



ESCUELA TÉCNICA SUPERIOR DE INGENIERÍA - ICAI

## Master Universitario en Sector Eléctrico (Erasmus Mundus)

EMIN: International Master in Economics and Management of Network Industries

“Decision support models in the electric  
power industry”  
Bulk system reliability

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Session MOD.10





# Bibliography

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- *IEEE Tutorial Course on Reliability Assessment of Composite Generation and Transmission Systems.* IEEE October 1989
- *EPRI Composite-system reliability evaluation.* EPRI EL-5290. December 1987
- *Rivier, M. (1998) Modelo probabilista de explotación de un sistema eléctrico: contribución a la teoría marginalista.* Tesis doctoral. Universidad Pontificia Comillas.
- *Sánchez, P. (1998) Mejoras en la eficacia computacional de modelos probabilistas de explotación generación/red a medio plazo.* Tesis doctoral. Universidad Pontificia Comillas.  
([http://www.iit.upcomillas.es/aramos/tesis/tesis\\_PedroSanchez.pdf](http://www.iit.upcomillas.es/aramos/tesis/tesis_PedroSanchez.pdf))





# Content

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- Motivation and applications
  - Probabilistic operation models
  - Uncertainty modeling
  - Some models





# Motivation

- To give an indication about what it is possible to state with a decision tool
  - Capabilities and limitations
- To become familiar with network modeling techniques
- To give the mathematical foundation





# Long term applications

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- Network expansion planning
- Selection and evaluation of network investments
- Impact on the generation equipment and consumption
- Interconnections





# Medium term applications

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- **Traditional environment**
  - Studies about network performance
  - Generation localization
  - Adequacy assessment/reliability studies
  - Network maintenance
  - Operation planning
- **TPA or open access**
  - Check transfer capabilities
  - Determine payment for the network use
  - Assign network costs
  - Network remuneration studies
  - Evaluate network contracts





# Short term applications

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- Check the viability of the generation and consumption dispatch
- Determine nodal marginal prices
- Identify and determine losses
- Identify and determine zonal or local ancillary services
- Decisions about network operation



