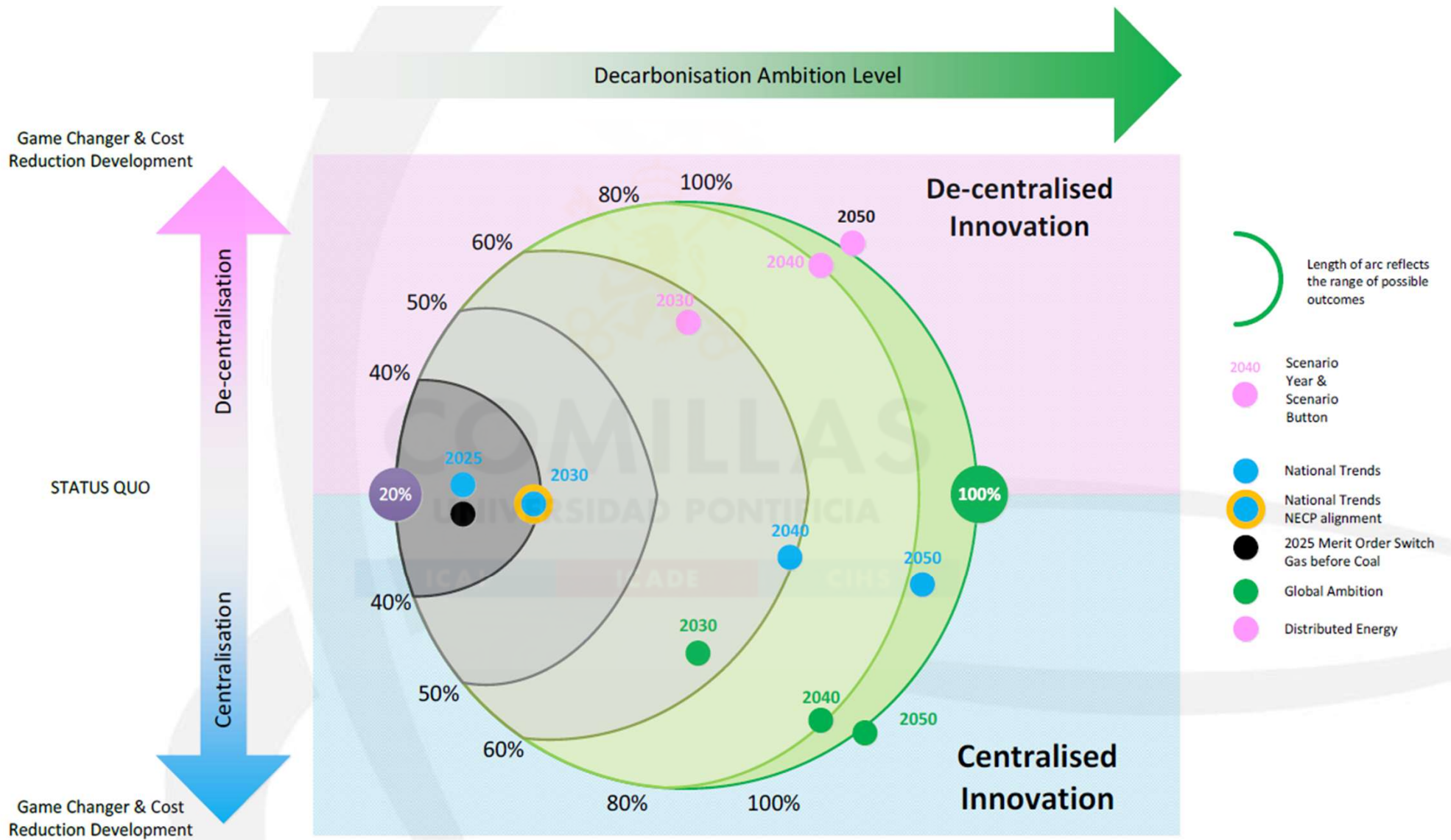




# Future storylines for TYNDP 2018



# TYNDP. Scenario Report



<https://www.entsos-tyndp2020-scenarios.eu/#download>



# Scenarios of uncertainty

- Long-term (some of them are non-random –nonrepeatable–)
  - Electricity demand growth. Macroeconomic data
  - Inflation and discount rate
  - Demand side management (DSM) programs
  - Location of generation plants (CCS plants? CSP generation?)
  - Intermittent generation capacity
  - Fuel and CO2 prices
  - Public opinion (No nukes?)
  - Available transmission technologies
- Medium-term (random –repeatable–)
  - Climate conditions (hydro inflows, wind, sun, temperature)
  - Contingencies (availability of generation and network elements)
  - System operation for several snapshots representative of the situations that may occur over the horizon year (Peak/Off-peak? Winter/Summer?). Possible use of clustering techniques

## Criteria/Objectives

- Enable a low-cost operation of the system
- Enable a high level of security of supply
- Contribute to a sustainable energy supply
- Facilitate grid access to all market participants
- Contribute to internal market integration, facilitate competition and harmonization
- Contribute to the energy efficiency of the system

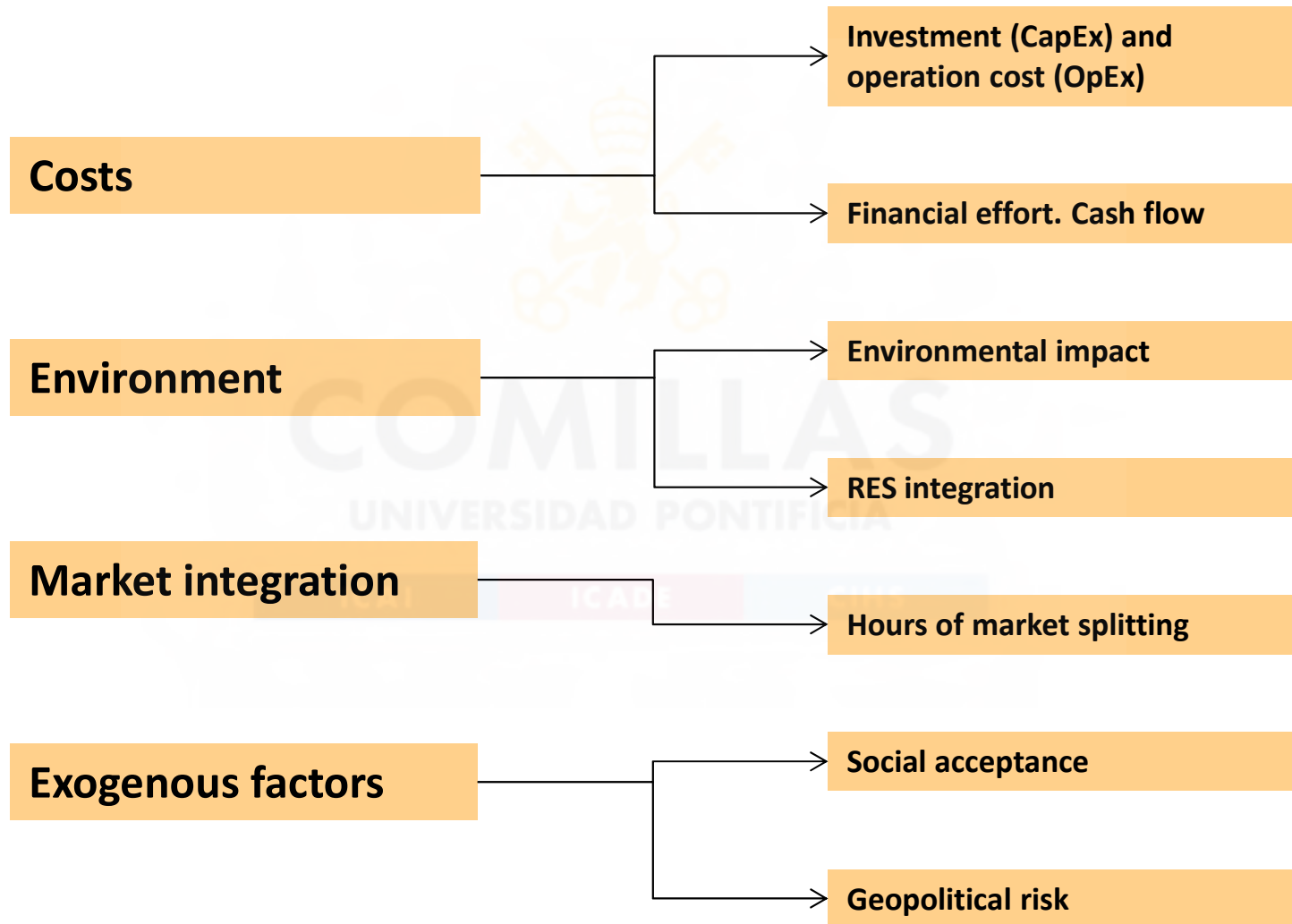
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# Multicriteria Decision Making (MCDM)

## Criteria

## Attributes



# Which is the fastest animal of the nature in running, flying and swimming simultaneously?

- The fastest runner?



***Cheetah* is the fastest running animal in the world**

- The fastest flying?



***Peregrine falcon* is the fastest bird in the world**

- The fastest swimmer?



***Sailfish* is the fastest fish in the world**

# Which is the fastest animal of the nature in all the three attributes simultaneously? And the winner is ... the DUCK

- Can run, although less than the cheetah
- Can fly, although less than the peregrine falcon
- Can swim, although less than the sailfish



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# Weighted-Sum Method of MCDM

- Combines several quantifiable criteria in a **single one** by **monetizing** the criteria

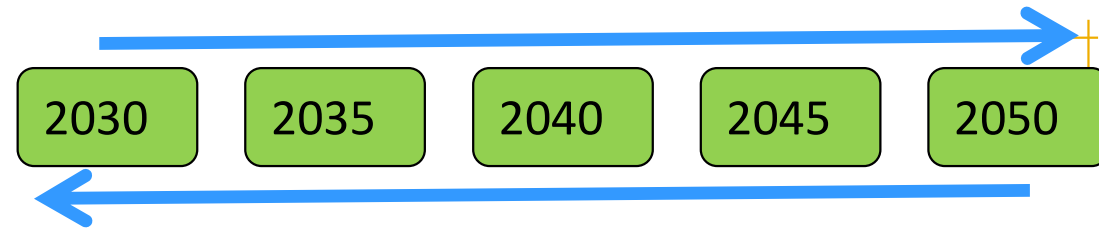
$$\min \sum_i \lambda_i z_i(x)$$

- $\lambda_i$  the weight of each criterion and  $z_i$  the value of the criterion
  - **Reliability**: not served is energy [MWh] monetized by multiplying by the cost of the energy not served [€/MWh]
  - **RES integration**: RES curtailment/spillage [MWh] monetized by multiplying by the penalty associated with RES curtailment/spillage [€/MWh]
  - **Environmental impact**: length of the line [km] multiplied by the restoration measures to be taken [€/km]
- No quantifiable criteria are usually analyzed as a post-process for the best decisions under the previous method

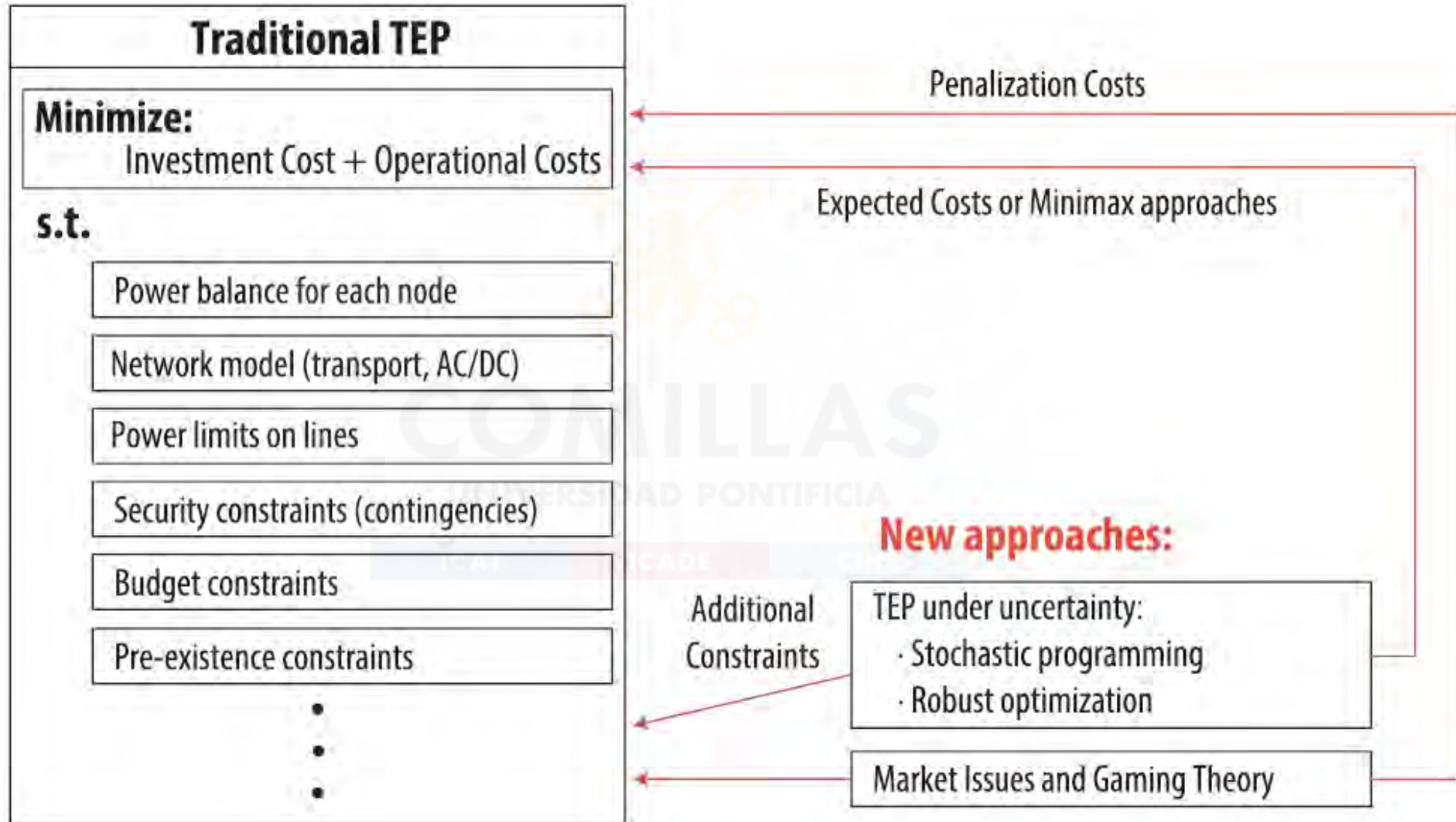
# Time scope

## Decision dynamics

- Static (myopic or short-sighted)
  - Determine optimal investment decisions for a horizon (the year 2030) without representing how to achieve this optimal solution from now on
  - Can be helpful as an “ideal” reference for very long-time horizons
- Sequential static (forward vs. backward planning)
- Dynamic
  - Determine optimal investment decisions since nowadays, up to a particular horizon
  - More cumbersome to solve



# Transmission expansion planning model





# Other uses of transmission planning models

- Remuneration based on the marginal contribution of the line to the system (**congestion rent**)
  - Difference of locational marginal prices (LMP) times the power flow
- Management of **transmission capacity markets**

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## After getting several optimal TEP plans...

- Check that transmission plan can be operated without voltage, stability and short-circuit concerns



1. Transmission Expansion Planning
2. Simple TEP models
3. Modeling issues
4. **Prototype TEP. Mathematical formulation**
5. Prototype TEP. Computer implementation
6. Takeaways



4



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Prototype TEP.

Mathematical formulation



# Mathematical formulation

- **Objective function**
  - Minimize the total investment and expected operation costs
- **Investment variables**
  - *Investment decisions (what lines to build). Binary by nature*
- **Operation variables for each year**
  - Commitment, startup, and shutdown of thermal units
  - Thermal, storage hydro, and pumped storage hydro output
  - Flows through the lines
- **Investment constraints**
  - Operating capacity lower than installed capacity
- **Operation constraints for each year**
  - **Inter-period**
    - Storage hydro and pumped storage hydro scheduling
  - **Intra-period**
    - Load and reserve balance
    - Detailed hydro basin modeling
    - Thermal, hydro, and pumped-storage operation constraints

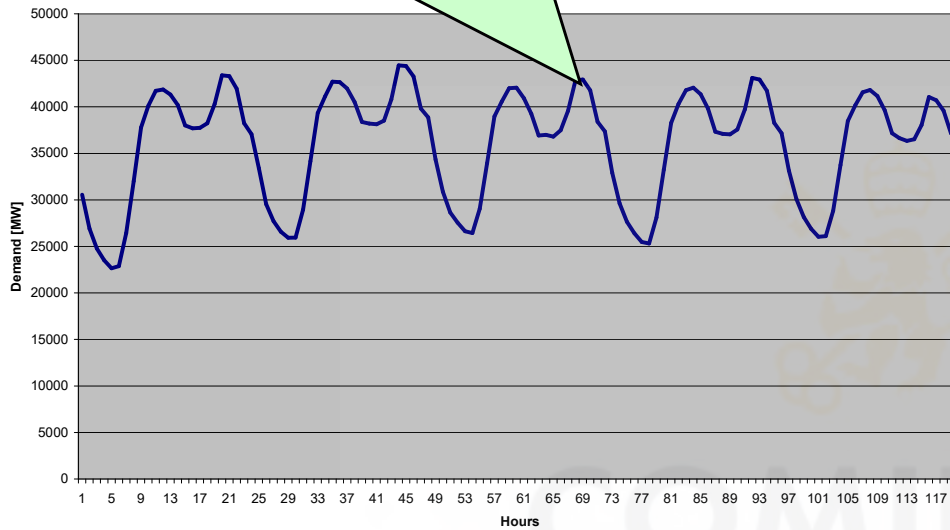
# Indices

- Time scope
  - years
- Period
  - 1 month
- Subperiod
  - weekdays and weekends
- Load level
  - peak, shoulder, and off-peak
- Node

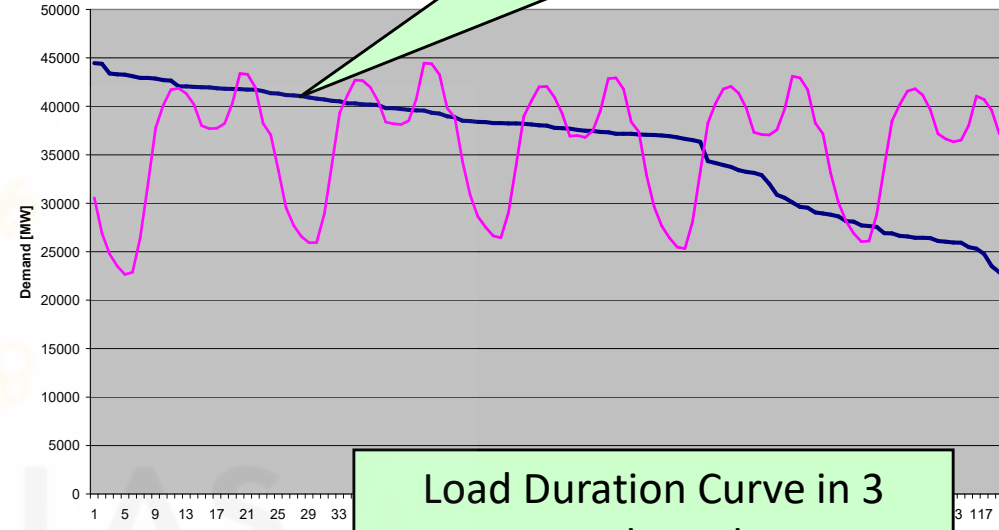
<i>Year</i>	<i>y</i>
<i>Period</i>	<i>p</i>
<i>Subperiod</i>	<i>s</i>
<i>Load level</i>	<i>n</i>
<i>Node</i>	<i>d</i>

# Demand (5 weekdays)

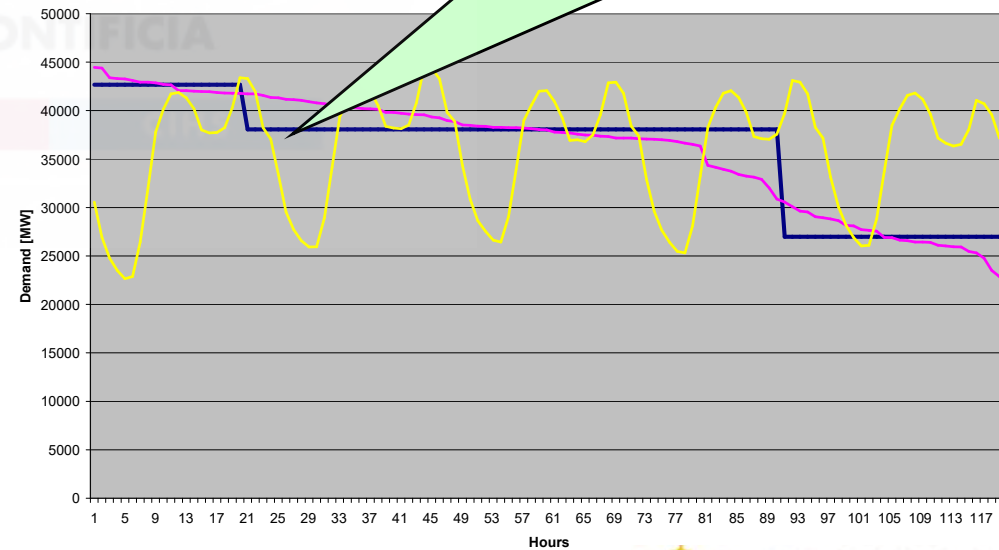
Chronological Load Curve



Load Duration Curve



Load Duration Curve in 3 Load Levels

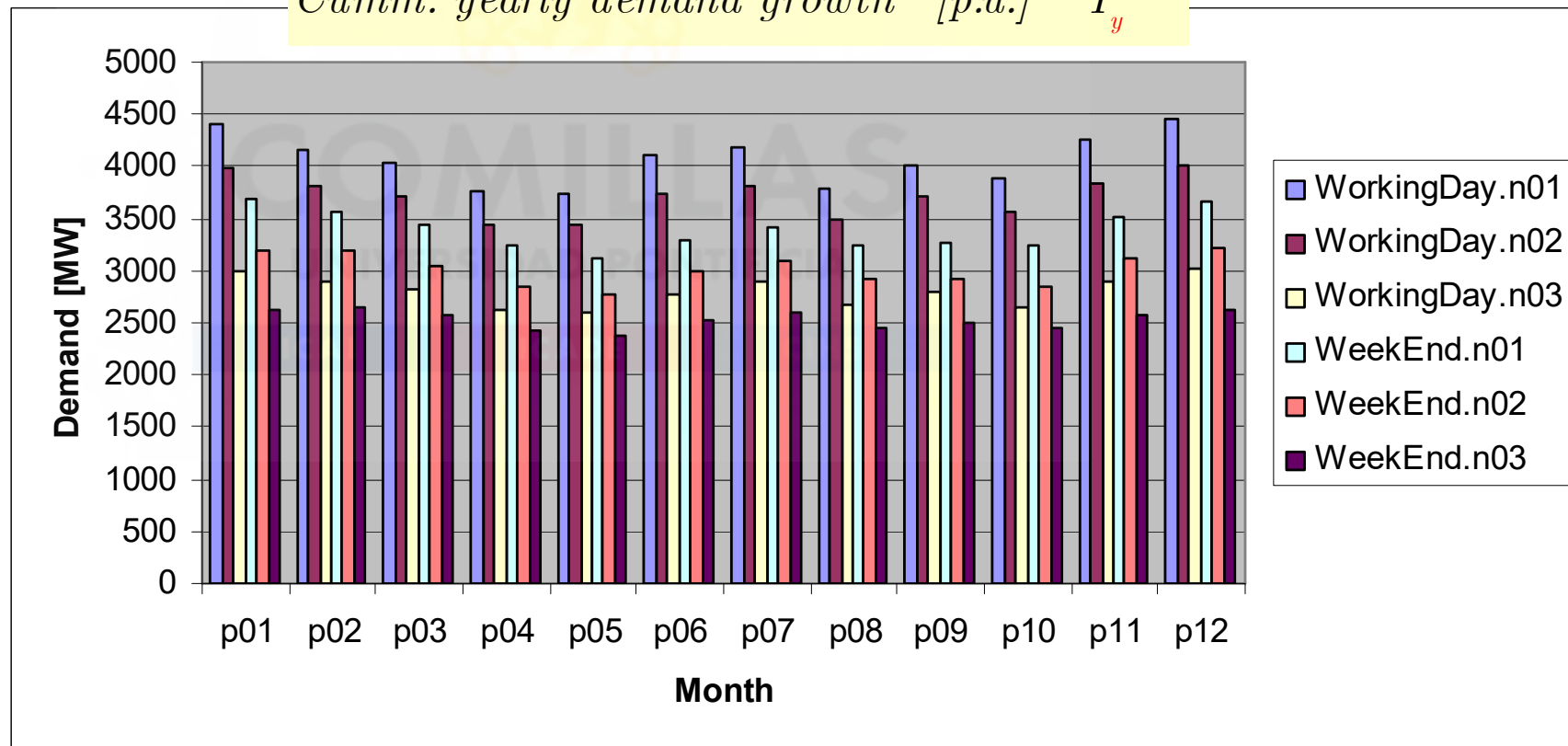




# Demand

- Monthly demand with several load levels
  - Peak, shoulder, and off-peak for weekdays and weekends
- All the weekdays of the same month are similar (same for weekends)

*Demand for each node* [MW]  $D_{psnd}$   
*Duration* [h]  $d_{psn}$   
*Cumm. yearly demand growth* [p.u.]  $I_y$



# Technical characteristics of thermal units ( $t$ )

- Maximum and minimum output
- Fuel cost
- Slope and intercept of the heat rate straight line
- Operation and maintenance (O&M) variable cost
  - No load cost = fuel cost x heat rate intercept
  - Variable cost = fuel cost x heat rate slope + O&M cost
- Cold startup and shutdown cost
- Equivalent forced outage rate (EFOR)

<i>Max and min output</i>	$[MW]$	$\bar{p}_t, \underline{p}_t$
<i>No load cost</i>	$[\text{€} / h]$	$f_t$
<i>Variable cost</i>	$[\text{€} / MWh]$	$v_t$
<i>Startup, shutdown cost</i>	$[\text{€}]$	$su_t, sd_t$
<i>EFOR</i>	$[p.u.]$	$q_t$

# Technical characteristics of hydro plants ( $h$ )

- Maximum and minimum output
- Production function (efficiency for conversion of water inflow to electric power)
- Round-trip efficiency of pumped storage hydro plants
  - Only this ratio of the energy consumed to pump the water is recovered by turbinning it

<i>Max and min output</i>	<i>[MW]</i>	$\bar{p}_h, \underline{p}_h$
<i>Production function</i>	<i>[kWh / m<sup>3</sup>]</i>	$c_h$
<i>Efficiency</i>	<i>[p.u.]</i>	$\eta_h$

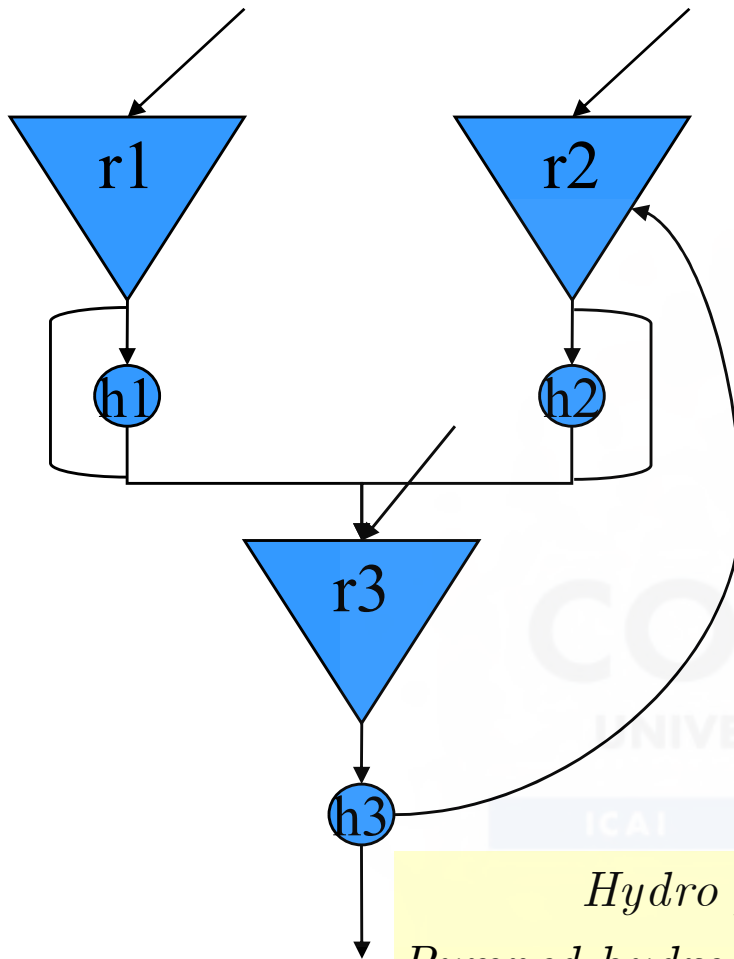


# Technical characteristics of hydro reservoirs ( $r$ )

- Maximum and minimum reserve
- Initial reserve **for every year**
  - Final reserve = initial reserve
- Stochastic inflows independent **for every year**
- **Assumption: There is no connection in reservoir levels or inflows between consecutive years**

<i>Max and min reserve</i>	$[hm^3]$	$\bar{r}_r, r_r$
<i>Initial and final reserve</i>	$[hm^3]$	$r_r'$
<i>Stochastic inflows</i>	$[m^3 / s]$	$i_{pr}^\omega$

# Hydro topology



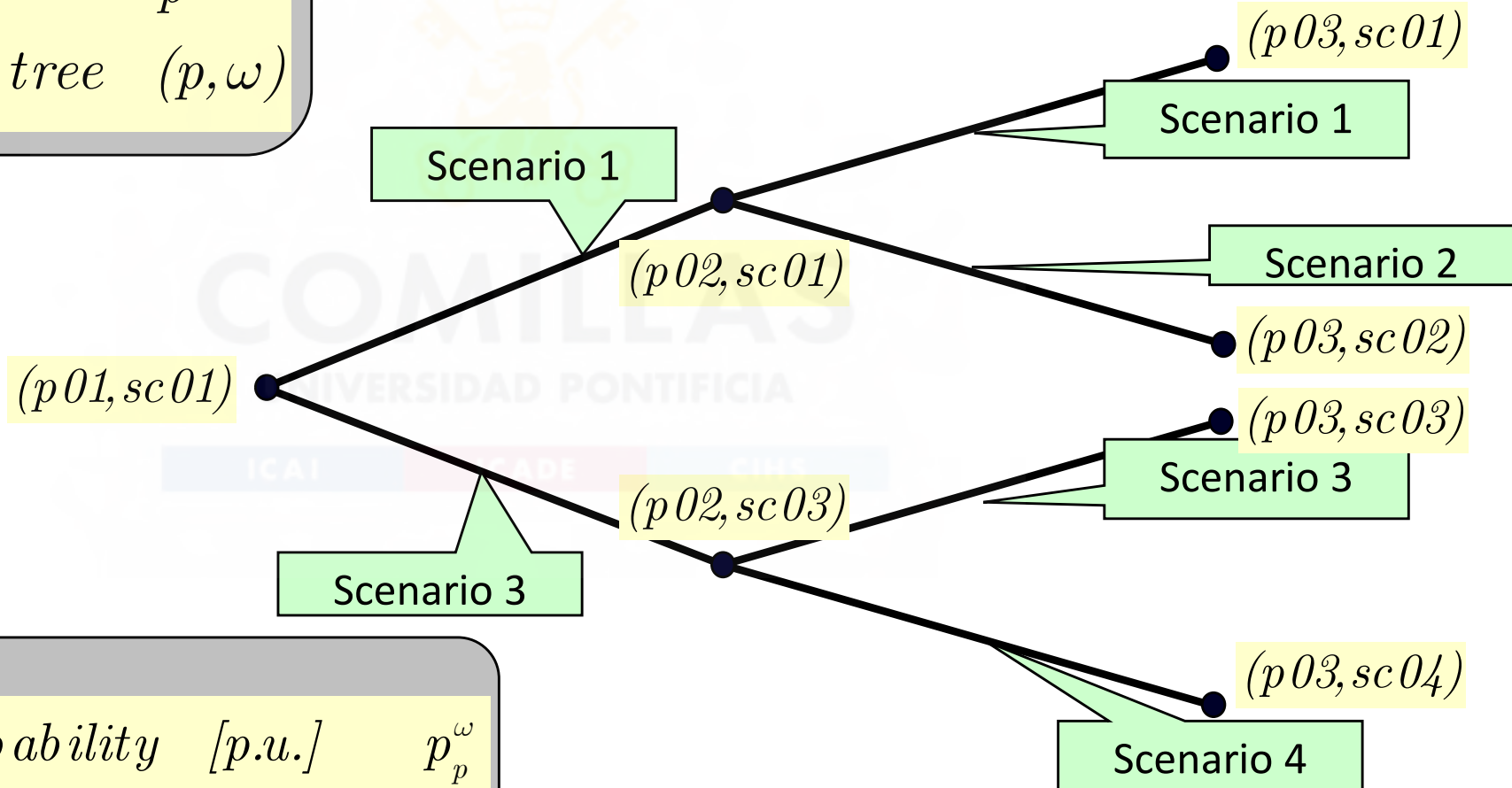
Only one spillage per reservoir can be considered

<i>Hydro plant upstream of reservoir</i>	$h \in up(r)$	$hur(h, r)$	$(h1, r3)$
<i>Pumped hydro plant upstream of reservoir</i>	$h \in up(r)$	$hpr(h, r)$	$(h3, r2)$
<i>Reservoir upstream of hydro plant</i>	$h \in dw(r)$	$ruh(r, h)$	$(r2, h2)$
<i>Reservoir upstream of pumped hydro plant</i>	$h \in dw(r)$	$rph(r, h)$	$(r3, h3)$
<i>Reservoir upstream of reservoir</i>	$r' \in up(r)$	$rur(r, r)$	$(r1, r3)$

# Scenario tree. Ancestor and descendant

Tree structure	
Scenario	$\omega$
Period	$p$
Scenario tree	$(p, \omega)$

Tree relations
$\omega' \in a(\omega) \quad (p02, sc03) \in a[(p03, sc03)]$



Tree data		
Scenario probability	[p.u.]	$p_p^\omega$
Stochastic inflows	$[m^3 / s]$	$i_{pr}^\omega$





# Technical characteristics of transmission lines ( $dd'$ )

- Resistance
- Reactance
- Maximum flow

<i>Resistance</i>	<i>[p.u.]</i>	$R_{dd'}$
<i>Reactance</i>	<i>[p.u.]</i>	$X_{dd'}$
<i>Maximum flow</i>	<i>[MW]</i>	$\bar{F}_{dd'}$

## Technical characteristics of transmission lines ( $dd'$ )

- Overnight investment cost
- Fixed charge rate
  - Annual investment cost = Overnight investment cost x Fixed charge rate

*Annual investment cost* [€]  $f'_{dd'}$

## Other system parameters

- Energy not served cost
- Operating power reserve not served
- Operating power reserve
- Base power

<i>Energy not served cost</i>	$[\text{€} / \text{MWh}]$	$v'$
<i>Power not served cost</i>	$[\text{€} / \text{MW}]$	$v''$
<i>Operating reserve</i>	$[\text{MW}]$	$O_{ps1}$
<i>Base power</i>	$[\text{MW}]$	$S_B$



## Investment variables

- Transmission line exists in year  $y$

*Candidate line exists in year  $y$*   $\{0, 1\}$   $IC_{ydd'}$

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# Operation variables for each year

- Commitment, startup, and shutdown of thermal units

*Commitment, startup and shutdown*  $\{0, 1\}$   $UC_{ypst}^\omega, SU_{ypst}^\omega, SD_{ypst}^\omega$

- Production of thermal and hydro units

*Production of a thermal or hydro unit* [MW]  $P_{ypsnt}^\omega, P_{ypsnh}^\omega$

- Consumption of pumped storage hydro plants

*Consumption of a hydro plant* [MW]  $C_{ypsnh}^\omega$

- Reservoir levels

*Reservoir level* [hm<sup>3</sup>]  $R_{ypr}^\omega$

- Energy not served for each node, and power not served

*Energy and power not served* [MW]  $ENS_{ypsnd}^\omega, PNS_{yps}^\omega$

# Operation variables for each year

- Flow for the transmission lines

$$\text{Flow [MW]} \quad F_{ypsn dd'}^{\omega}$$

- Voltage angle in any node

$$\text{Voltage angle [rad]} \quad \theta_{ypsn d}^{\omega}$$

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# Constraints: Operating power reserve

*Committed output of thermal units*  
 + *Maximum output of hydro plants*  
 + *Power not served*  
 $\geq$  *Demand*  
 + *Operating reserve*

*for peak load level, subperiod,*  
*period and scenario* [MW]

$$\sum_t \bar{p}_t UC_{ypst}^\omega + \sum_h \bar{p}_h + PNS_{yps}^\omega \geq (D_{ps1} + O_{ps1}) I_y \quad \forall \omega yps$$

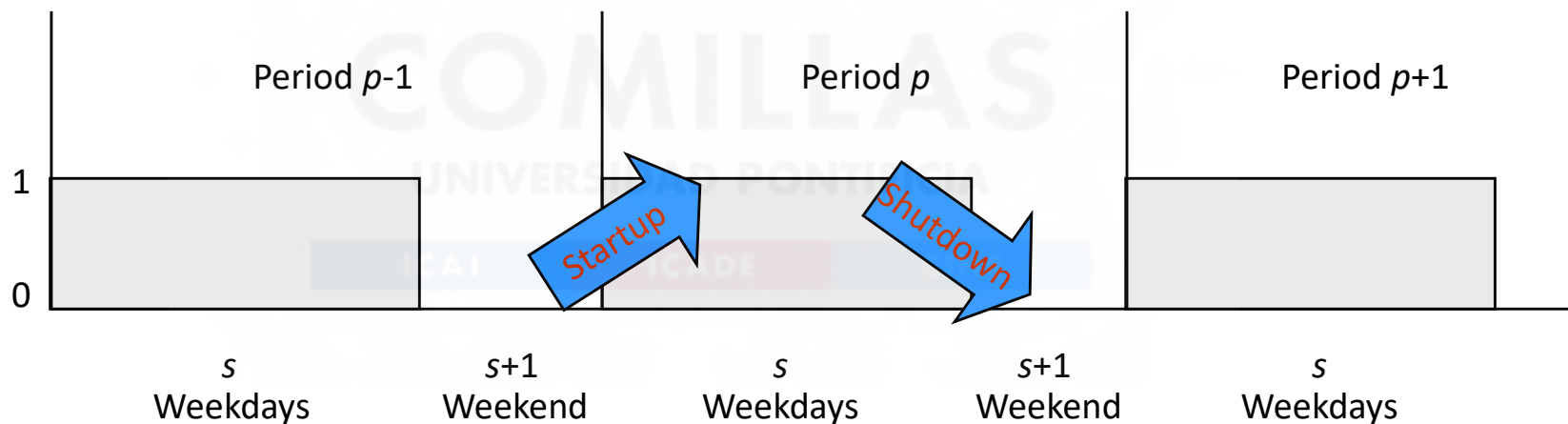
# Constraints: Generation and load balance for each node

- Generation of thermal units*
  - + Generation of storage hydro plants*
  - Consumption of pumped storage hydro plants*
  - + Energy not served*
  - + Flow from incoming lines*
  - Flow from outgoing lines*
  - = Demand*
- for each node, load level, subperiod,  
period, year and scenario [MW]*

$$\sum_{t \in d} P_{ypsnt}^{\omega} + \sum_{h \in d} P_{ypsh}^{\omega} - \sum_{h \in d} C_{ypsh}^{\omega} + ENS_{ypsnd}^{\omega} + \sum_{d'} F_{ypsnd'd}^{\omega} - \sum_{d'} F_{ypsndd'}^{\omega} = D_{psnd} I_y \quad \forall \omega ypsnd$$

# Constraints: Commitment, startup and shutdown

- All the weekdays of the same month are similar (same for weekends)
- Commitment decision of a thermal unit
- Assumption: no startup between periods of consecutive years





# Constraints: Commitment, startup and shutdown

- **Startup** of thermal units can only be made in the transition between consecutive weekend and weekdays

*Commitment of a thermal unit in a weekday*

– *Commitment of a thermal unit in the weekend of previous period*

= *Startup of a thermal unit in this weekday*

– *Startup of a thermal unit in this weekday* [p.u.]

$$UC_{ypst}^{\omega} - UC_{yp-1s+1t}^{\omega'} = SU_{ypst}^{\omega} - SD_{ypst}^{\omega} \quad \forall \omega ypst \quad \omega' \in a(\omega)$$

- **Shutdown** only in the opposite transition

*Commitment of a thermal unit in a weekend*

– *Commitment of a thermal unit in the previous weekday*

= *Startup of a thermal unit in this weekend*

– *Shutdown of a thermal unit in this weekend* [p.u.]

$$UC_{yps+1t}^{\omega} - UC_{ypst}^{\omega} = SU_{yps+1t}^{\omega} - SD_{yps+1t}^{\omega} \quad \forall \omega ypst$$

# Constraints: Commitment and production

*Production of a thermal unit*

$\geq$  *Commitment of a thermal unit times the minimum output reduced by availability rate* [MW]

*Production of a thermal unit*

$\leq$  *Commitment of a thermal unit times the maximum output reduced by availability rate* [MW]

$$UC_{ypst}^{\omega} \underline{p}_t (1 - q_t) \leq P_{ypsnt}^{\omega} \leq UC_{ypst}^{\omega} \bar{p}_t (1 - q_t) \quad \forall \omega ypsnt$$

- If the thermal unit is committed ( $UC_{ypst}^{\omega} = 1$ ) it can produce between its minimum and maximum output
- If the thermal unit is not committed ( $UC_{ypst}^{\omega} = 0$ ) it can't produce

# Constraints: Water balance for each reservoir

*Reservoir volume at the beginning of the period*

– *Reservoir volume at the end of the period*

+ *Natural hydro inflows*

– *Spills from this reservoir*

+ *Spills from upstream reservoirs*

+ *Turbined water from upstream storage hydro plants*

– *Turbined and pumped water from this reservoir*

+ *Pumped water from upstream pumped hydro plants = 0*      *for each reservoir,*  
*period, year and scenario*  
*[hm<sup>3</sup>]*

$$\begin{aligned}
 & R_{yp-1r}^{\omega'} - R_{ypr}^{\omega} + i_{pr}^{\omega} - S_{ypr}^{\omega} + \sum_{r' \in up(r)} S_{ypr'}^{\omega} \\
 & + \sum_{\substack{sn \\ h \in up(r)}} d_{psn} P_{ypsnh}^{\omega} / c_h - \sum_{\substack{sn \\ h \in dw(r)}} d_{psn} P_{ypsnh}^{\omega} / c_h \\
 & + \sum_{\substack{sn \\ h \in up(r)}} d_{psn} C_{ypsnh}^{\omega} \eta_h / c_h - \sum_{\substack{sn \\ h \in dw(r)}} d_{psn} C_{ypsnh}^{\omega} \eta_h / c_h = 0 \quad \forall \omega ypr \quad \omega' \in a(\omega)
 \end{aligned}$$