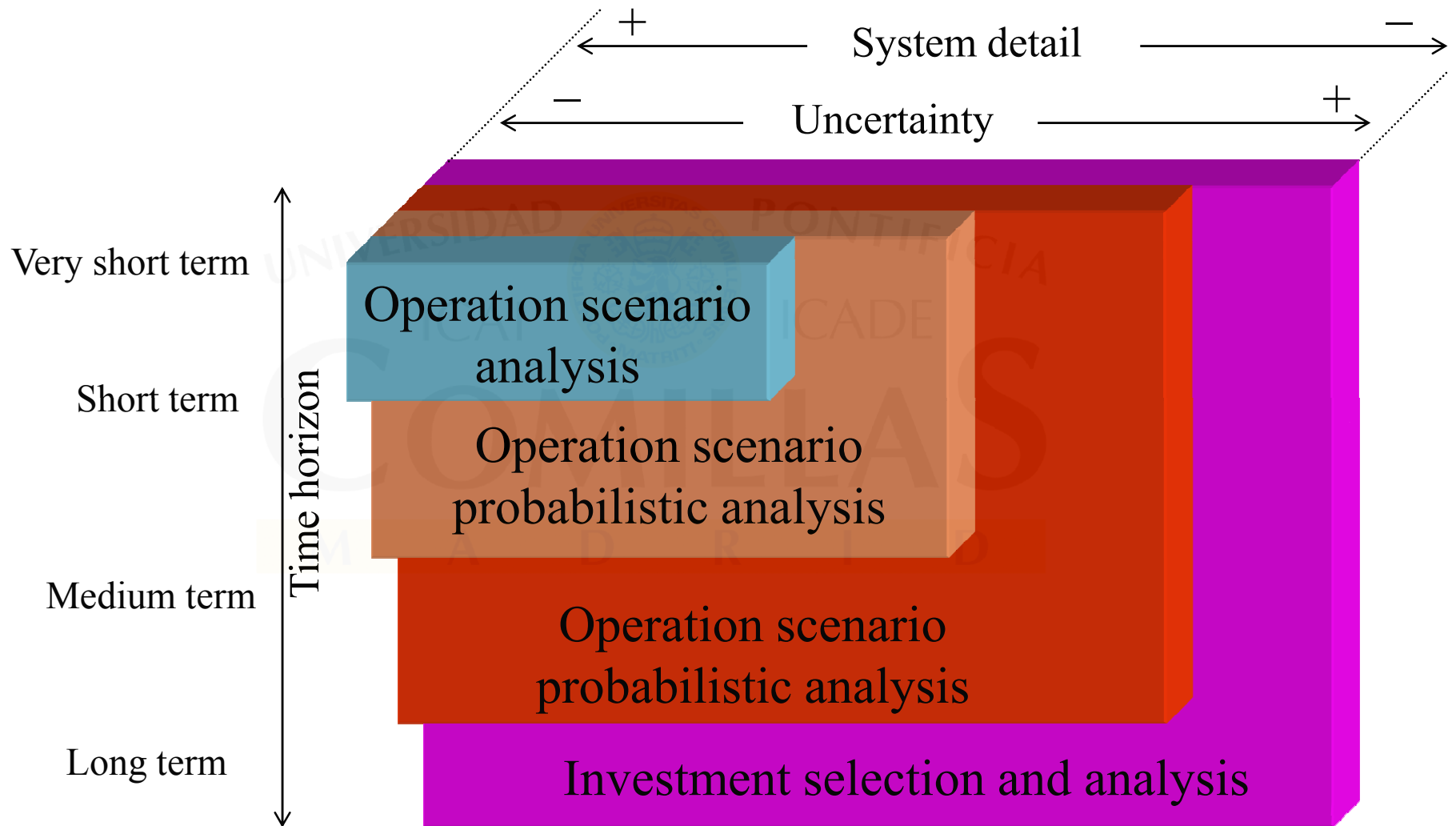
# Very short term applications

- **Static** analysis of the network
  - Flows
  - Voltages
- **Dynamic** analysis of the network
  - Stability
  - Voltage collapse





# Model hierarchy





# Content

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- Motivation and applications
- Probabilistic operation models
- Uncertainty modeling
- Some models