# Constraints: Operation limits

Reservoir volumes between limits for each hydro reservoir [hm<sup>3</sup>]

$$\underline{r}_r \leq R_{ypr}^\omega \leq \bar{r}_r \quad \forall \omega ypr$$

$$R_{0r} = R_{yPr}^\omega = r'_r \quad \forall \omega yr$$

Operation power lower than installed capacity [MW]

$$0 \leq P_{ypsnt}^\omega \leq \bar{p}_t (1 - q_t) \quad \forall \omega ypsnt$$

$$0 \leq P_{ypsnh}^\omega, C_{ypsnh}^\omega \leq \bar{p}_h \quad \forall \omega ypsnh$$

Commitment, startup and shutdown for each unit [MW]

$$UC_{ypst}^\omega, SU_{ypst}^\omega, SD_{ypst}^\omega \in \{0, 1\} \quad \forall \omega ypst$$

## Constraints: DC linearized load flow and flow limits

Flow in existing lines as a function of the voltage angles of beginning and ending nodes [MW]

$$F_{ypsndd'}^\omega = \frac{\theta_{ypsnd}^\omega - \theta_{ypsnd'}^\omega}{X_{dd'}} S_B \quad \forall \omega ypsndd'$$

Flow in candidate lines as a function of the voltage angles of beginning and ending nodes [MW]

$$F_{ypsndd'}^\omega \leq \frac{\theta_{ypsnd}^\omega - \theta_{ypsnd'}^\omega}{X_{dd'}} S_B + \bar{F}'_{dd'} (1 - IC_{ydd'}) \quad \forall \omega ypsndd'$$

$$F_{ypsndd'}^\omega \geq \frac{\theta_{ypsnd}^\omega - \theta_{ypsnd'}^\omega}{X_{dd'}} S_B - \bar{F}'_{dd'} (1 - IC_{ydd'}) \quad \forall \omega ypsndd'$$

# Constraints: Flow limits and voltage angle

Flow of existing lines below limit for every year [MW]

$$-\bar{F}_{dd'} \leq F_{ypsndd'}^\omega \leq \bar{F}_{dd'} \quad \forall \omega ypsndd'$$

Flow of candidate lines below limit for every year [MW]

$$-\bar{F}_{dd'} IC_{ydd'} \leq F_{ypsndd'}^\omega \leq \bar{F}_{dd'} IC_{ydd'} \quad \forall \omega ypsndd'$$

Reference angle [rad]

$$\theta_{ypsnd}^\omega = 0 \quad \forall \omega ypsn$$



# Constraints: Installation decision in consecutive years

Existence of an installed line in the following year

[p.u.]

$$IC_{y-1dd'} \leq IC_{ydd'} \quad \forall ydd'$$

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# Weighted-sum objective function

- Minimize

- Transmission investment costs [€]

$$\sum_y \sum_{dd'} f'_{dd'} IC_{ydd'}$$

- Thermal unit expected variable (fuel, O&M, emission) costs [€]

$$\sum_{y\omega p s t} p_p^\omega s u_t S U_{y p s t}^\omega + \sum_{y\omega p s t} p_p^\omega s d_t S D_{y p s t}^\omega + \sum_{y\omega p s n t} p_p^\omega d_{p s n} f_t U C_{y p s t}^\omega + \sum_{y\omega p s n t} p_p^\omega d_{p s n} v_t P_{y p s n t}^\omega$$

- Expected penalties introduced in the objective function for energy not served and power non served [€]

$$\sum_{y\omega p s n d} p_p^\omega d_{p s n} v' E N S_{y p s n d}^\omega + \sum_{y\omega p s} p_p^\omega v'' P N S_{y p s}^\omega$$

# Long (Short) Run Marginal Cost (LRMC-SRMC)

- **Dual variable** of generation and load balance in each node [€/MW]
  - Change in the objective function due to a marginal increase in the demand when binary variables (investment, commitment, startup, and shutdown) are relaxed (LRMC) or binary/fixed (SRMC)

$$\sum_{t \in d} P_{ypsnt}^{\omega} + \sum_{h \in d} P_{ypsh}^{\omega} - \sum_{h \in d} C_{ypsh}^{\omega} + ENS_{ypsnd}^{\omega} + \sum_{d'} F_{ypsnd'd}^{\omega} - \sum_{d'} F_{ypsndd'}^{\omega} = D_{psnd} I_y : \sigma_{ypsnd}^{\omega} \quad \forall \omega ypsnd$$

- **Long/Short Run Marginal Cost** = dual variable / load level duration / scenario probability. Expressed in [€/MWh]

$$LRMC \text{ or } SRMC_{ypsnd}^{\omega} = \sigma_{ypsnd}^{\omega} / d_{psn} / p_p^{\omega} \quad \forall \omega ypsnd$$



1. Transmission Expansion Planning
2. Simple TEP models
3. Modeling issues
4. Prototype TEP. Mathematical formulation
5. **Prototype TEP. Computer implementation**
6. Takeaways

5

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Prototype TEP.

Computer implementation

# openTEPES Open Generation, Storage, and Transmission Operation and Expansion Planning Model with RES and ESS in Pyomo

(<https://pascua.iit.comillas.edu/aramos/openTEPES/index.html>) (<https://github.com/IIT-EnergySystemModels/openTEPES>)



Open Generation, Storage, and Transmission Operation and Expansion Planning Model with RES and ESS (openTEPES)



*"Simplicity and Transparency in Energy Systems Planning"*

The **openTEPES** model has been developed at the [Instituto de Investigación Tecnológica \(IIT\)](#) of the [Universidad Pontificia Comillas](#).

It is integrated into the [open energy system modelling platform](#), helping model Europe's energy system.

It has been used by the **Ministry for the Ecological Transition and the Demographic Challenge (MITECO)** to analyze the electricity sector in the latest Spanish [National Energy and Climate Plan \(NECP\) 2023-2030](#) in June 2023.

**Reference:** A. Ramos, E. Quispe, S. Lumbreras "OpenTEPES: Open-source Transmission and Generation Expansion Planning" SoftwareX 18: June 2022 [10.1016/j.softx.2022.101070](#)

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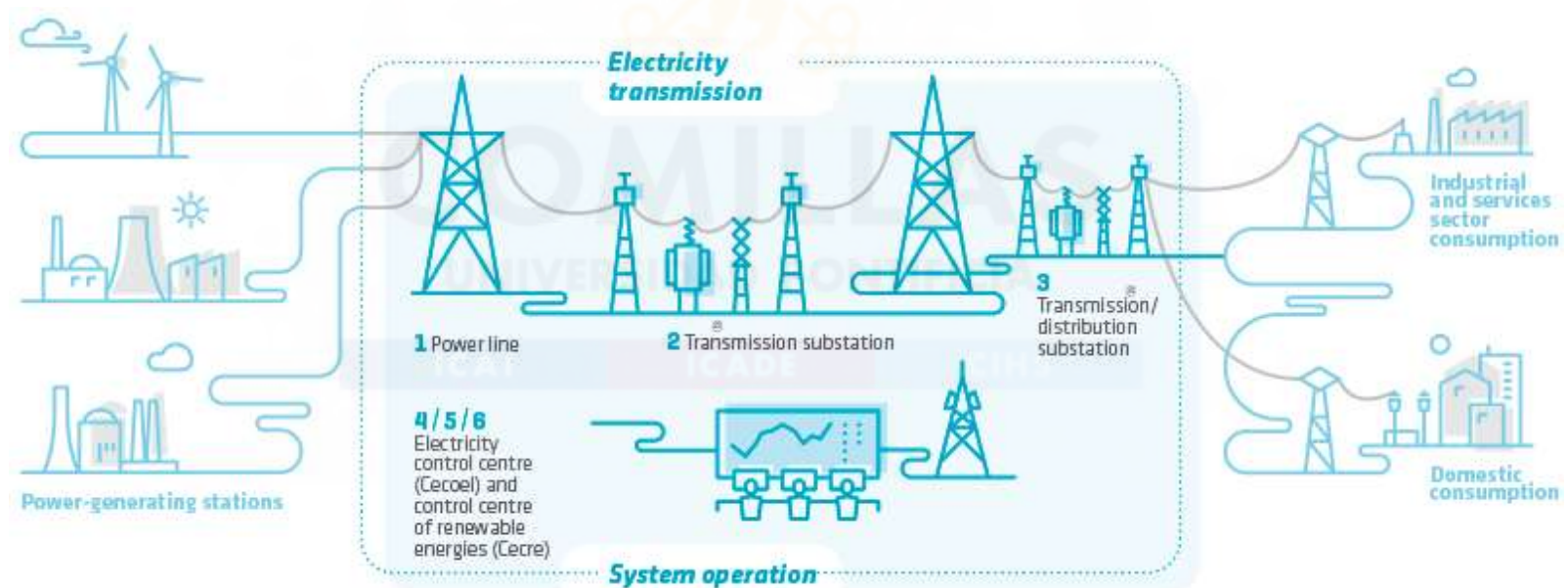
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# Main modeling features (i)

- Generation and transmission operation and expansion planning
- Network-constrained unit commitment (NCUC)
- DC power flow (DCPF) with losses
- Hourly, bi-hourly, etc. time steps





## Main modeling features (ii)

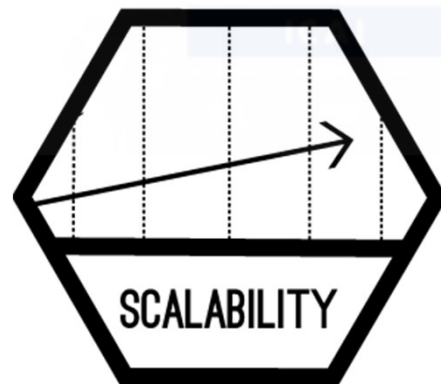
- **Energy Storage Systems (ESS)**, e.g., hydropower plants, open- and closed-loop pumped-storage hydro, battery
- Pumped-storage hydro (PSH) or batteries **operate shifting energy between different timeframes** and represent a **small modification of the operation variable cost** → a detailed system operation modeling is mandatory
  - Hourly operation
  - Unit-based modeling of energy storage units



# Main code features

- Simplicity and transparency
- Code is written to be read by humans
- Tight and compact formulation
- Careful implementation. Numerical stability
- Scalability: from small- to large-scale cases

## Simplicity





# Sets

$\omega$	Scenario
$p$	Period
$n$	Load level
$\nu$	Time step. Duration of each load level (e.g., 2 h, 3 h)
$g$	Generator (thermal or hydro unit or ESS)
$t$	Thermal unit
$e$	Energy Storage System (ESS)
$i, j$	Node
$z$	Zone. Each node belongs to a zone $i \in z$
$a$	Area. Each zone belongs to an area $z \in a$
$r$	Region. Each area belongs to a region $a \in r$
$c$	Circuit
$ijc$	Line (initial node, final node, circuit)
$EG, CG$	Set of existing and candidate generators
$EE, CE$	Set of existing and candidate ESS
$EL, CL$	Set of existing and candidate lines



# Demand and operating reserves

- **Balance** of generation and demand [GW]
- **Upward and downward operating reserves** [GW] provided by controllable generators (CCGT, storage hydro) and ESS (pumped-storage hydro, batteries), **including activation** of these reserves [GWh]
- **Reserve activation**: a proportion (e.g., 25-30 %) of the power provided as operating reserves that are asked to be deployed as energy

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# Parameters. Demand and operating reserves

They are written in capital letters.

Demand		
$D_{\omega pni}$	Demand in each node	GW
$DUR_n$	Duration of each load level	h
$CENS$	Cost of energy not served. Value of Lost Load (VoLL)	€/MWh

Scenarios		
$P_{\omega}$	Probability of each scenario	p.u.

Operating reserves		
$URA, DRA$	Upward and downward reserve activation	p.u.
$UR_{\omega pna}, DR_{\omega pna}$	Upward and downward operating reserves for each area	GW

# Thermal subsystem

- Maximum and minimum output of the second block of a committed unit (all except the VRES units) [p.u.]
- Total output of a committed unit [GW]
- Logical relation between commitment, startup, and shutdown status of a committed unit [p.u.]
- Maximum ramp up and down for the second block of a thermal unit [p.u.]
- Minimum up time and down time of a thermal unit [h]





# Hydro and storage subsystems



- Power plants: **hydro**, **open-loop pumped-storage hydro (PSH)** aggregated in management units, **closed-loop PSH** treated individually, and system **battery** storage
- ESS **energy inventory** (only for load levels multiple of 24 or 168 h depending on the ESS type) [TWh]
- Total charge of an ESS unit [GW]
- Maximum and minimum charge of an ESS [p.u.]
- **Incompatibility between charge and discharge** of an ESS [p.u.]

# Variable renewable energy sources (VRES)

- Power plants: solar PV, solar thermal, onshore wind, biomass
- Distinction between existing onshore wind and a new one
- **Maximum and minimum hourly variable generation**



Transmissio



# Parameters. Generation

Generation system		
$CFG_g$	Annualized fixed cost of a candidate generator	M€
$\underline{GP}_g, \overline{GP}_g$	Minimum load and maximum output of a generator	GW
$\overline{GC}_e$	Maximum consumption of an ESS	GW
$CF_g, CV_g$	Fixed and variable cost of a generator. Variable cost includes fuel, O&M and emission cost	€/h, €/MWh
$CV_e$	Variable cost of an ESS when charging	€/MWh
$RU_t, RD_t$	Ramp up and ramp down of a thermal unit	MW/h
$TU_t, TD_t$	Minimum uptime and downtime of a thermal unit	h
$CSU_g, CSD_g$	Startup and shutdown cost of a committed unit	M€
$\tau_e$	Characteristic duration of the ESS (e.g., 24 h, 168 h, 672 h -for daily, weekly, monthly-)	h
$EF_e$	Efficiency of the pump/turbine cycle of a hydro power plant or charge/discharge of a battery	p.u.
$I_e$	Capacity of an ESS (e.g., hydro power plant)	GWh
$EI_{wpng}$	Energy inflows of an ESS (e.g., hydro power plant)	GWh



# Parameters. Transmission network

Transmission system		
$CFT_{ijc}$	Annualized fixed cost of a candidate transmission line	M€
$\bar{F}_{ijc}$	Net transfer capacity (total transfer capacity multiplied by the security coefficient) of a transmission line	GW
$\bar{F}'_{ijc}$	Maximum flow used in the Kirchhoff's 2nd law constraint (e.g., disjunctive constraint for the candidate AC lines)	GW
$L_{ijc}, X_{ijc}$	Loss factor and reactance of a transmission line	p.u.
$S_B$	Base power	GW

The net transfer capacity of a transmission line can be different in each direction. However, here it is presented as equal for simplicity.

# Variables. ENS and generation

They are written in lower letters.

<b>Demand</b>		
$ens_{\omega pni}$	Energy not served	GW

<b>Generation system</b>		
$icg_g$	Candidate generator or ESS installed or not	{0,1}
$gp_{\omega png}, gc_{\omega png}$	Generator output (discharge if an ESS) and consumption (charge if an ESS)	GW
$p_{\omega png}$	Generator output of the second block (i.e., above the minimum load)	GW
$c_{\omega pne}$	Generator charge	GW
$ur_{\omega png}, dr_{\omega png}$	Upward and downward operating reserves of a non-renewable generating unit	GW
$ur'_{\omega pne}, dr'_{\omega pne}$	Upward and downward operating reserves of an ESS consumption unit	GW
$i_{\omega pne}$	ESS stored energy (inventory)	GWh
$s_{\omega pne}$	ESS spilled energy	GWh
$uc_{\omega png}, su_{\omega png}, sd_{\omega png}$	Commitment, startup and shutdown of generation unit per load level	{0,1}

# Variables. Transmission network

Transmission system		
$ict_{ijc}$	Candidate line installed or not	{0,1}
$f_{\omega pni jc}$	Flow through a line	GW
$l_{\omega pni jc}$	Half ohmic losses of a line	GW
$\theta_{\omega pni}$	Voltage angle of a node	rad



# Objective function

**Objective function:** minimization of total (investment and operation) cost for the scope of the model

Generation, storage and network investment cost [M€]

$$\sum_g CFG_g icg_g + \sum_{ijc} CFT_{ijc} ict_{ijc} +$$

Generation operation cost [M€]

$$\sum_{\omega png} [P_{\omega} DUR_n (CV_{gpg} p_{\omega png} + CF_{guc} u_{\omega png}) + CSU_{gsu} s_{\omega png} + CSD_{gsd} s_{\omega png}] +$$

Variable consumption operation cost [M€]

$$\sum_{\omega pne} [P_{\omega} DUR_n CV_{egc} c_{\omega pne}] +$$

Reliability cost [M€]

$$\sum_{\omega pni} P_{\omega} DUR_n CENS_{ens} s_{\omega pni}$$

# Constraints. Operation bounded by investment

Commitment decision bounded by investment decision for candidate committed units (all except the VRES units)  
[p.u.]

$$u_{C_{\omega p n g}} \leq i_{c g} \quad \forall \omega p n g, g \in CG$$

Output and consumption bounded by investment decision for candidate ESS [p.u.]

$$\frac{g_{P_{\omega p n e}}}{G_{P_e}} \leq i_{c g_e} \quad \forall \omega p n e, e \in CE$$

$$\frac{g_{C_{\omega p n e}}}{G_{C_e}} \leq i_{c g_e} \quad \forall \omega p n e, e \in CE$$

# Constraints. Balance and operating reserves

Balance of generation and demand at each node with ohmic losses [GW]

$$\sum_{g \in i} g p_{\omega p n g} - \sum_{e \in i} g c_{\omega p n e} + e n s_{\omega p n i} = D_{\omega p n i} + \sum_{j c} l_{\omega p n i j c} + \sum_{j c} l_{\omega p n j i c} + \sum_{j c} f_{\omega p n i j c} - \sum_{j c} f_{\omega p n j i c} \quad \forall \omega p n i$$

Upward and downward operating reserves provided by non-renewable generators, and ESS when charging for each area [GW]

$$\sum_{g \in a} u r_{\omega p n g} + \sum_{e \in a} u r'_{\omega p n e} = U R_{\omega p n a} \quad \forall \omega p n a$$

$$\sum_{g \in a} d r_{\omega p n g} + \sum_{e \in a} d r'_{\omega p n e} = D R_{\omega p n a} \quad \forall \omega p n a$$

VRES units (i.e., those with linear variable cost equal to 0 and no storage capacity) do not contribute to the the operating reserves.

Operating reserves from ESS can only be provided if enough energy is available for producing

$$u r_{\omega p n e} \leq \frac{i_{\omega p n e}}{D U R_n} \quad \forall \omega p n e$$

$$d r_{\omega p n e} \leq \frac{I_e - i_{\omega p n e}}{D U R_n} \quad \forall \omega p n e$$

or for storing

$$u r'_{\omega p n e} \leq \frac{I_e - i_{\omega p n e}}{D U R_n} \quad \forall \omega p n e$$

$$d r'_{\omega p n e} \leq \frac{i_{\omega p n e}}{D U R_n} \quad \forall \omega p n e$$



# Constraints. ESS Inventory. Total output

ESS energy inventory (only for load levels multiple of 24, 168 or 672 h depending on the ESS type) [GWh]

$$i_{\omega p, n-\tau_e, e} + \sum_{n'=n+\nu-\tau_e}^n DUR_{n'} (EI_{\omega p n e} - gp_{\omega p n e} + EF_e gc_{\omega p n e}) = i_{\omega p n e} + s_{\omega p n e} \quad \forall \omega p n e$$

Maximum and minimum output of the second block of a committed unit (all except the VRES units) [p.u.]

- D.A. Tejada-Arango, S. Lumbreras, P. Sánchez-Martín, and A. Ramos “Which Unit-Commitment Formulation is Best? A Systematic Comparison” IEEE Transactions on Power Systems 35 (4): 2926-2936, Jul 2020  
[10.1109/TPWRS.2019.2962024](https://doi.org/10.1109/TPWRS.2019.2962024)
- C. Gentile, G. Morales-España, and A. Ramos “A tight MIP formulation of the unit commitment problem with start-up and shut-down constraints” EURO Journal on Computational Optimization 5 (1), 177-201, Mar 2017. [10.1007/s13675-016-0066-y](https://doi.org/10.1007/s13675-016-0066-y)
- G. Morales-España, A. Ramos, and J. Garcia-Gonzalez “An MIP Formulation for Joint Market-Clearing of Energy and Reserves Based on Ramp Scheduling” IEEE Transactions on Power Systems 29 (1): 476-488, Jan 2014.  
[10.1109/TPWRS.2013.2259601](https://doi.org/10.1109/TPWRS.2013.2259601)
- G. Morales-España, J.M. Latorre, and A. Ramos “Tight and Compact MILP Formulation for the Thermal Unit Commitment Problem” IEEE Transactions on Power Systems 28 (4): 4897-4908, Nov 2013.  
[10.1109/TPWRS.2013.2251373](https://doi.org/10.1109/TPWRS.2013.2251373)

$$\frac{p_{\omega p n g} + URA \, ur_{\omega p n g} + ur_{\omega p n g}}{GP_g - GP_g} \leq uc_{\omega p n g} \quad \forall \omega p n g$$

$$\frac{p_{\omega p n g} - DRA \, dr_{\omega p n g} - dr_{\omega p n g}}{GP_g - GP_g} \geq 0 \quad \forall \omega p n g$$

Ricobayo  
hydroelectric  
power plant



# Constraints. Charge/discharge of ESS. Commitment, startup, shutdown

Maximum and minimum charge of an ESS [p.u.]

$$\frac{c_{\omega p n e} + URA dr'_{\omega p n e} + dr'_{\omega p n e}}{GC_e} \leq 1 \quad \forall \omega p n e$$

$$\frac{c_{\omega p n e} - DRA ur'_{\omega p n e} - ur'_{\omega p n e}}{GC_e} \geq 0 \quad \forall \omega p n e$$

Source: Wikipedia

Incompatibility between charge and discharge of an ESS [p.u.]

$$\frac{p_{\omega p n e} + URA ur'_{\omega p n e} + ur_{\omega p n g}}{GP_e - GP_e} + \frac{c_{\omega p n e} + URA dr'_{\omega p n e} + dr'_{\omega p n e}}{GC_e} \leq 1 \quad \forall \omega p n e, e \in CE$$

Total output of a committed unit (all except the VRES units) [GW]

$$\frac{gp_{\omega p n g}}{GP_g} = uc_{\omega p n g} + \frac{p_{\omega p n g} + URA ur_{\omega p n g} - DRA dr_{\omega p n g}}{GP_g} \quad \forall \omega p n g$$

Total charge of an ESS unit [GW]

$$gc_{\omega p n e} = c_{\omega p n e} + URA dr'_{\omega p n e} - DRA ur'_{\omega p n e} \quad \forall \omega p n e, e \in CE$$

Logical relation between commitment, startup and shutdown status of committed unit (all except the VRES units)  
[p.u.]

$$uc_{\omega p n g} - uc_{\omega p, n-v, g} = su_{\omega p n g} - sd_{\omega p n g} \quad \forall \omega p n g$$

Initial commitment of the units is determined by the model based on the merit order loading, including the VRES and ESS units.





# Constraints. Ramps, minimum up- and downtime

Maximum ramp up and ramp down for the second block of a thermal unit [p.u.]

- P. Damcı-Kurt, S. Küçükyavuz, D. Rajan, and A. Atamtürk, “A polyhedral study of production ramping,” *Math. Program.*, vol. 158, no. 1–2, pp. 175–205, Jul. 2016. [10.1007/s10107-015-0919-9](https://doi.org/10.1007/s10107-015-0919-9)

$$\frac{-P_{\omega p, n-\nu, t} - URA \, ur_{\omega p, n-\nu, t} + P_{\omega pnt} + URA \, ur_{\omega pnt} + ur_{\omega pnt}}{DUR_n RU_t} \leq uc_{\omega pnt} - su_{\omega pnt} \quad \forall \omega pnt$$

$$\frac{-P_{\omega p, n-\nu, t} + DRA \, dr_{\omega p, n-\nu, t} + P_{\omega pnt} - DRA \, dr_{\omega pnt} - dr_{\omega pnt}}{DUR_n RD_t} \geq -uc_{\omega p, n-\nu, t} + sd_{\omega pnt} \quad \forall \omega pnt$$

Minimum up time and down time of thermal unit [h]

- D. Rajan and S. Takriti, “Minimum up/down polytopes of the unit commitment problem with start-up costs,” IBM, New York, Technical Report RC23628, 2005. <https://pdfs.semanticscholar.org/b886/42e36b414d5929fed48593d0ac46ae3e2070.pdf>

$$\sum_{n'=n+\nu-TU_t}^n su_{\omega pnt} \leq uc_{\omega pnt} \quad \forall \omega pnt$$

$$\sum_{n'=n+\nu-TD_t}^n sd_{\omega pnt} \leq 1 - uc_{\omega pnt} \quad \forall \omega pnt$$



# Constraints. Transmission network. DC power flow

Transfer capacity in candidate transmission lines [p.u.]

$$-ict_{ijc} \leq \frac{f_{\omega p n i j c}}{\bar{F}_{ijc}} \leq ict_{ijc} \quad \forall \omega p n i j c, i j c \in CL$$

DC Power flow for existing and candidate AC-type lines (Kirchhoff's second law) [rad]

$$\frac{f_{\omega p n i j c}}{\bar{F}'_{ijc}} = (\theta_{\omega p n i} - \theta_{\omega p n j}) \frac{S_B}{X_{ijc} \bar{F}'_{ijc}} \quad \forall \omega p n i j c, i j c \in EL$$

$$-1 + ict_{ijc} \leq \frac{f_{\omega p n i j c}}{\bar{F}'_{ijc}} - (\theta_{\omega p n i} - \theta_{\omega p n j}) \frac{S_B}{X_{ijc} \bar{F}'_{ijc}} \leq 1 - ict_{ijc} \quad \forall \omega p n i j c, i j c \in CL$$

Half ohmic losses are linearly approximated as a function of the flow [GW]

$$-\frac{L_{ijc}}{2} f_{\omega p n i j c} \leq l_{\omega p n i j c} \leq \frac{L_{ijc}}{2} f_{\omega p n i j c} \quad \forall \omega p n i j c$$

Source: REE



# Constraints. Bounds

Bounds on generation variables [GW]

$$0 \leq gp_{\omega p n g} \leq \overline{GP}_g \quad \forall \omega p n g$$

$$0 \leq qc_{\omega p n e} \leq \overline{GC}_e \quad \forall \omega p n e$$

$$0 \leq ur_{\omega p n g} \leq \overline{CP}_g - \underline{GP}_g \quad \forall \omega p n g$$

$$0 \leq ur'_{\omega p n e} \leq \overline{CP}_e - \underline{GP}_e \quad \forall \omega p n e$$

$$0 \leq dr_{\omega p n g} \leq \overline{CP}_g - \underline{GP}_g \quad \forall \omega p n g$$

$$0 \leq dr'_{\omega p n e} \leq \overline{CP}_e - \underline{GP}_e \quad \forall \omega p n e$$

$$0 \leq p_{\omega p n g} \leq \overline{GP}_g - \underline{GP}_g \quad \forall \omega p n g$$

$$0 \leq c_{\omega p n e} \leq \overline{GC}_e \quad \forall \omega p n e$$

$$0 \leq i_{\omega p n e} \leq I_e \quad \forall \omega p n e$$

$$0 \leq s_{\omega p n e} \quad \forall \omega p n e$$

$$0 \leq ens_{\omega p n i} \leq D_{\omega p n i} \quad \forall \omega p n i$$

Bounds on network variables [GW]

$$0 \leq l_{\omega p n i j c} \leq \frac{L_{i j c}}{2} \overline{F}_{i j c} \quad \forall \omega p n i j c$$

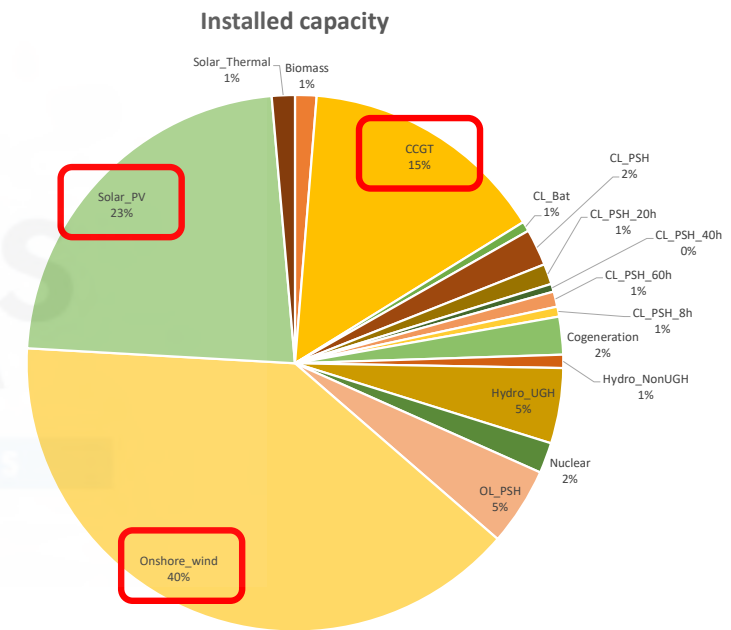
$$-\overline{F}_{i j c} \leq f_{\omega p n i j c} \leq \overline{F}_{i j c} \quad \forall \omega p n i j c, i j c \in EL$$

Voltage angle of the reference node fixed to 0 for each scenario, period, and load level [rad]

$$\theta_{\omega p n, node_{ref}} = 0$$

# Case study: Spain 2030

- 10-year Integrated National Energy and Climate Plan (NECP)
- Installed capacity: **165,000 MW**
- Half of the nuclear units phased out (**3,100 MW**), no coal units, existing CCGT (**24,500 MW**)
- Significant investments in solar PV (**37,500 MW**) and onshore wind (**65,200 MW**)
- Existing (**11,500 MW**) and additional pumped-storage hydro (**5,300 MW**)
- Batteries forced to be installed (**1,000 MW**)





# Why flexibility will be needed in future electric systems?

1. Conventional generation is being phased out
2. VRES introduce additional flexibility requirements
  - Flexibility **mechanisms**:
    - ESS (**Energy Storage Systems**) (PSH, batteries)
    - Flexible electricity **generation** (CCGT, hydro)
    - Solar Thermal
    - Flexible **demand** (DSM)
    - **Electric Vehicle** (EV)
    - **Grid** expansion

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# Operational flexibility

- Ability of the system to withstand the uncertainty and variability in generation and electricity demand while maintaining the desired reliability at an affordable cost
- Measure: the contribution of each dispatchable technology to the variation of the (net) demand at different time horizons (monthly, weekly, daily)

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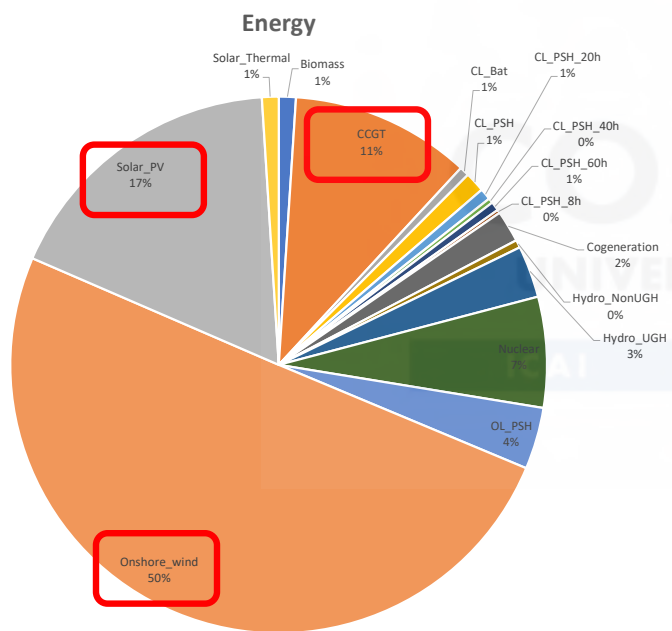
ICAI

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# System operation

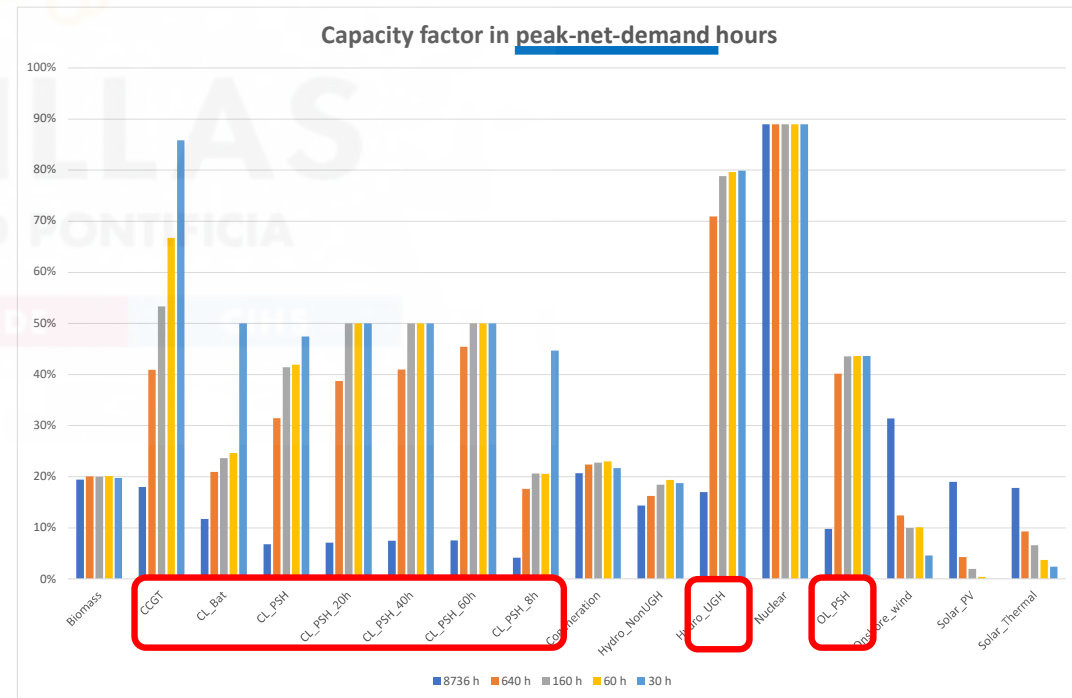
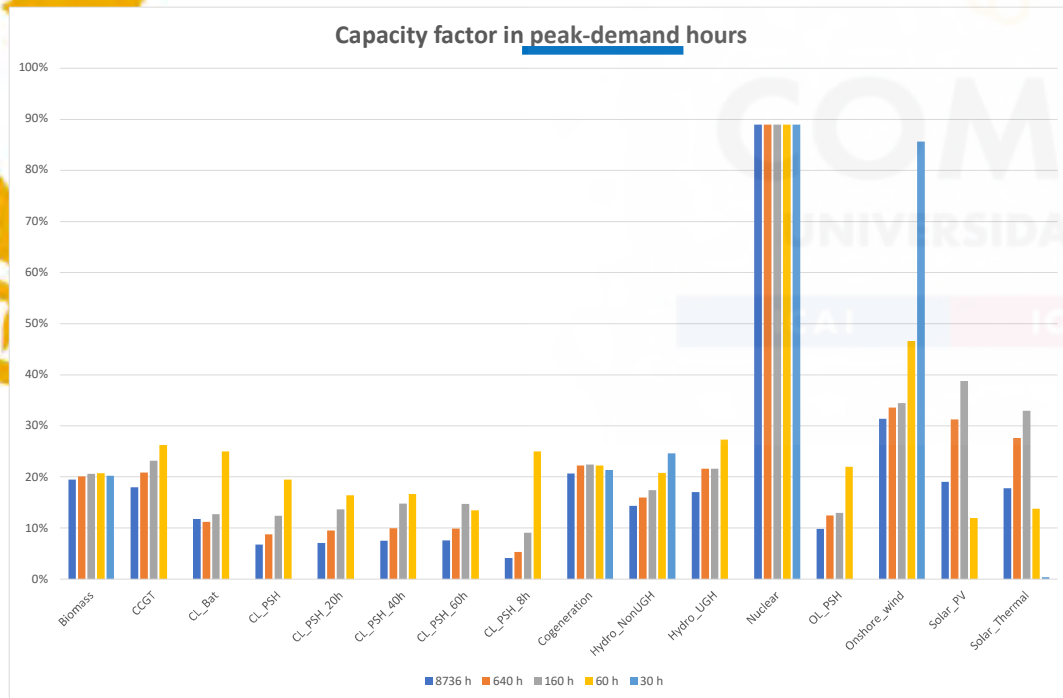
Energy demand: 334,270 GWh





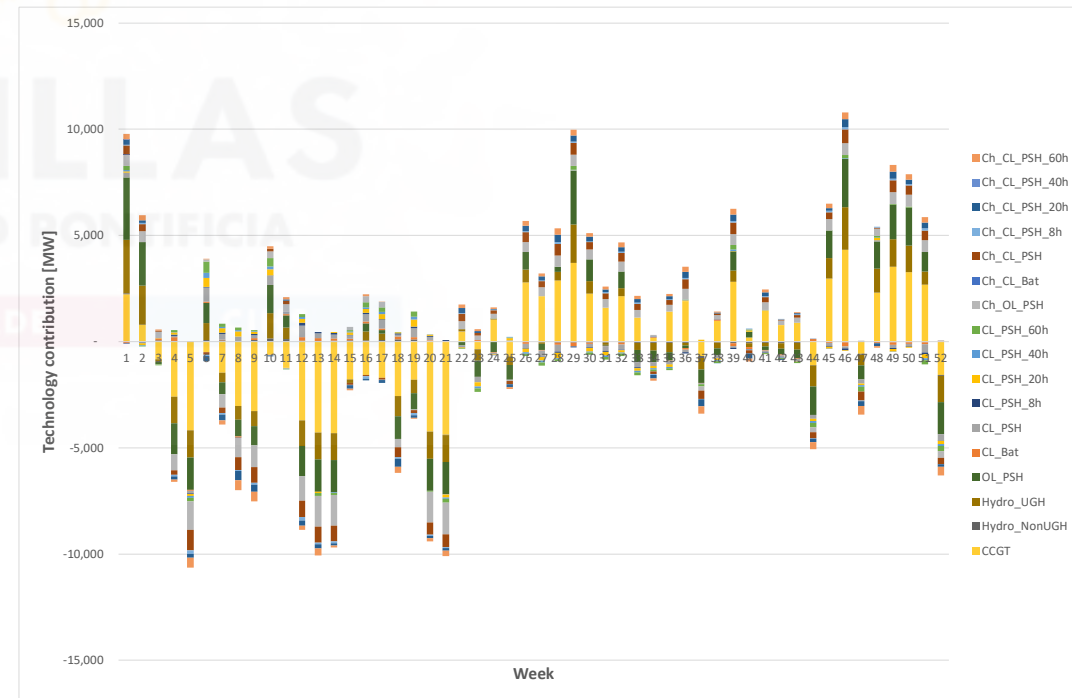
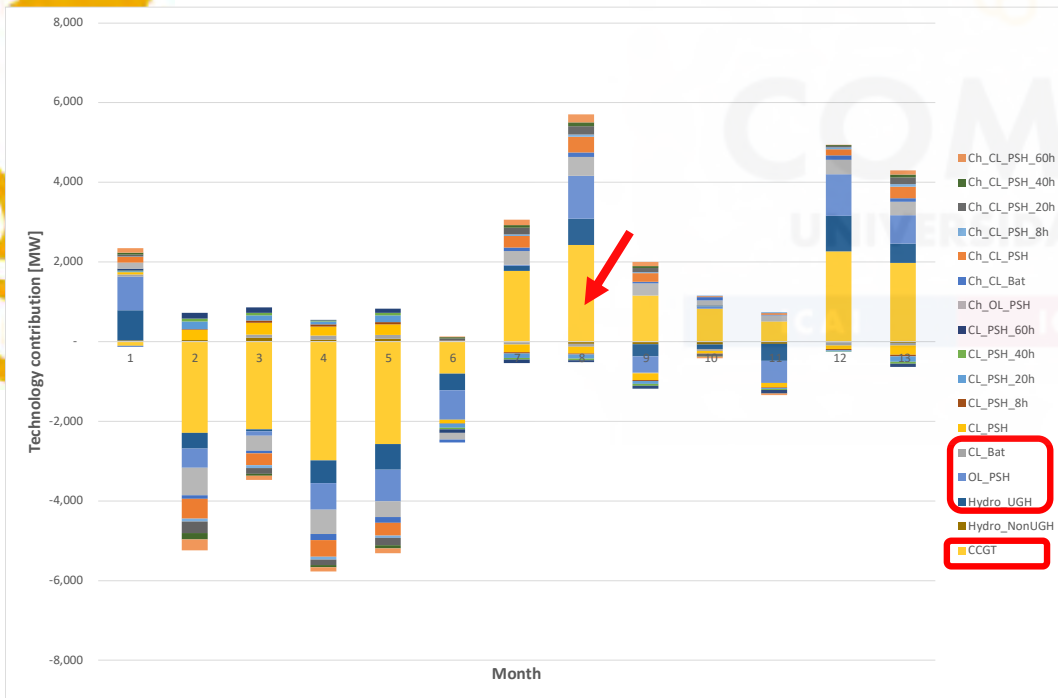
# Firmness/Electric Load Carrying Capability (ELCC)

- Capacity factors of the different technologies at peak hours of demand and net demand



# Flexibility

Technology contribution to the monthly/weekly variation of the net demand (difference between the value and its mean)



# Conclusions

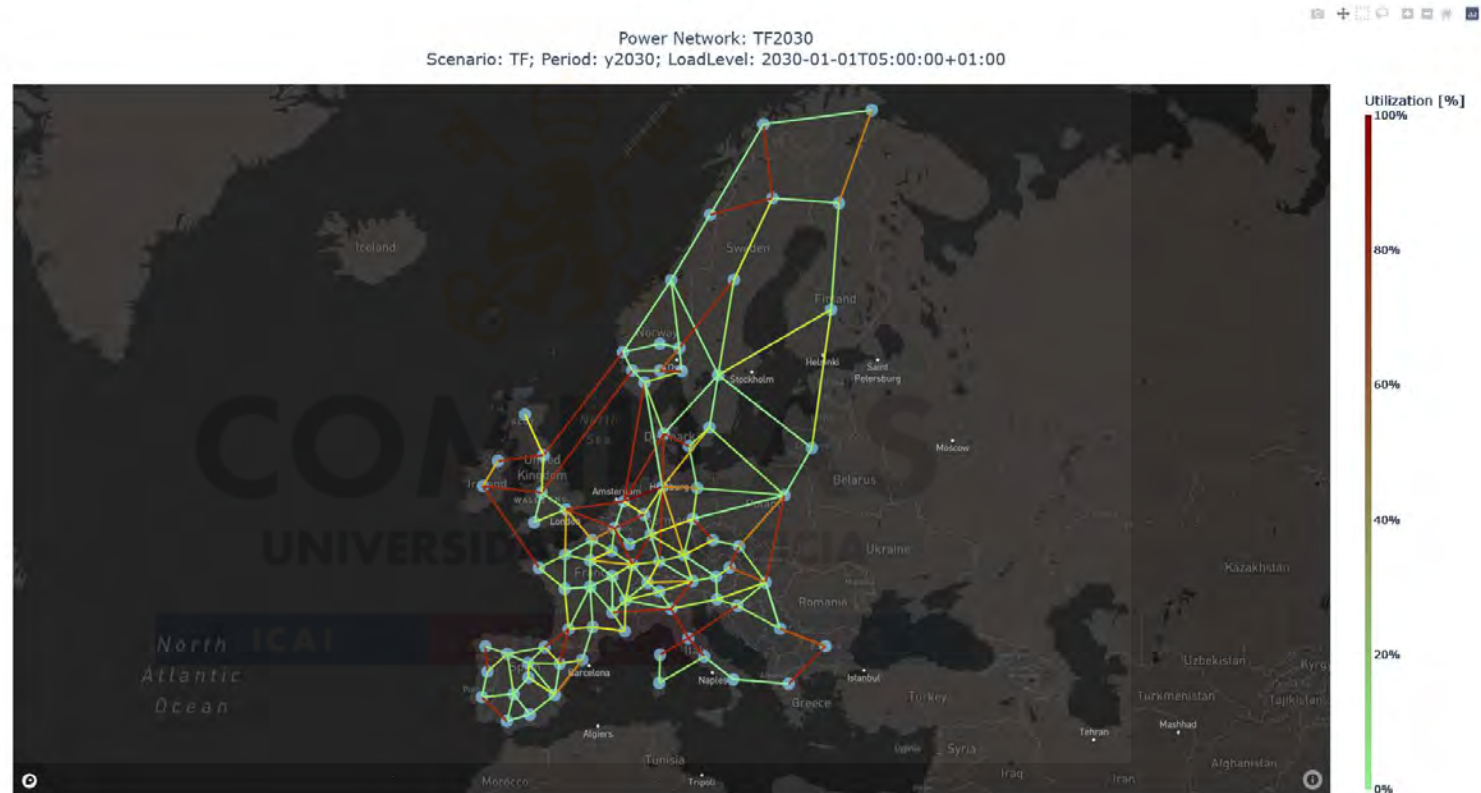
- Future electric systems with a **high share of VRES will require flexible generation and ESS**
- A **detailed operation model** is mandatory and suitable for capturing the operation of ESS
- At **peak net-demand hours, CCGT, hydro, open- and closed-loop PSH have larger capacity factors while VRES decrease their capacity factor**
- **Flexibility provided by CCGT, hydro, PSH, and batteries**
- **The higher the storage capacity the more ESS is used (PSH with large reservoirs preferred over smaller ones). Batteries compete with the PSH with small size (8 h)**



# MAF (Mid Term Adequacy Forecast) 2020

(<https://www.entsoe.eu/outlooks/maf/Pages/default.aspx>)

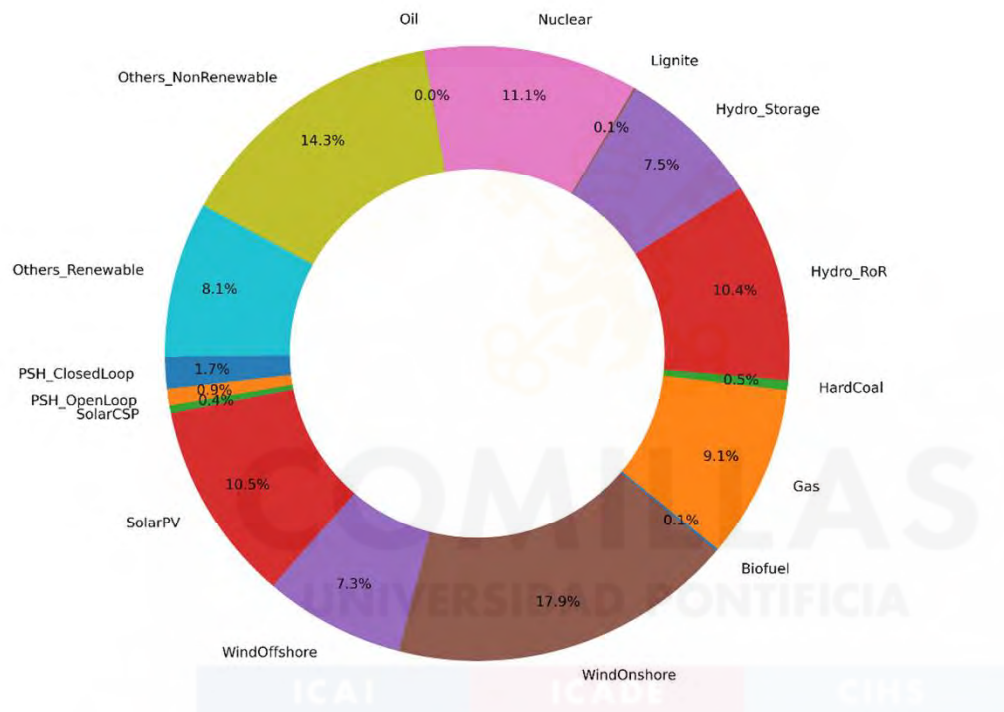
- How is the European system going to be in 2025 and 2030 from an adequacy point of view?



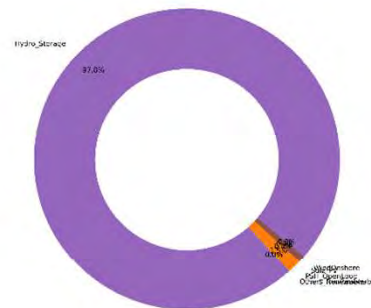
- Like Reliability Assessment and Performance Analysis done by NERC in the USA

# Energy generation mix

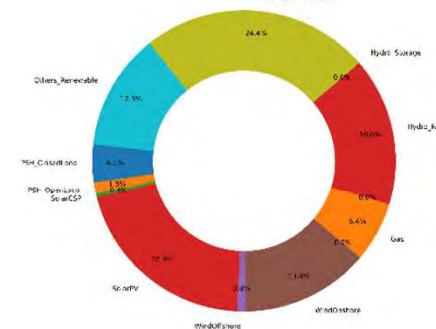
## Europe



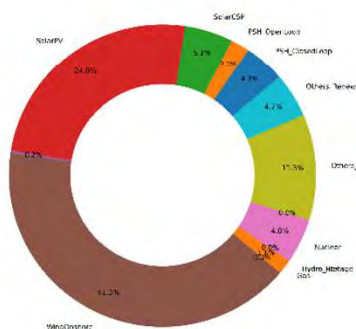
## Norway



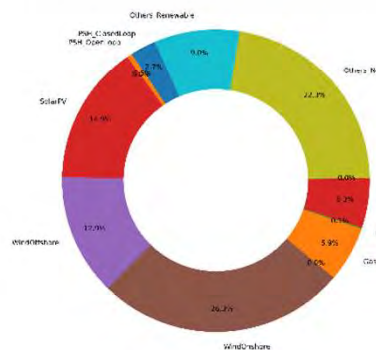
## Italy



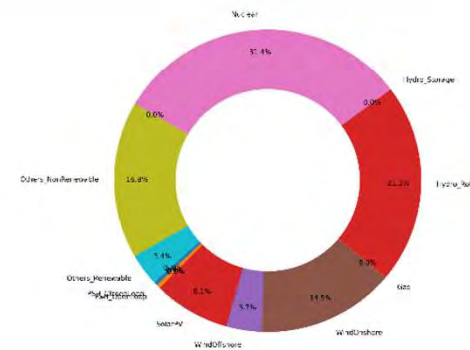
## Spain



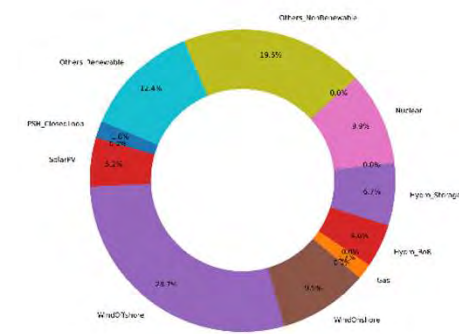
## Germany



## France



## UK





# Research projects (i)

- Hydro generation advanced systems: modeling, control, and optimized integration to the system (AVANHID), developed for **Iberdrola** under **NextGenerationEU** funds of the **Ministry of Science and Innovation** (CPP2021-009114). December 2022 - November 2025. [A. Ramos](#), [J.M. Latorre](#)
- Local markets for energy communities: designing efficient markets and assessing the integration from the electricity system perspective (OptiREC), developed under **NextGenerationEU** funds for the **Ministry of Science and Innovation** (TED2021-131365B-C43). December 2022 - November 2024. [A. Ramos](#), [J.P. Chaves](#), [J.M. Latorre](#), [M. Troncia](#)
- Delivering the next generation of open Integrated Assessment Models for Net-zero, sustainable Development (DIAMOND), developed for the **European Commission**. October 2022 - August 2025. [S. Lumbreras](#), [L. Olmos](#), [A. Ramos](#)

It will update, upgrade, and fully open six IAMs that are emblematic in scientific and policy processes, improving their sectoral and technological detail, spatiotemporal resolution, and geographic granularity. It will further enhance modelling capacity to assess the feasibility and desirability of Paris-compliant mitigation pathways, their interplay with adaptation, circular economy, and other SDGs, their distributional and equity effects, and their resilience to extremes, as well as robust risk management and investment strategies.

- [Application of the ENTSO-e cost-benefit analysis method to Aguayo II pumped-hydro storage](#), developed for **Repsol**. June 2022. [A. Ramos](#), [L. Olmos](#), [L. Sigrist](#)

It aims at writing a report on the application of the ENTSO-e cost-benefit analysis method to Aguayo II pumped-hydro storage.

- [Application of the ENTSO-e cost-benefit analysis method to Los Guájares pumped-hydro storage](#), developed for **VM Energía**. May 2022 - June 2022. [A. Ramos](#), [L. Olmos](#), [L. Sigrist](#)

It aims at writing a report on the application of the ENTSO-e cost-benefit analysis method to Los Guájares pumped-hydro storage.



# Research projects (ii)

- Impact of the electric vehicle in the electricity markets in 2030, developed for **Repsol**. November 2021 - February 2022. A. Ramos, P. Frías, J.P. Chaves, P. Linares, J.J. Valentín

It aims at analyzing the impact on the electricity markets of the mainland Spanish system of the high penetration of electric vehicles in a 2030 scenario.

- European Climate and Energy Modelling Forum (ECEMF), developed for the **European Commission**. May 2021 - December 2024. S. Lumbreras, A. Ramos, L. Olmos, C. Mateo, D. Santos Oliveira

It aims at providing the knowledge to inform the development of future energy and climate policies at national and European levels. In support of this aim, ECEMF proposes a range of activities to achieve five objectives and meet the four challenges set out in the call text. ECEMF's programme of events and novel IT-based communications channel will enable researchers to identify and co-develop the most pressing policy-relevant research questions with a range of stakeholders to meet ambitious European energy and climate policy goals, in particular the European Green Deal and the transformation to a climate neutral society.



- Assessment of the storage needs for the Spanish electric system in a horizon 2020-2050 with large share of renewables, developed for the **Instituto para la Diversificación y Ahorro de la Energía (IDAE)**. January 2021 - June 2022. A. Ramos, P. Linares, J.P. Chaves, J. García, S. Wogrin, J.J. Valentín

It aims at assessing, from a technical and economic point of view, the daily, weekly, and seasonal storage needs for the Spanish electricity system in the 2020-2050 horizon.



# Research projects (iii)

- FlexEner. New 100% renewable, flexible and robust energy system for the integration of new technologies in generation, networks and demand - Scenarios, developed for **Iberdrola** under **Misiones CDTI 2019** program (MIG-20201002). October 2020 - December 2023. M. Rivier, T. Gómez, A. Sánchez, F. Martín, T. Freire, J.P. Chaves, A. Ramos

It aims at investigating new technologies and simulation models in the field of renewable generation, storage systems and flexible demand management and operation of the distribution network. A 100% renewable and decarbonised energy mix is sought, effectively integrated into the electrical system of the future in a flexible, efficient and safe way.

- Improving energy system modelling tools and capacity, developed for the **European Commission**. October 2020 - June 2022. S. Lumbreras, A. Ramos, P. Linares, D. Santos, M. Pérez-Bravo, A.F. Rodríguez Matas, J.C. Romero

It aims at improving the description of the Spanish energy system in model TIMES-SINERGIA, from the technologies considered or a higher time resolution to the detailed modeling of the power sector, such as the inclusion of transmission constraints.

- MODESC – Platform of innovative models for speeding the energy transition towards a decarbonized economy, developed for the **Ministry of Science and Innovation** under **Retos Colaboración 2019** program (RTC2019-007315-3). September 2020 - December 2023. T. Gómez, M. Rivier, J.P. Chaves, A. Ramos, P. Linares, F. Martín, L. Herding

It aims at developing of a global platform that integrates innovative energy simulation and impact assessment models that allow speeding the decarbonization of the electricity system including the electrification of the energy demand.

# Research projects (iv)

- Open ENergy TRansition ANalyses for a low-carbon Economy (openENTRANCE), developed for the **European Union**. May 2019 - April 2023. L. Olmos, S. Lumbreras, A. Ramos, E. Alvarez

It aims at developing, using, and disseminating an open, transparent and integrated modelling platform for assessing low-carbon transition pathways in Europe.



- Analysis of the expansion and operation of the Spanish electricity system for a 2030-2050 time horizon, developed for **Iberdrola**. January 2019 - December 2021. M. Rivier, T. Gómez, A. Sánchez, F. Martín, T. Freire, J.P. Chaves, T. Gerres, S. Huclin, A. Ramos

It aims at evaluating the potential and role that each generation, storage and consumption technology can play in the future mix of the Spanish electricity system.



# StarNetLite\_TEPM Long-Term Transmission Expansion Model

([https://pascua.iit.comillas.edu/aramos/StarNetLite\\_TEPM.zip](https://pascua.iit.comillas.edu/aramos/StarNetLite_TEPM.zip))

- Files

- Microsoft Excel interface for input data and output results  
StarNetLite\_TEPM.xlsm
- GAMS file StarNetLite\_TEPM.gms

- How to run it from Windows

- Save the Excel workbook if data have changed

- Run the model

Run

- The model creates

- tmp\_StarNetLite\_TEPM.xlsx with the output results
- tmp\_StarNetLite\_TEPM.gdx with the output results
- StarNetLite\_TEPM.lst as the listing file of the GAMS execution

- Load the results into the Excel interface

Load results



# StarNetLite\_TEPM Long-Term Transmission Expansion Model

([https://pascua.iit.comillas.edu/aramos/StarNetLite\\_TEPM.zip](https://pascua.iit.comillas.edu/aramos/StarNetLite_TEPM.zip))

- Files
  - Text files for input data
  - GAMS file `StarNetLite_TEPM.gms`
- How to run it from MacOS
  - Run the model from GAMS Studio with these parameters
    - `u1= StarNetLite_TEPM u2=1 u3=1`
  - The model creates
    - `tmp_StarNetLite_TEPM.gdx` with the output results
    - `StarNetLite_TEPM.lst` as the listing file of the GAMS execution



# Menu

StarNet Lite Long Term Transmission Expansion Planning Model

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*Andrés Ramos*  
<https://www.iit.comillas.edu/aramos/>  
[andres.ramos@comillas.edu](mailto:andres.ramos@comillas.edu)

Run  
Load results

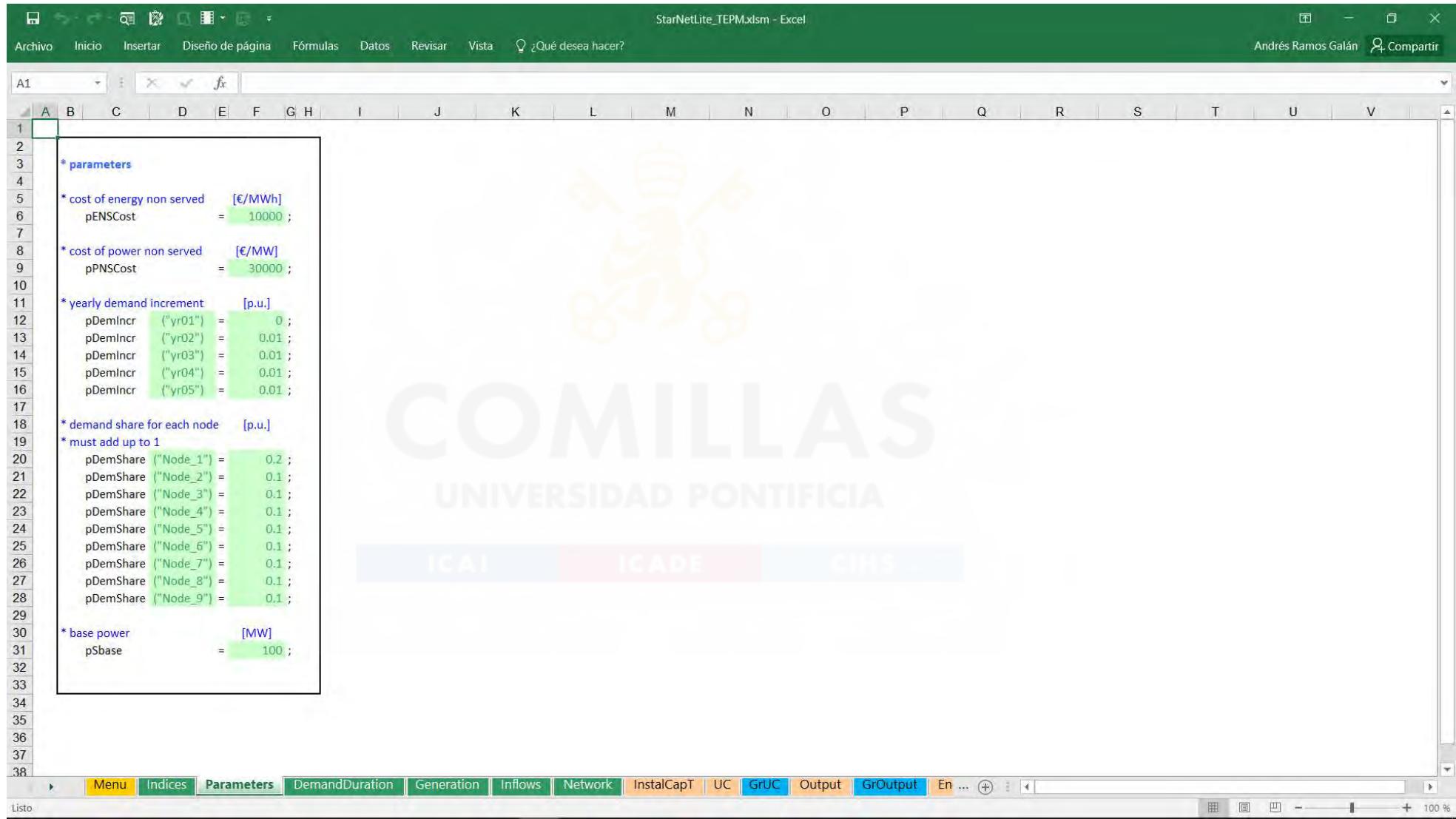
Menu Indices Parameters DemandDuration Generation Inflows Network InstalCapT UC GrUC Output GrOutput En ...



# Input Data. Indices

Index	Value
y	years / yr01 * yr05 /
p	periods / p01 * p12 /
s	subperiods / WeekDay , WeekEnd /
n	load levels / n01 * n03 /
sc	scenarios / sc01 * sc03 /
g	thermal units /
	Nuclear
	DomesticCoal_Anthracite
	BrownLignite
	ImportedCoal_SubBituminous
	ImportedCoal_Bituminous
	CCGT_1
	CCGT_2
	CCGT_3
	CCGT_4
	OCGT_1
	OCGT_2
	OCGT_3
	FuelOilGas
*	hydro plants
	RunOfRiver
	StorageHydro1_Basin1
	StorageHydro2_Basin1
	StorageHydro3_Basin1
	PumpedStorageHydro
r	reservoirs /
	RunOfRiver
	Reservoir1_Basin1
	Reservoir2_Basin1

# Input Data. Cost of energy or power not served. Demand growth. Base power



StarNetLite\_TEPM.xlsm - Excel

Archivo Inicio Insertar Diseño de página Fórmulas Datos Revisar Vista ¿Qué desea hacer? Andrés Ramos Galán Compartir

Parameter	Unit	Value
<b>* parameters</b>		
<b>* cost of energy non served</b> [€/MWh]		
pENSCost		= 10000 ;
<b>* cost of power non served</b> [€/MW]		
pPNSCost		= 30000 ;
<b>* yearly demand increment</b> [p.u.]		
pDemIncr ("yr01")		= 0 ;
pDemIncr ("yr02")		= 0.01 ;
pDemIncr ("yr03")		= 0.01 ;
pDemIncr ("yr04")		= 0.01 ;
pDemIncr ("yr05")		= 0.01 ;
<b>* demand share for each node</b> [p.u.]		
<b>* must add up to 1</b>		
pDemShare ("Node_1")		= 0.2 ;
pDemShare ("Node_2")		= 0.1 ;
pDemShare ("Node_3")		= 0.1 ;
pDemShare ("Node_4")		= 0.1 ;
pDemShare ("Node_5")		= 0.1 ;
pDemShare ("Node_6")		= 0.1 ;
pDemShare ("Node_7")		= 0.1 ;
pDemShare ("Node_8")		= 0.1 ;
pDemShare ("Node_9")		= 0.1 ;
<b>* base power</b> [MW]		
pSbase		= 100 ;

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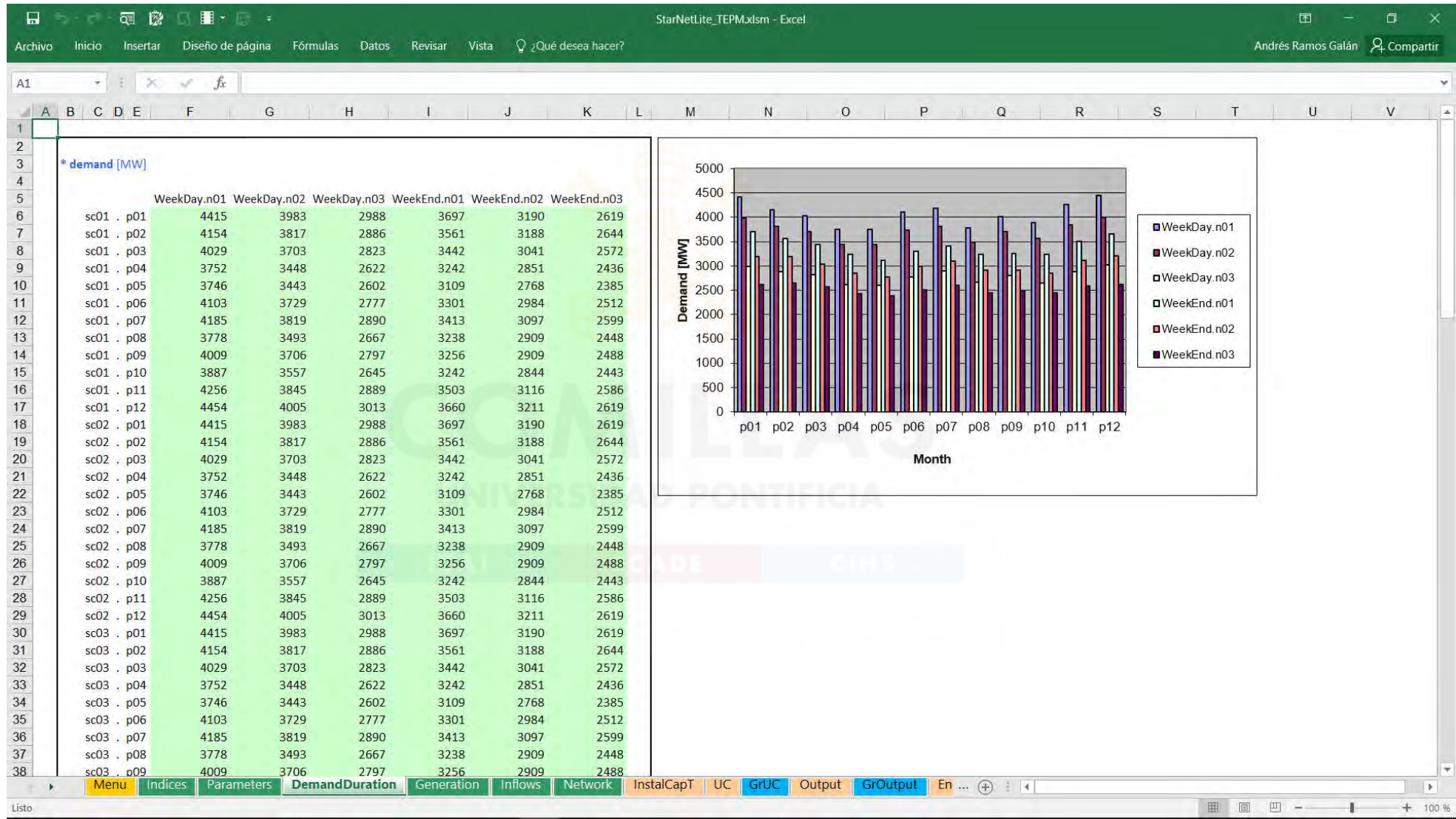
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Menu Indices Parameters DemandDuration Generation Inflows Network InstalCapT UC GrUC Output GrOutput En ...

Listo 100 %



# Input Data. Demand, operating reserve and duration





# Input Data. Thermal and hydro parameters

StarNetLite\_TEPm.xlsm - Excel

Archivo Inicio Insertar Diseño de página Fórmulas Datos Revisar Vista ¿Qué desea hacer? Andrés Ramos Galán Compartir

A1

* thermal generation										
	MaxProd	MinProd	FuelCost	SlopeVarCost	InterVarCost	OMVarCost	StartupCost	EFOR	Aux	
	[MW]	[MW]	[€/Mcal]	[Mcal/MWh]	[Mcal/h]	[€/MWh]	[Mcal]	[p.u.]	[€/MWh]	
Nuclear	771.6	771.6	1.00	15				0.00	15.00	
DomesticCoal_Anthracite	588.0	235.2	0.02	2400	50000	6	2000000	0.00	49.70	
BrownLignite	203.1	81.2	0.02	2300	50000	6	2000000	0.00	50.92	
ImportedCoal_SubBituminous	150.4	60.2	0.02	2300	50000	6	2000000	0.00	52.65	
ImportedCoal_Bituminous	194.4	77.8	0.02	2200	50000	6	2000000	0.00	49.14	
CCGT_1	500.0	100.0	0.03	800	300000	6	1000000	0.00	42.00	
CCGT_2	500.0	100.0	0.03	900	300000	4	1000000	0.00	45.00	
CCGT_3	500.0	100.0	0.03	1000	300000	4	1000000	0.00	48.00	
CCGT_4	667.5	133.5	0.03	800	300000	4	1000000	0.00	37.48	
OCGT_1	400.0		0.03	2000	100000	4		0.00	67.50	
OCGT_2	400.0		0.03	2100	100000	4		0.00	70.50	
OCGT_3	400.0		0.03	2200	100000	4		0.00	73.50	
FuelOilGas	441.8		0.06	2000	300000	3	1000000	0.00	160.74	

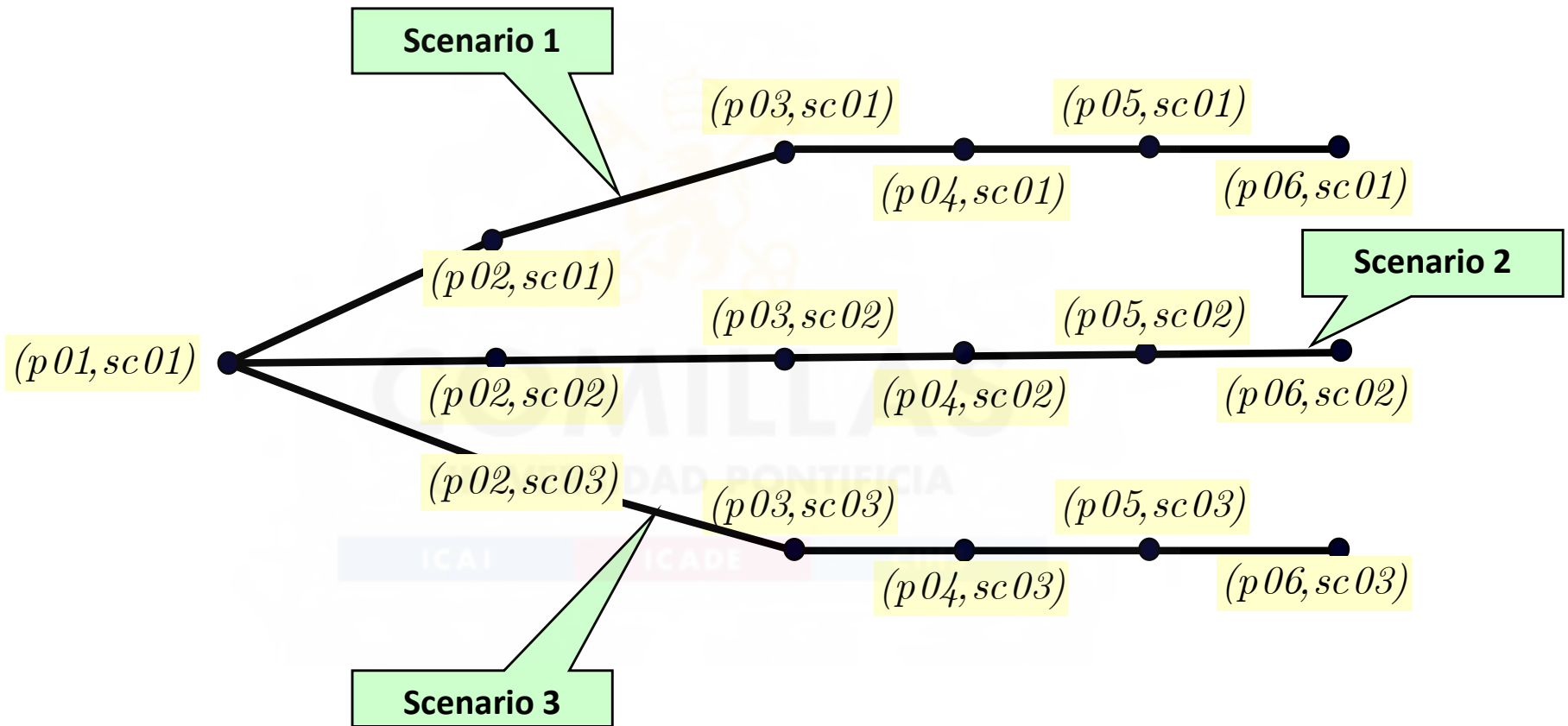
* hydro generation					
	MaxProd	MinProd	ProdFunc	Efficiency	MaxCons
	[MW]	[MW]	[kWh/m³]	[p.u.]	[MW]
RunOfRiver	150.0				
StorageHydro1_Basin1	200.0		0.30		
StorageHydro2_Basin1	200.0		0.30		
StorageHydro3_Basin1	200.0		0.30		
PumpedStorageHydro	200.0			0.70	200.0

* reservoir
-------------

Menu Indices Parameters DemandDuration Generation Inflows Network InstalCapT UC GrUC Output GrOutput En ...

# Scenario tree



# Input Data. Inflows

StarNetLite\_TEPM.xlsm - Excel

Archivo Inicio Insertar Diseño de página Fórmulas Datos Revisar Vista ¿Qué desea hacer?

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A1

		p01	p02	p03	p04	p05	p06	p07	p08	p09	p10	p11	p12
* natural hydro inflows [m³/s]													
RunOfRiver	. sc01	40.0	40.0	40.0	35.0	30.0	20.0	20.0	20.0	30.0	35.0	40.0	40.0
RunOfRiver	. sc02	40.0	38.0	38.0	33.3	28.5	19.0	19.0	19.0	28.5	33.3	38.0	38.0
RunOfRiver	. sc03	40.0	42.0	42.0	36.8	31.5	21.0	21.0	21.0	31.5	36.8	42.0	42.0
* RunOfRiver	. sc01	40.0	39.4	39.4	34.5	29.6	19.7	19.7	19.7	29.6	34.5	39.4	39.4
Reservoir1_Basin1	. sc01	34.5	48.7	66.2	76.1	33.6	10.4	5.4	15.3	14.6	16.1	62.7	157.1
Reservoir1_Basin1	. sc02	34.5	34.1	46.3	53.3	23.5	7.3	3.8	10.7	10.2	11.3	43.9	110.0
Reservoir1_Basin1	. sc03	34.5	65.7	89.4	102.7	45.4	14.0	7.3	20.7	19.7	21.7	84.6	212.1
* Reservoir1_Basin1	. sc01	34.5	44.6	60.6	69.6	30.7	9.5	4.9	14.0	13.4	14.7	57.4	143.7
Reservoir2_Basin1	. sc01	28.8	6.9	11.9	4.4	16.6	4.6	5.3	8.8	6.1	10.7	36.3	60.0
Reservoir2_Basin1	. sc02	28.8	5.2	8.9	3.3	12.5	3.5	4.0	6.6	4.6	8.0	27.2	45.0
Reservoir2_Basin1	. sc03	28.8	9.7	16.7	6.2	23.2	6.4	7.4	12.3	8.5	15.0	50.8	84.0
* Reservoir2_Basin1	. sc01	28.8	6.5	11.2	4.1	15.6	4.3	5.0	8.3	5.7	10.1	34.1	56.4
Reservoir3_Basin1	. sc01	113.8	54.9	101.0	21.2	29.6	54.9	25.3	16.8	21.2	21.2	33.7	168.4
Reservoir3_Basin1	. sc02	113.8	32.9	60.6	12.7	17.8	32.9	15.2	10.1	12.7	12.7	20.2	101.0
Reservoir3_Basin1	. sc03	113.8	76.8	141.4	29.7	41.5	76.8	35.4	23.6	29.7	29.7	47.1	235.7
* Reservoir3_Basin1	. sc01	113.8	48.3	88.9	18.7	26.1	48.3	22.2	14.8	18.7	18.7	29.6	148.1
* scenario tree													
		Ancestost	Peri	Prob									
	sc01	-1	1	0.500									
	sc02	-1	1	0.400									
	sc03	-1	1	0.100									

Menu Indices Parameters DemandDuration Generation Inflows Network InstalCapT UC GrUC Output GrOutput En ...

Listo 100%



# Input Data. Existing and candidate lines

StarNetLite\_TEPM.xlsm - Excel

Archivo Inicio Insertar Diseño de página Fórmulas Datos Revisar Vista ¿Qué desea hacer? Andrés Ramos Galán Compartir

A1

* existing transmission network					
	r	X	TTC	FixedCost	FxChargeRate
	[p.u.]	[p.u.]	[MW]	[M€]	[p.u.]
Node_1 . Node_6	0.002	0.020	800.0		
Node_2 . Node_3	0.004	0.030	800.0		
Node_2 . Node_6	0.006	0.040	800.0		
Node_3 . Node_4	0.008	0.050	800.0		
Node_3 . Node_6	0.007	0.060	800.0		
Node_4 . Node_5	0.005	0.070	800.0		
Node_4 . Node_6	0.003	0.080	800.0		
Node_4 . Node_9	0.001	0.070	800.0		
Node_6 . Node_7	0.003	0.060	800.0		
Node_6 . Node_8	0.005	0.050	800.0		
Node_7 . Node_8	0.007	0.040	800.0		
Node_8 . Node_9	0.006	0.030	800.0		
* new transmission network					
	r	X	TTC	FixedCost	FxChargeRate
	[p.u.]	[p.u.]	[MW]	[M€]	[p.u.]
Node_1 . Node_4	0.006	0.030	800.0	100.0	0.075

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Menu Indices Parameters DemandDuration Generation Inflows Network InstalCapT UC GrUC Output GrOutput En ...

Listo 100%

# StarNetLite\_TEPM (i)

\$Title StarNet Lite Long Term Transmission Expansion Planning Model (TEPM)

\$OnText

*Developed by*

*Andrés Ramos  
Instituto de Investigacion Tecnologica  
Escuela Tecnica Superior de Ingenieria - ICAI  
UNIVERSIDAD PONTIFICIA COMILLAS  
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28015 Madrid, Spain  
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[https://pascua.iit.comillas.edu/aramos/Ramos\\_CV.htm](https://pascua.iit.comillas.edu/aramos/Ramos_CV.htm)*

*October 23, 2017*

\$OffText

\$OnEmpty OnMulti OffListing

*\* options to skip or not the Excel input/output  
\* if you want to skip it put these values to 1  
\* in such a case input files have to be already in the directory created by any other means  
\* output file will be the tmp.gdx that can be exported to Excel manually*

\$ifthen.OptSkipExcelInput %gams.user2% == ""

\$ setglobal OptSkipExcelInput 0

\$else.OptSkipExcelInput

\$ setglobal OptSkipExcelInput %gams.user2%

\$endif.OptSkipExcelInput

\$ifthen.OptSkipExcelOutput %gams.user3% == ""

\$ setglobal OptSkipExcelOutput 0

\$else.OptSkipExcelOutput

\$ setglobal OptSkipExcelOutput %gams.user3%

\$endif.OptSkipExcelOutput

*\* solve the optimization problems until relative optimality of 1 %*

**option** OptcR = 0.01, IterLim=1000000, ResLim=3600, MINLP=SBB

# StarNetLite\_TEPM (ii)

\* definitions

## sets

```

y          year
ly(y)     not last year
z (y)     year
p          period
p1(p)     first  period
pn(p)     last   period
s          subperiod
s1(s)     first subperiod
n          load level
n1(n)     first load level
sc         scenario
sca (sc   ) scenario
scp (sc,p ) tree defined as scenario and period
scscp(sc,p,sc) ancestor      sc2   of node (sc1 p)
scsch(sc,sc,p) descendant   (sc2 p) of node  sc1
scscr(sc,p,sc) representative sc2   of node (sc1 p)
spsn(sc,p,s,n) active load levels for each scenario
psn (   p,s,n) active load levels

g          generating unit
t (g)     thermal  unit
h (g)     hydro    plant
r          reservoir
rs(r)     storage  reservoir
ruh(r,g)  reservoir  upstream of      hydro plant
rph(r,g)  reservoir  upstream of pumped hydro plant
hur(g,r)  hydro plant upstream of reservoir
hpr(g,r)  pumped hydro plant upstream of reservoir
rur(r,r)  reservoir 1 upstream of reservoir 2

nd         node (bus)
la(nd,nd) existing and candidate lines
lc(nd,nd) candidate lines
le(nd,nd) existing      lines
gnd(g,nd) location of a unit at a node

```

alias (sc,scc), (r,rr), (nd,ni,nf)



# StarNetLite\_TEPM (iii)

## parameters

pDemand	( sc, p,s,n)	hourly load by node	[GW]
pDemShare	( nd )	demand share	[p.u.]
pOperReserve	( sc, p,s,n)	hourly operating reserve	[GW]
pDuration	( p,s,n)	duration	[h]
pCommitt	( y,sc,g, p,s )	commitment of the unit	[0-1]
pProduct	( y,sc,g, p,s,n)	production of the unit	[MW]
pEnergy	( y,sc,g, p,s,n)	energy of the unit	[MWh]
pLRMC	( y,sc,nd, p,s,n)	long run marginal cost	[€ per MWh]
pReserve	( y,sc,r, p )	reservoir level	[hm <sup>3</sup> ]
pWValue	( y,sc,r, p )	water value	[M€ per hm <sup>3</sup> ]
pFlow	( y,sc,nd,nd,p,s,n)	flow	[MW]
pTheta	( y,sc,nd, p,s,n)	voltage angle	[rad]
pInstalCapT	( nd,nd,y)	TEP investment decision	[0-1]
pDemIncr	( y)	yearly demand increase	[p.u.]
pCumDemIncr	( y)	cum yearly demand increase	[p.u.]
pOrder	( y)	ordinal of the year	
pEFOR	( g)	EFOR	[p.u.]
pMaxProd	( g)	maximum output	[GW]
pMinProd	( g)	minimum output	[GW]
pMaxCons	( g)	maximum consumption	[GW]
pSlopeVarCost	( g)	slope variable cost	[M€ per GWh]
pInterVarCost	( g)	intercept variable cost	[M€ per h]
pStartupCost	( g)	startup cost	[M€]
pMaxReserve	( r)	maximum reserve	[km <sup>3</sup> ]
pMinReserve	( r)	minimum reserve	[km <sup>3</sup> ]
pIniReserve	( r)	initial reserve	[km <sup>3</sup> ]
pProdFunct	( g)	production function	[GWh per km <sup>3</sup> ]
pEffic	( g)	pumping efficiency	[p.u.]
pInflows	( r,sc,p)	inflows	[km <sup>3</sup> ]
pENSCost		energy non-served cost	[M€ per GWh]
pPNSCost		power non-served cost	[M€ per GW]
pProbsc	( sc,p)	probability of a given period	
pR	( nd,nd)	line resistance	[p.u.]
pX	( nd,nd)	line reactance	[p.u.]
pTTC	( nd,nd)	total transfer capacity	[GW]
pFixedCost	( nd,nd)	fixed cost	[M€]
pSbase		base power	[GW]
lag(p)		backward counting of period	
scaux		scenario number	

# StarNetLite\_TEPM (iv)

## variables

vTotalTCost	total system cost	[M€]
vTotalFCost	total system fixed cost	[M€]
vTotalVCost	total system variable cost	[M€]

## binary variables

vCommitt (y,sc,p,s, g)	commitment of the unit	[0-1]
vStartup (y,sc,p,s, g)	startup of the unit	[0-1]
vShutdown (y,sc,p,s, g)	shutdown of the unit	[0-1]
vCumInstDc(y, nd,nd)	installation decision in year y	[0-1]

## positive variables

vProduct (y,sc,p,s,n,g)	production of the unit	[GW]
vConsump (y,sc,p,s,n,g)	consumption of the unit	[GW]
vLosses (y,sc,p,s,n,nd)	losses in a node	[GW]
vENS (y,sc,p,s,n,nd)	energy non served	[GW]
vPNS (y,sc,p,s )	power non served	[GW]
vWtReserve(y,sc,p, r)	water reserve at end of period	[km3]
vSpillage (y,sc,p, r)	spillage	[km3]

## variables

vFlow (y,sc,p,s,n,nd,nd)	flow	[GW]
vTheta (y,sc,p,s,n,nd )	voltage angle	[rad]

## equations

eTotalTCost	total system cost	[M€]
eTotalFCost	total system fixed cost	[M€]
eTotalVCost	total system variable cost	[M€]
eOpReserve(y,sc,p,s,n )	operating reserve	[GW]
eBalance (y,sc,p,s,n,nd )	load generation balance	[GW]
eInstlCapC(y, nd,nd )	consecutive installed capacity	[GW]
eInstlCap1(y,sc,p,s,n,nd,nd)	max flow by installed capacity	[GW]
eInstlCap2(y,sc,p,s,n,nd,nd)	max flow by installed capacity	[GW]
eFlowNetN1(y,sc,p,s,n,nd,nd)	flow for each candidate line	[GW]
eFlowNetN2(y,sc,p,s,n,nd,nd)	flow for each candidate line	[GW]
eFlowNetEx(y,sc,p,s,n,nd,nd)	flow for each existing line	[GW]
eLosses (y,sc,p,s,n,nd )	losses in a node	[GW]
eMaxOutput(y,sc,p,s,n,g)	max output of a committed unit	[GW]
eMinOutput(y,sc,p,s,n,g)	min output of a committed unit	[GW]
eProdctPer(y,sc,p,s,n,g)	unit production in same period	[GW]
eStrtUpPer(y,sc,p,s, g)	unit startup in same period	
eStrtUpNxt(y,sc,p,s, g)	unit startup in next period	
eWtReserve(y,sc,p, r)	water reserve	[km3] ;

# StarNetLite\_TEPM (v)

\* mathematical formulation

```

eTotalTCost .. vTotalTCost =e= vTotalFCost + vTotalVCost ;

eTotalFCost .. vTotalFCost =e= sum[(y,lc), pFixedCost(lc)*vCumInstDc(y,lc)] ;

eTotalVCost .. vTotalVCost =e= sum[(y,spsn(sc,p,s,n),nd), pProbSc(sc,p)*pDuration(p,s,n)*pENSCost *vENS (y,sc,p,s,n,nd)] +
sum[(y,scp (sc,p),s ), pProbSc(sc,p) *pPNSCost *vPNS (y,sc,p,s )] +
sum[(y,scp (sc,p),s, t ), pProbSc(sc,p) *pStartupCost (t)*vStartup(y,sc,p,s, t )] +
sum[(y,spsn(sc,p,s,n),t ), pProbSc(sc,p)*pDuration(p,s,n)*pInterVarCost(t)*vCommitt(y,sc,p,s, t )] +
sum[(y,spsn(sc,p,s,n),t ), pProbSc(sc,p)*pDuration(p,s,n)*pSlopeVarCost(t)*vProduct(y,sc,p,s,n,t )] ;

eOpReserve(y,spsn(sc,p,s,n1(n) )) $pOperReserve(sc,p,s,n) .. sum[t, pMaxProd(t)*vCommitt(y,sc,p,s, t)] + sum[h, pMaxProd( h)] + vPNS(y,sc,p,s ) =g= [pDemand(sc,p,s,n) + pOperReserve(sc,p,s,n)] *
pCumDemIncr(y) ;
eBalance (y,spsn(sc,p,s, n), nd ) .. sum[gnd(g,nd), vProduct(y,sc,p,s,n,g)] - sum[gnd(h,nd), vConsump(y,sc,p,s,n,h)] + vENS(y,sc,p,s,n,nd) =e= pDemand(sc,p,s,n) * pDemShare(nd) *
pCumDemIncr(y) +
sum[la(nd,nf), vFlow(y,sc,p,s,n,nd,nf)] - sum[la(ni,nd), vFlow(y,sc,p,s,n,ni,nd)] + vLosses(y,spsn,nd) ;

eInstlCapC(ly(y),lc ) .. vCumInstDc(y,lc) =l= vCumInstDc(y+1,lc) ;

eInstlCap1(y,spsn(sc,p,s, n),lc(ni,nf)) .. vFlow(y,sc,p,s,n,ni,nf) / pTTC(ni,nf) =g= vCumInstDc(y,ni,nf) ;
eInstlCap2(y,spsn(sc,p,s, n),lc(ni,nf)) .. vFlow(y,sc,p,s,n,ni,nf) / pTTC(ni,nf) =l= vCumInstDc(y,ni,nf) ;
eFlowNetN1(y,spsn(sc,p,s, n),lc(ni,nf)) .. vFlow(y,sc,p,s,n,ni,nf) / 1e3*pTTC(ni,nf) =g= [vTheta(y,sc,p,s,n,ni) - vTheta(y,sc,p,s,n,nf)] * pSbase / pX(ni,nf) / 1e3*pTTC(ni,nf) - 1 + vCumInstDc(y,ni,nf) ;
eFlowNetN2(y,spsn(sc,p,s, n),lc(ni,nf)) .. vFlow(y,sc,p,s,n,ni,nf) / 1e3*pTTC(ni,nf) =l= [vTheta(y,sc,p,s,n,ni) - vTheta(y,sc,p,s,n,nf)] * pSbase / pX(ni,nf) / 1e3*pTTC(ni,nf) + 1 - vCumInstDc(y,ni,nf) ;
eFlowNetEx(y,spsn(sc,p,s, n),le(ni,nf)) .. vFlow(y,sc,p,s,n,ni,nf) =e= [vTheta(y,sc,p,s,n,ni) - vTheta(y,sc,p,s,n,nf)] * pSbase / pX(ni,nf) ;

eLosses(y,spsn(sc,p,s,n),nd) .. vLosses(y,sc,p,s,n,nd) =e= pSbase * sum[la(ni,nd), (1-cos(vTheta(y,sc,p,s,n,ni) - vTheta(y,sc,p,s,n,nd)))] * pR(la)/[sqr(pR(la))+sqr(pX(la))] +
pSbase * sum[la(nd,nf), (1-cos(vTheta(y,sc,p,s,n,nd) - vTheta(y,sc,p,s,n,nf)))] * pR(la)/[sqr(pR(la))+sqr(pX(la))] ;

eMaxOutput(y,spsn(sc,p,s,n),t) $pMaxProd(t) .. vProduct(y,sc,p,s,n,t) / pMaxProd(t) =l= vCommitt(y,sc,p,s,t) ;
eMinOutput(y,spsn(sc,p,s,n),t) $pMinProd(t) .. vProduct(y,sc,p,s,n,t) / pMinProd(t) =g= vCommitt(y,sc,p,s,t) ;

eProdctPer(y,spsn(sc,p,s1(s),n),g) .. vProduct(y,sc,p,s+1,n,g) =l= vProduct(y,sc,p,s,n,g) ;

eStrtUpPer(y,scp(sc,p),s1(s),t) $[card(s) > 1] .. vCommitt(y,sc,p,s+1,t) =g= vCommitt(y,sc,p,s,t) + vStartup(y,sc,p,s+1,t) - vShutdown(y,sc,p,s+1,t) ;
eStrtUpNxt(y,scp(sc,p),s1(s),t) $[card(s) > 1 and not p1(p)] .. vCommitt(y,sc,p,s,t) =g= sum[scscsp(sc,p,scc), vCommitt(y,sc,p-1,s+1,t)] + vStartup(y,sc,p,s,t) - vShutdown(y,sc,p,s,t) ;

eWtReserve(y,scp(sc,p), r) .. sum[scscsp(sc,p,scc), vWtReserve(y,scc,p-1,r)] + pIniReserve(r) $p1(p) - vWtReserve(y,sc,p,r) +
pInflows(r,sc,p) - vSpillage(y,sc,p,r) + sum[rur(rr,r), vSpillage(y,sc,p,rr)] +
sum{(s,n), pDuration(p,s,n)*sum[hur(h,r), vProduct(y,sc,p,s,n,h)/pProdFunc(h)]} -
sum{(s,n), pDuration(p,s,n)*sum[ruh(r,h), vProduct(y,sc,p,s,n,h)/pProdFunc(h)]} +
sum{(s,n), pDuration(p,s,n)*sum[hpr(h,r), vConsump(y,sc,p,s,n,h)/pProdFunc(h)*pEffic(h)]} -
sum{(s,n), pDuration(p,s,n)*sum[rph(r,h), vConsump(y,sc,p,s,n,h)/pProdFunc(h)*pEffic(h)]} =e= 0 ;

model mTEPM / all - eLosses / ;
mTEPM.SolPrint = 1 ; mTEPM.HoldFixed = 1 ; mTEPM.TryLinear = 1 ;

```



# StarNetLite\_TEPM (vi)

*\* read input data from Excel and include into the model*

```
file TMP / tmp_%gams.user1%.txt /
$OnEcho > tmp_%gams.user1%.txt
r1= indices
o1=tmp_indices.txt
r2= param
o2=tmp_param.txt
r3= demand
o3=tmp_demand.txt
r4= oprres
o4=tmp_oprres.txt
r5= duration
o5=tmp_duration.txt
r6= thermalgen
o6=tmp_thermalgen.txt
r7= hydrogen
o7=tmp_hydrogen.txt
r8= reservoir
o8=tmp_reservoir.txt
r9= inflows
o9=tmp_inflows.txt
r10= tree
o10=tmp_tree.txt
r11= network
o11=tmp_network.txt
```

\$OffEcho

*\* Mac OS X and Linux users must comment the following call and copy and paste the named ranges of the Excel interface into the txt files*

```
$ifthen.OptSkipExcelInput '%OptSkipExcelInput%' == '0'
$call xls2gms m i="%gams.user1%.xls" @"tmp_%gams.user1%.txt"
$else.OptSkipExcelInput
$ log Excel input skipped
$endif.OptSkipExcelInput
```

sets

```
$include tmp_indices.txt
;
$include tmp_param.txt
table pDemand(sc,p,s,n)
$include tmp_demand.txt
table pOperReserve(sc,p,s,n)
$include tmp_oprres.txt
table pDuration(p,s,n)
$include tmp_duration.txt
table pThermalGen(g,*)
$include tmp_thermalgen.txt
table pHydroGen(g,*)
$include tmp_hydrogen.txt
table pReservoir(r,*)
$include tmp_reservoir.txt
table pInflows(r,sc,p)
$include tmp_inflows.txt
table pScnTree(sc,*)
$include tmp_tree.txt
table pNetwork(nd,nd,*)
$include tmp_network.txt
;
```

*\* Mac OS X and Linux users must comment the following execute*

```
execute 'del tmp_%gams.user1%.txt tmp_indices.txt tmp_param.txt tmp_demand.txt tmp_oprres.txt tmp_duration.txt tmp_thermalgen.txt tmp_hydrogen.txt tmp_reservoir.txt tmp_inflows.txt tmp_tree.txt tmp_network.txt' ;
```



# StarNetLite\_TEPM (vii)

*\* determine the first and last period and the first subperiod*

$p1(p) \quad \text{\$}[\text{ord}(p) = 1] = \text{yes} ;$   
 $s1(s) \quad \text{\$}[\text{ord}(s) = 1] = \text{yes} ;$   
 $n1(n) \quad \text{\$}[\text{ord}(n) = 1] = \text{yes} ;$   
 $pn(p) \quad \text{\$}[\text{ord}(p) = \text{card}(p)] = \text{yes} ;$   
 $psn(p,s,n) \quad \text{\$}pDuration(p,s,n) = \text{yes} ;$   
 $lag(p) \quad = \text{card}(p) - 2*\text{ord}(p) + 1 ;$

*\* assignment of thermal units, storage hydro and pumped storage hydro plants*

$t(g) \quad \text{\$}[\text{pThermalGen}(g, 'MaxProd') \text{ and } \text{pThermalGen}(g, 'FuelCost')] = \text{yes} ;$   
 $h(g) \quad \text{\$}[\text{pHydroGen}(g, 'MaxProd')] = \text{yes} ;$   
 $rs(r) \quad \text{\$}[\text{pReservoir}(r, 'MaxReserve') > 0] = \text{yes} ;$

*\* compute the cumulative yearly demand growth*

$ly(y) \quad \text{\$}[\text{ord}(y) < \text{card}(y)] = \text{yes} ;$   
 $z \quad (y) = \text{yes} ;$   
 $pOrder \quad (y) = \text{ord}(y) ;$   
 $pCumDemIncr(y) = \text{prod}[z \quad \text{\$}[\text{pOrder}(z) \leq \text{ord}(y)], 1+\text{pDemIncr}(z)] ;$

# StarNetLite\_TEPM (viii)

```

* scaling of parameters

pDemand      (sc,p,s,n) = pDemand      (sc,p,s,n)      * 1e-3 ;
pOperReserve(sc,p,s,n) = pOperReserve(sc,p,s,n)      * 1e-3 ;
pENSCost      = pENSCost      * 1e-3 ;
pPNSCost      = pPNSCost      * 1e-3 ;

pEFOR        (t) = pThermalGen(t,'EFOR'      )      ;
pMaxProd      (t) = pThermalGen(t,'MaxProd'   ) * 1e-3 * [1-pEFOR(t)] ;
pMinProd      (t) = pThermalGen(t,'MinProd'   ) * 1e-3 * [1-pEFOR(t)] ;
pSlopeVarCost(t) = pThermalGen(t,'OMVarCost'  ) * 1e-3 +
                  pThermalGen(t,'SlopeVarCost') * 1e-3 * pThermalGen(t,'FuelCost') ;
pInterVarCost(t) = pThermalGen(t,'InterVarCost') * 1e-6 * pThermalGen(t,'FuelCost') ;
pStartupCost (t) = pThermalGen(t,'StartupCost') * 1e-6 * pThermalGen(t,'FuelCost') ;

pMaxProd      (h) = pHydroGen (h,'MaxProd'   ) * 1e-3 ;
pMinProd      (h) = pHydroGen (h,'MinProd'   ) * 1e-3 ;
pMaxCons      (h) = pHydroGen (h,'MaxCons'   ) * 1e-3 ;
pProdFunct    (h) = pHydroGen (h,'ProdFunct'  ) * 1e+3 ;
pEffic        (h) = pHydroGen (h,'Efficiency'  )      ;
pMaxReserve   (r) = pReservoir (r,'MaxReserve') * 1e-3 ;
pMinReserve   (r) = pReservoir (r,'MinReserve') * 1e-3 ;
pIniReserve   (r) = pReservoir (r,'IniReserve') * 1e-3 ;

pInflows(r,sc,p) = pInflows (r,sc,p      ) * 1e-6 * 3.6*sum[(s,n), pDuration(p,s,n)] ;

pR            (ni,nf) = pNetwork (ni,nf,'R'   )      ;
pX            (ni,nf) = pNetwork (ni,nf,'X'   )      ;
pTTC          (ni,nf) = pNetwork (ni,nf,'TTC'  ) * 1e-3 ;
pFixedCost(ni,nf) = pNetwork (ni,nf,'FixedCost') * pNetwork(ni,nf,'FxChargeRate') ;

pSbase        = pSbase      * 1e-3 ;

* assignment of all network lines (La) candidate lines (Lc) and existing lines (Le)

la( ni,nf ) $pX      (ni,nf) = yes ;
lc( ni,nf ) $pFixedCost(ni,nf) = yes ;
le(la(ni,nf)) $[not lc(ni,nf)] = yes ;

* if the production function of a hydro plant is 0, it is changed to 1 and scaled to 1000
* if the efficiency of a hydro plant is 0, it is changed to 1

pProdFunct(h) $[pProdFunct(h) = 0] = 1e3 ;
pEffic (h) $[pEffic (h) = 0] = 1 ;

```



# StarNetLite\_TEPM (ix)

*\* bounds on variables*

```
vProduct.up (y,sc,p,s,n,g) = pMaxProd(g) ;  
vConsump.up (y,sc,p,s,n,g) = pMaxCons(g) ;
```

```
vPNS.up (y,sc,p,s) = sum[n1(n), [pDemand(sc,p,s,n) + pOperReserve(sc,p,s,n)] * pCumDemIncr(y)] ;  
vENS.up (y,sc,p,s,nd) = pDemand(sc,p,s,n) * pDemShare(nd) * pCumDemIncr(y) ;
```

```
vWtReserve.up(y,sc,p,r) = pMaxReserve(r) ;  
vWtReserve.lo(y,sc,p,r) = pMinReserve(r) ;  
vWtReserve.fx(y,sc,p,r) $pn(p) = pIniReserve(r) ;
```

```
vFlow.lo (y,sc,p,s,n,la) = - pTTC(la) ;  
vFlow.up (y,sc,p,s,n,la) = pTTC(la) ;
```

*\* voltage angle of the reference node is fixed to 0*

```
vTheta.fx (y,sc,p,s,n,nd) $[ord(nd) = 1] = 0 ;
```

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# StarNetLite\_TEPM (x)

*\* define the nodes of the scenario tree and determine ancestor sc2 of node (sc1 p) and descendant (sc2 p) of node sc1*

```
scp ( sc,p ) $[ord(p) >= pScnTree(sc,'FirstPeriod')] = yes ;
scscp(scscp(sc,p),scc) $[ord(p) > pScnTree(sc,'FirstPeriod') and ord(scc) = ord(sc)] = yes ;
scscp(scscp(sc,p),scc) $[ord(p) = pScnTree(sc,'FirstPeriod') and ord(scc) = pScnTree(sc,'Ancestor')] = yes ;
scsch(sc,scp(scc,p)) $scscp(scc,p,sc) = yes ;
```

```
pProbSc(sc,pn(p)) = pScnTree(sc,'Prob')/sum[scc, pScnTree(scc,'Prob')] ;
loop (p $[not p1(p)],
  pProbSc(scp(sc,p+lag(p))) = sum[scsch(sc,scc,p+(lag(p)+1)), pProbSc(scc,p+(lag(p)+1))] ;
) ;
```

*\* delete branches with probability 0 and define the active Load Levels*

```
scp ( sc,p ) $[pProbSc(sc,p) = 0] = no ;
scscp( sc,p ,scc) $[pProbSc(sc,p) = 0 or pProbSc(scc,p-1) = 0] = no ;
scsch(sc,scc,p ) = yes $scscp(scc,p,sc) ;
pspn (scp(sc,p),s,n) $psn (p,s,n) = yes ;
```

*\* determine the representative sc2 of node (sc1 p) for non-existing scenarios in the tree*

```
loop (sc $sum[p, pProbSc(sc,p)],
  scaux = ord(sc) ;
  loop (p,
    scscr(sc,p+lag(p),scc) $[ord(scc) = scaux] = yes ;
    SCA(scc) $[ord(scc) = scaux] = yes ;
    scaux = sum[scscp(sca,p+lag(p),scc), ord(scc)] ;
    SCA(scc) = no ;
  ) ;
) ;
SCA(sc) $sum[p, pProbSc(sc,p)] = yes ;
```

# StarNetLite\_TEPM (xi)

\* solve transmission expansion planning model

**solve** mTEPM using MINLP minimizing vTotalTCost ;

\* scaling of the results

```
pInstalCapT(lc,y) = vCumInstDc.l(y, lc) + eps ;
pCommitt(y,sca,t, p,s) = sum[scscrc(sca,p,sc) , vCommitt.l (y,sc,p,s, t) ] + eps ;
pProduct(y,sca,g,psn(p,s,n)) = sum[scscrc(sca,p,sc) , vProduct.l (y,sc,p,s,n,g) ]*1e3 + eps ;
pEnergy (y,sca,g,psn(p,s,n)) = sum[scscrc(sca,p,sc) , vProduct.l (y,sc,p,s,n,g) ]*1e3 + eps ;
pReserve(y,sca,rs(r),p) = sum[scscrc(sca,p,sc) , vWtReserve.l(y,sc,p, r) ]*1e3 + eps ;
pWValue (y,sca,rs(r),p) = sum[scscrc(sca,p,sc) $pProbSc(sc,p), eWtReserve.m(y,sc,p, r)/sum[psn(p,s,n), pDuration(p,s,n)]/pProbSc(sc,p)]*1e3 + eps ;
pFlow (y,sca,la,psn(p,s,n)) = sum[scscrc(sca,p,sc) , vFlow.l (y,sc,p,s,n,la) ]*1e3 + eps ;
pTheta (y,sca,nd,psn(p,s,n)) = sum[scscrc(sca,p,sc) , vTheta.l (y,sc,p,s,n,nd) ] + eps ;
pLRMC (y,sca,nd,psn(p,s,n)) = sum[scscrc(sca,p,sc) $pProbSc(sc,p), eBalance.m (y,sc,p,s,n,nd) /pDuration(p,s,n) /pProbSc(sc,p)]*1e3 + eps ;
```

\* data output to xls file

```
put TMP putclose 'par=pProduct rdim=3 rng=Output!a1' / 'par=pEnergy rdim=3 rng=Energy!a1' / 'par=pReserve rdim=3 rng=WtrReserve!a1' / 'par=pWValue rdim=3 rng=WtrValue!a1' / 'par=pLRMC rdim=3
rng=LRMC!a1' / 'par=pCommitt rdim=3 rng=UC!a1' / 'par=pInstalCapT rdim=2 rng=InstalCapT!a1' / 'par=pFlow rdim=4 rng=Flow!a1' / 'par=pTheta rdim=3 rng=Angle!a1' /
'text="Year" rng=Output!a1' / 'text="Year" rng=Energy!a1' / 'text="Year" rng=WtrReserve!a1' / 'text="Year" rng=WtrValue!a1' / 'text="Year"
rng=LRMC!a1' / 'text="Year" rng=UC!a1' / 'text="Node" rng=InstalCapT!a1' / 'text="Year" rng=Flow!a1' / 'text="Year" rng=Angle!a1' /
'text="Scen" rng=Output!b1' / 'text="Scen" rng=Energy!b1' / 'text="Scen" rng=WtrReserve!b1' / 'text="Scen" rng=WtrValue!b1' / 'text="Scen"
rng=LRMC!b1' / 'text="Scen" rng=UC!b1' / 'text="Node" rng=InstalCapT!b1' / 'text="Scen" rng=Flow!b1' / 'text="Scen" rng=Angle!b1' /
'text="Unit" rng=Output!c1' / 'text="Unit" rng=Energy!c1' / 'text="Reservoir" rng=WtrReserve!c1' / 'text="Reservoir" rng=WtrValue!c1' / 'text="Node"
rng=LRMC!c1' / 'text="Unit" rng=UC!c1' / 'text="Node" rng=Flow!c1' / 'text="Node" rng=Angle!c1' /
```

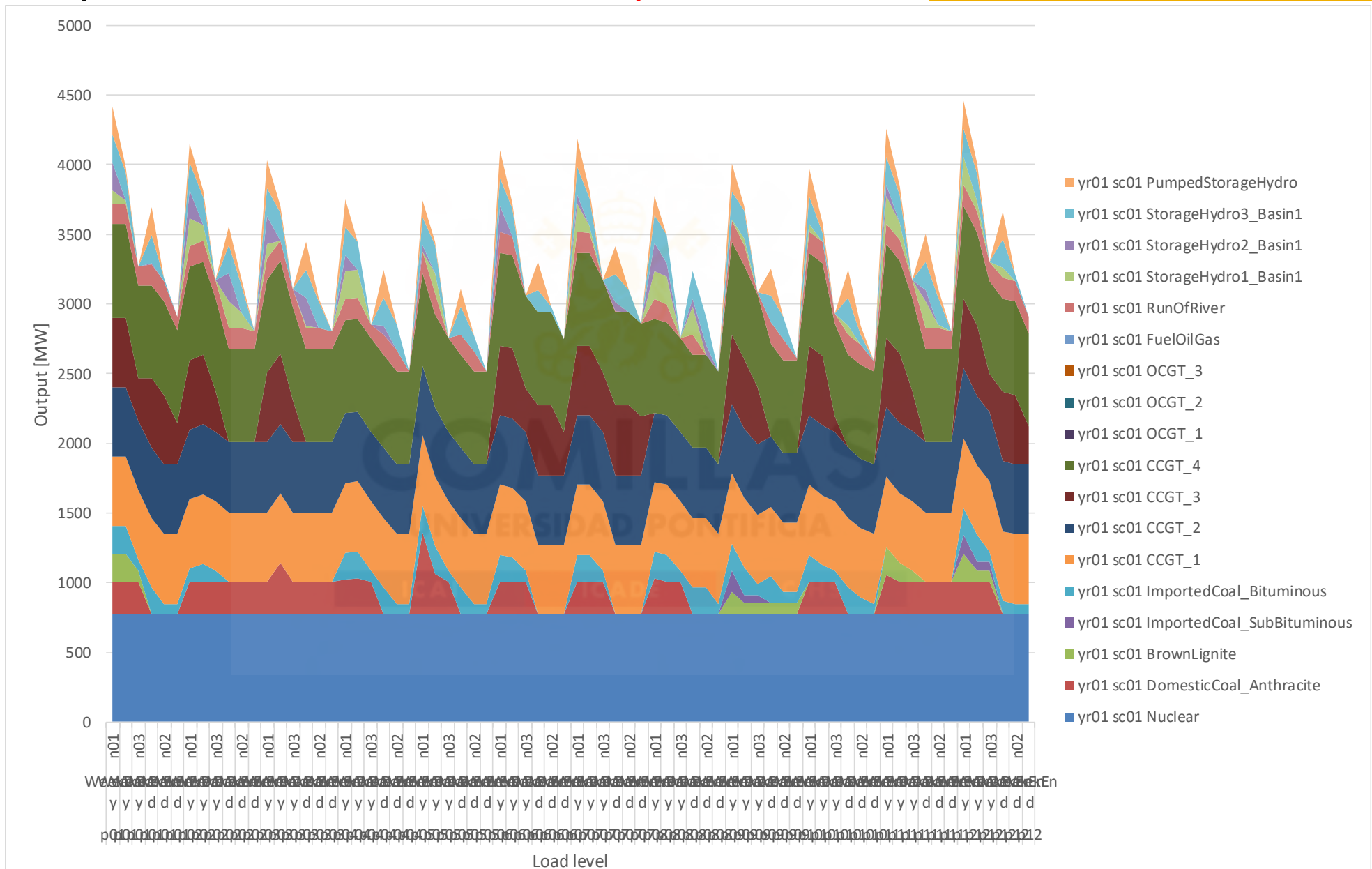
```
'text="Node" rng=Flow!d1' /
execute_unload 'tmp_%gams.user1%.gdx' pProduct pEnergy pReserve pWValue pLRMC pCommitt pInstalCapT pFlow pTheta
*$ifthen.OptSkipExcelOutput '%OptSkipExcelOutput%' == 0
execute 'gdxxrw tmp_%gams.user1%.gdx SQ=n EpsOut=0 0=tmp_%gams.user1%.xlsx @tmp_%gams.user1%.txt'
execute 'del tmp_%gams.user1%.gdx'
*$else.OptSkipExcelOutput
*$ Log Excel output skipped
*$endif.OptSkipExcelOutput
execute 'del tmp_%gams.user1%.txt'
```

\$OnListing

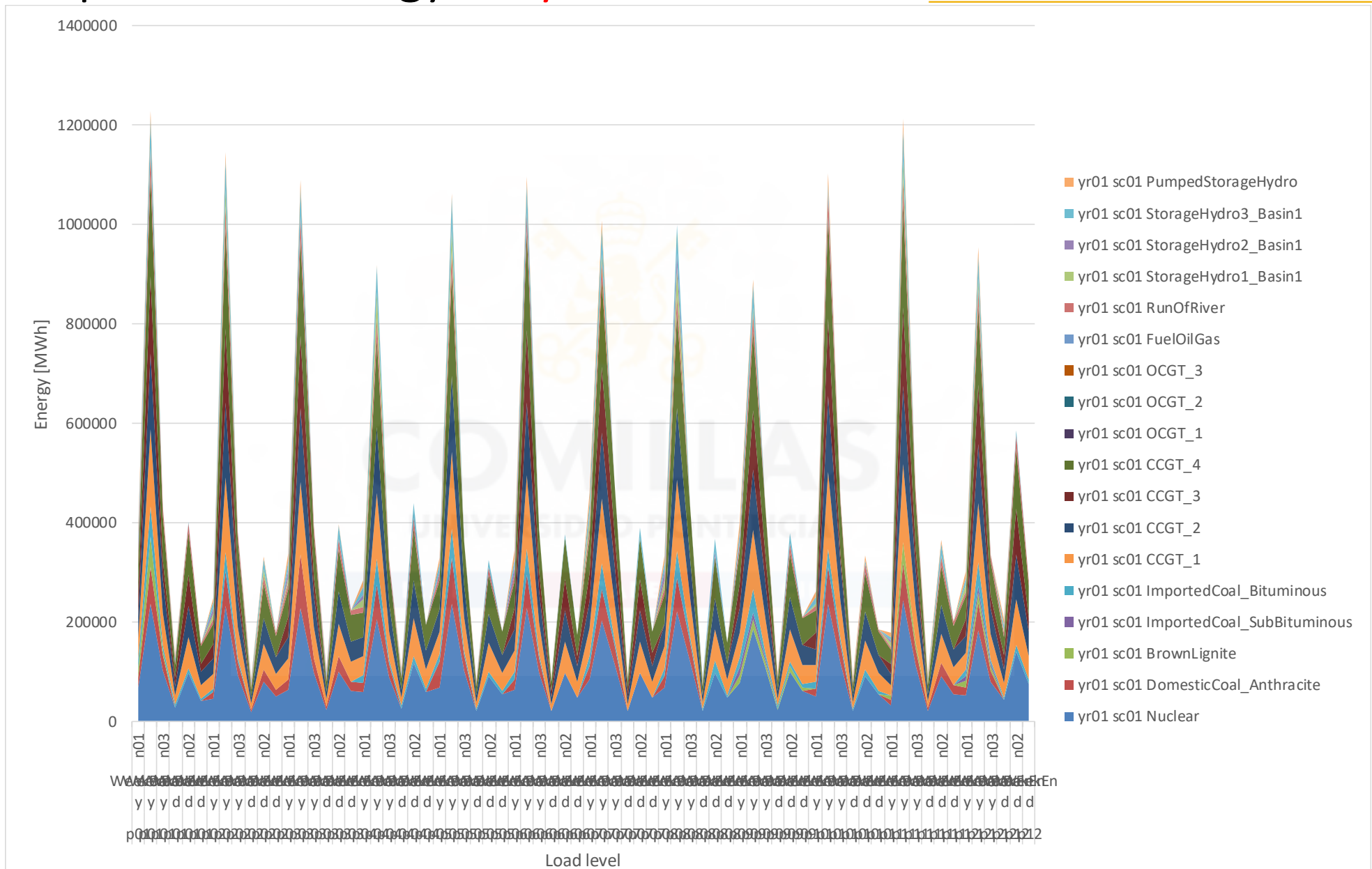




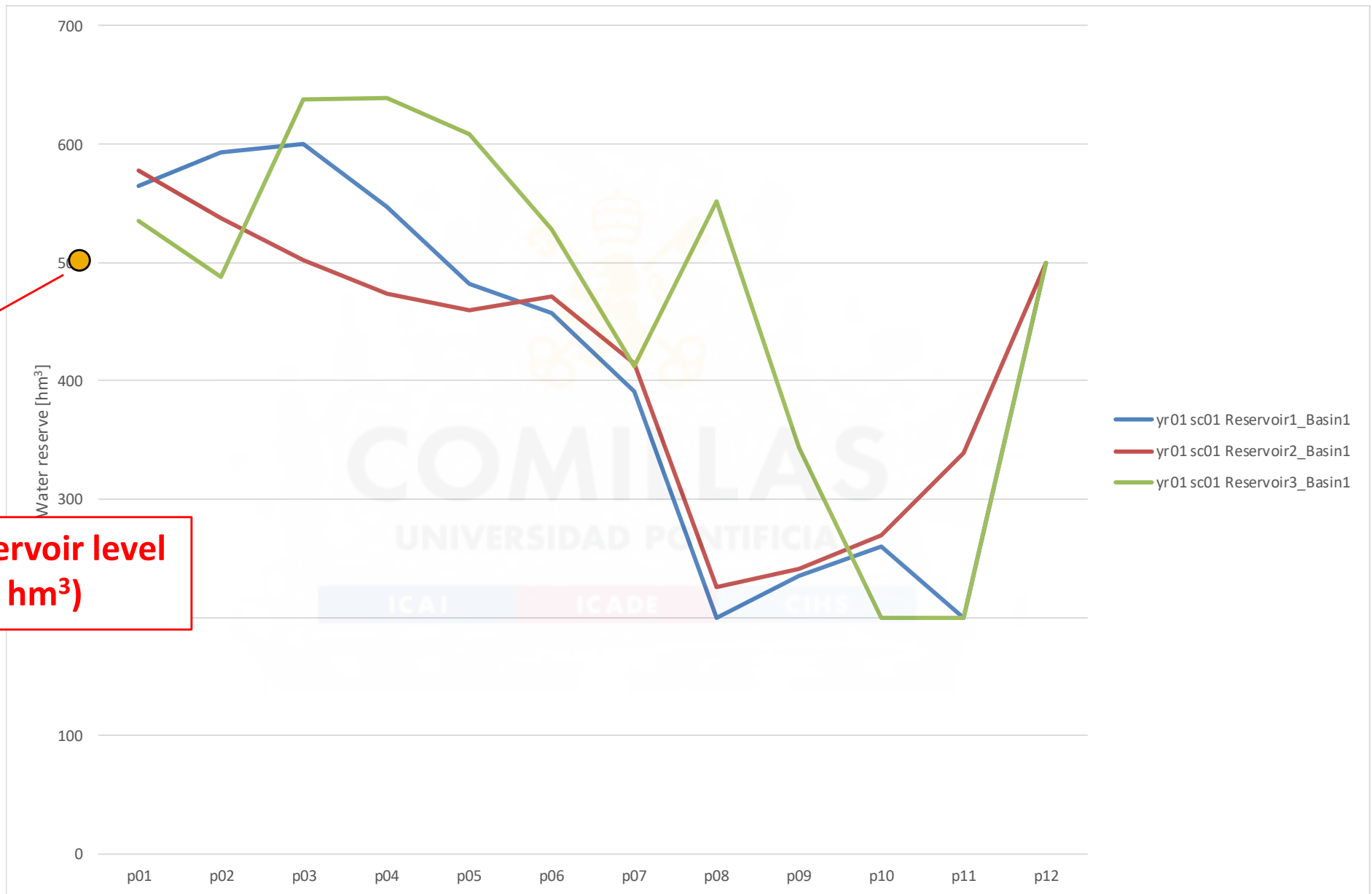
# Output Data. Production for year 1



# Output Data. Energy for year 1



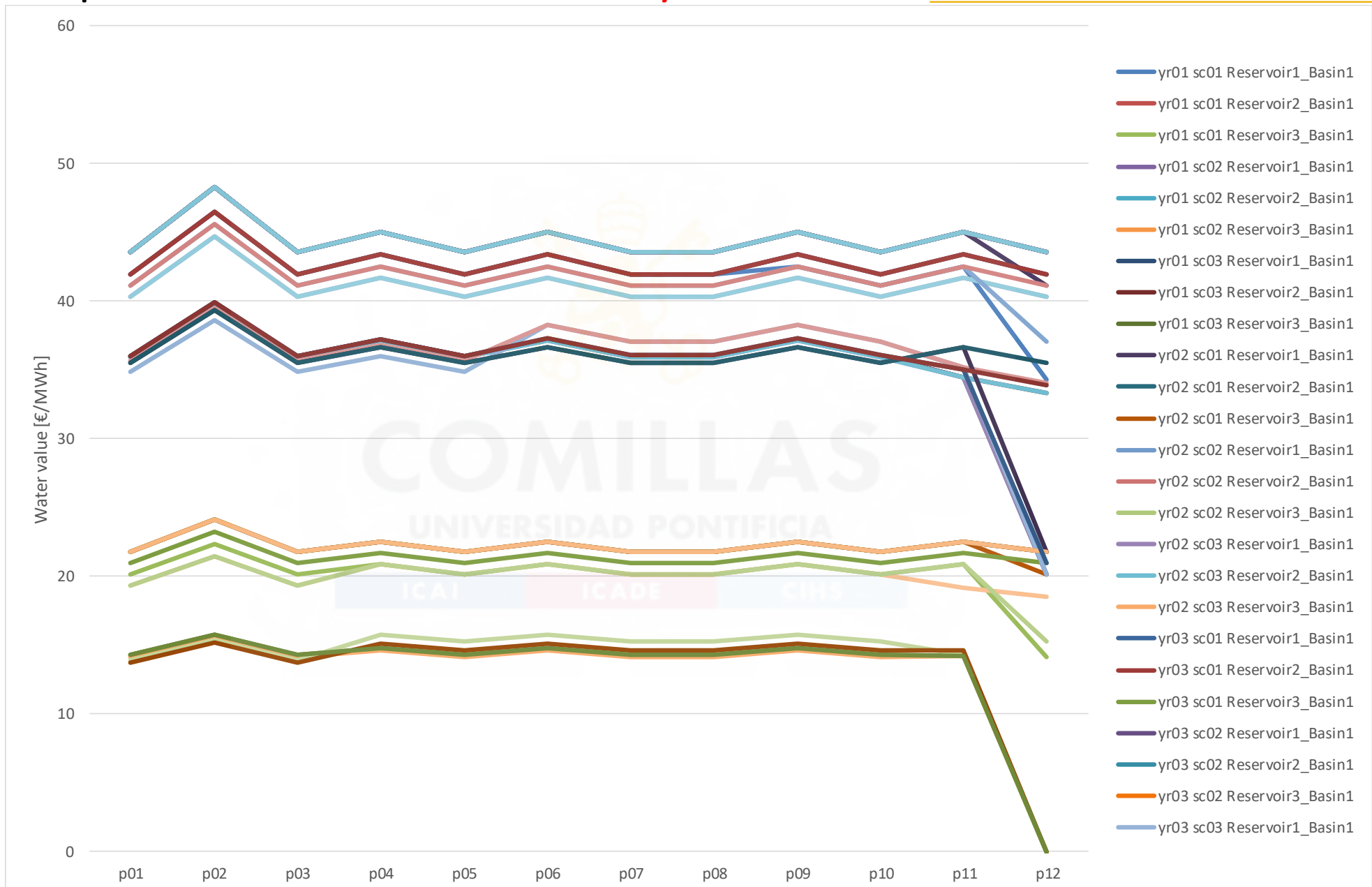
# Output Data. Reservoir level for year 1



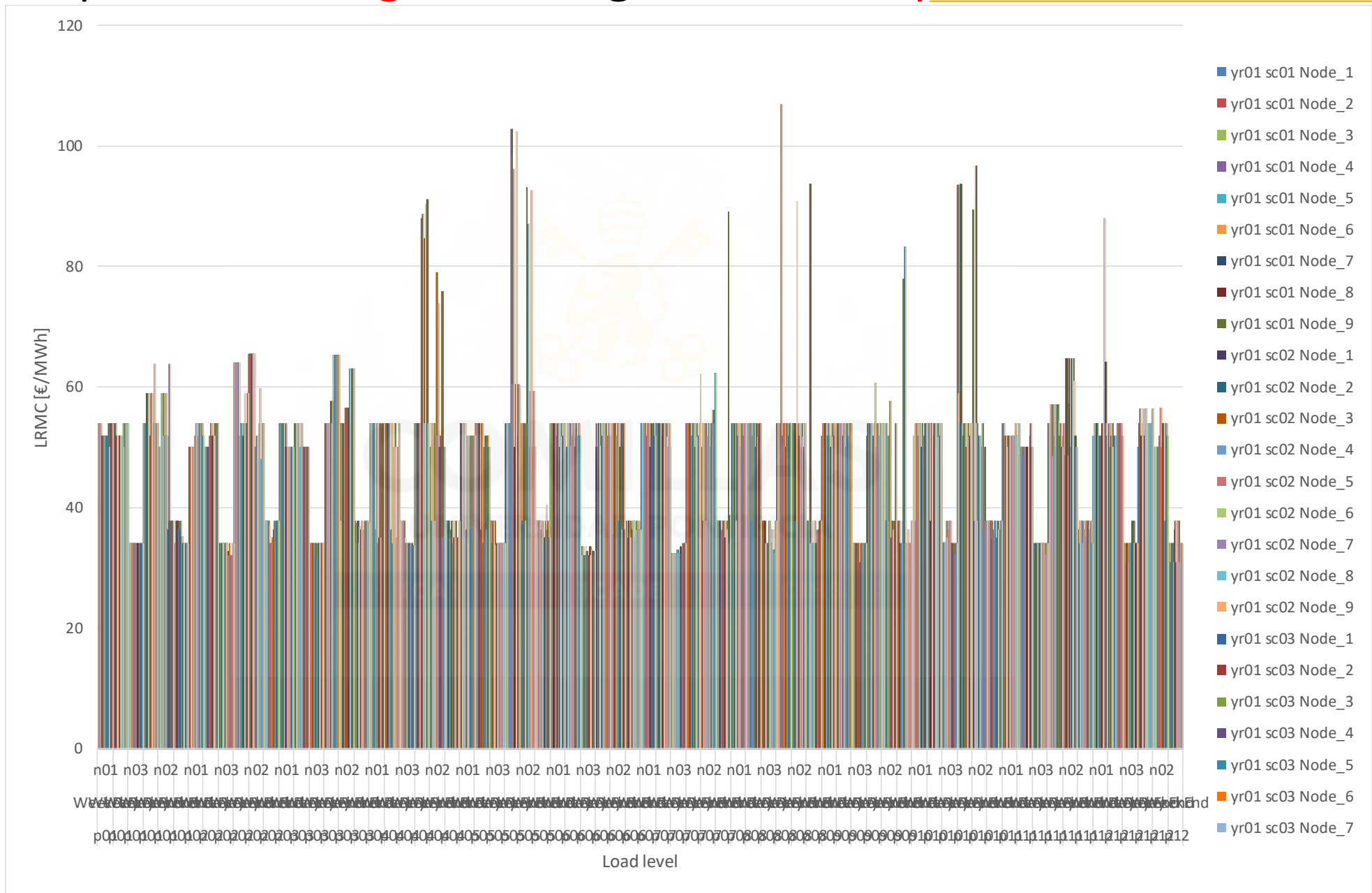
**Initial reservoir level (500 hm<sup>3</sup>)**



# Output Data. Water value for year 1



# Output Data. Long Run Marginal Cost for year 1



If TEP model is solved with binary investment decisions no marginal impact of those decisions is considered

1. Transmission Expansion Planning
2. Simple TEP models
3. Modeling issues
4. Prototype TEP. Mathematical formulation
5. Prototype TEP. Computer implementation
6. **Takeaways**



6



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Takeaways



# Task assignment

- At what threshold of transmission investment (fixed) cost does the potential new transmission line become economically viable (**breakeven**) in the sample model for installing the line in year 3?
- Assume that the transmission investment decisions have been already made, introduce the computation of **congestion rents** in GAMS and compare these congestion rents with the investment cost of a candidate transmission line
- Based on this model, think about how to implement mathematically the decision of opening lines (**switching**) in any period
- Analyze the impact of the **losses** (with and without) in the expansion decisions

# Takeaways

- Main **drivers** to build transmission lines
- Some **characteristics** to be considered in this model
- **Non-random and random uncertainties** affecting the analysis
- Main **criteria** used to define the best alternatives
- Decision **framed as an MCDM** solved by the weighted-sum method
- **Where to use** a transmission expansion planning model
- Input data and output results
- **Mathematical techniques** used to solve the model
- A **prototype** transmission expansion planning model



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