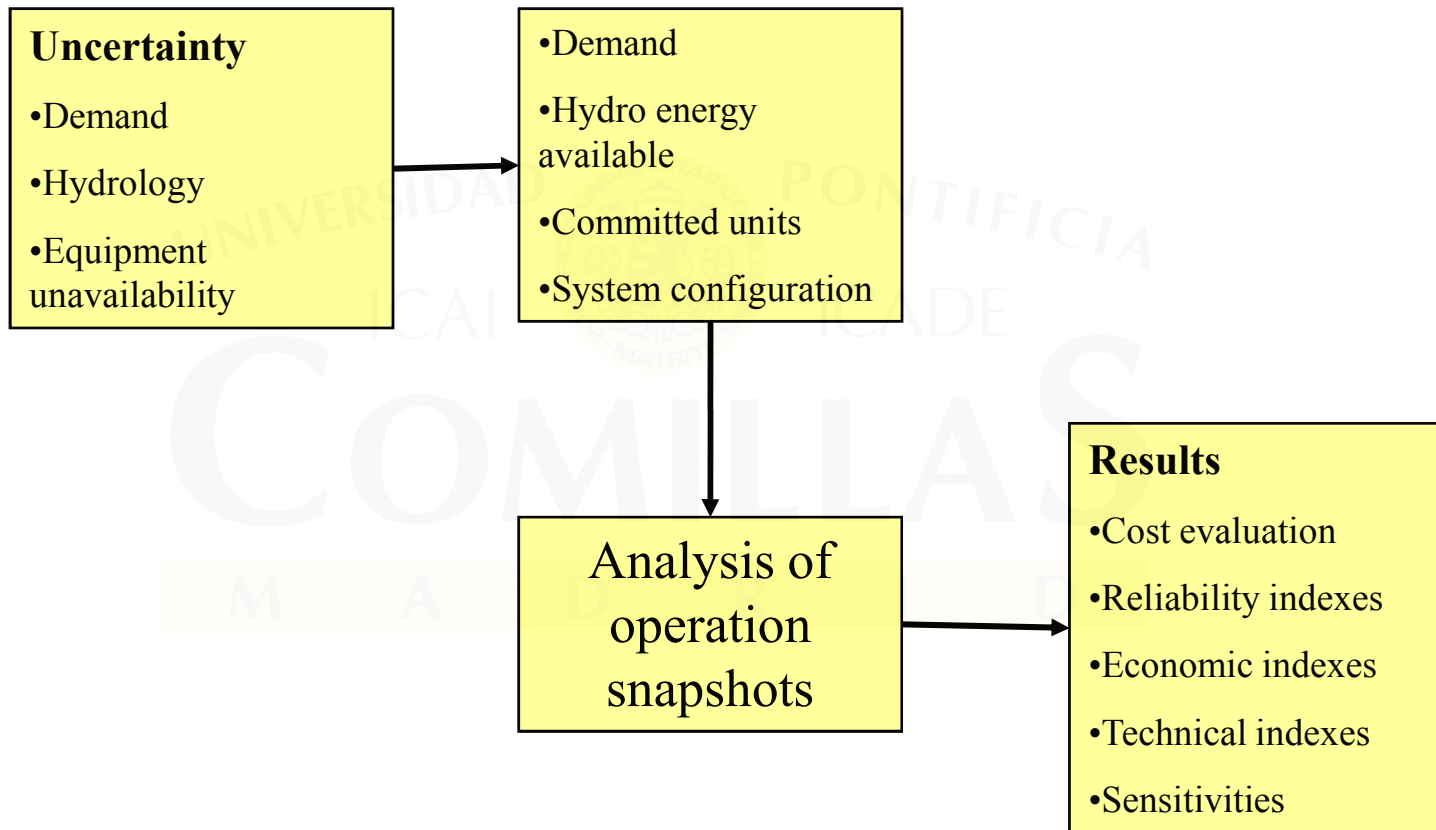
# Methods

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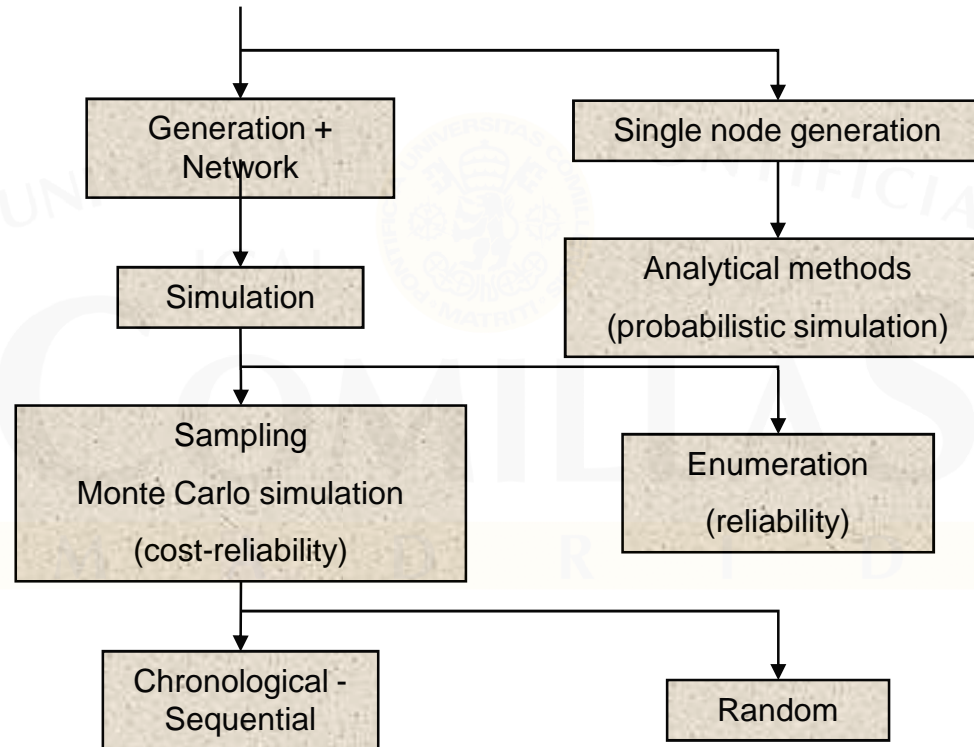
- Important developments in the field of **reliability studies** taking into account the transmission network
  - Adequacy assessment
- Extension to **cost studies**



# General structure



# Methods





# Electric network subsystem

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- Single node
- Generation/transmission
  - Transportation model (1st Kirchoff's law)
  - DC optimal power flow with or without losses
  - AC optimal power flow
  - Dynamic aspects
- Circuits
  - Branches: lines and transformers.
  - Nodes: substation buses.



# Security criterion in contingency dispatch

- Preventive

- Network and/or generation margin, N-1.
- Representation in the dispatch model (global optimization, relaxation, scenarios, reserve markets and interruptibility)

- Corrective

- Generation response margins
- Load redistribution



## Other characteristics to model

- Networks operating limits:
  - Line thermal limits.
  - Node voltages limits.
- Interruptible contracts
- Network emergency operation: e.g., tie and untie, substation reconfiguration
- Violation of preventive security regular criteria in special states (e.g., high cost, emergency)
- Reserves
- Exogenous criteria that condition the dispatch optimality (e.g., fuel quota)





# Generation dispatch model

- Optimization
- Simulation + heuristics
  - Sampling of random parameters
  - Logic rules and pre-established strategies to “optimize” the decisions





# Content

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- Motivation and applications
- Probabilistic operation models
- **Uncertainty modeling**
- Some models





# Uncertainty treatment



- Sources
  - Demand
  - Contingencies (availability of generation and network elements)
  - Unregulated inflows or hydro outputs
- Enumeration is not possible by **the huge number of states**  $\Rightarrow$  Monte Carlo simulation



# How many samples are needed?

- Let's suppose that **25 samples** are enough to determine the mean with a small enough confidence interval
- Failure probability
  - for a generator: **5 %**
  - for a line: **0.5 %**
- If I want to obtain 25 samples of
  - a generator failure I'll need **500 samples**
  - a line failure I'll need **5000 samples**
- Therefore, I'll need **at least 5000 samples** to obtain failures in lines and perhaps non served energy in certain nodes
- A **strong computational effort** is needed



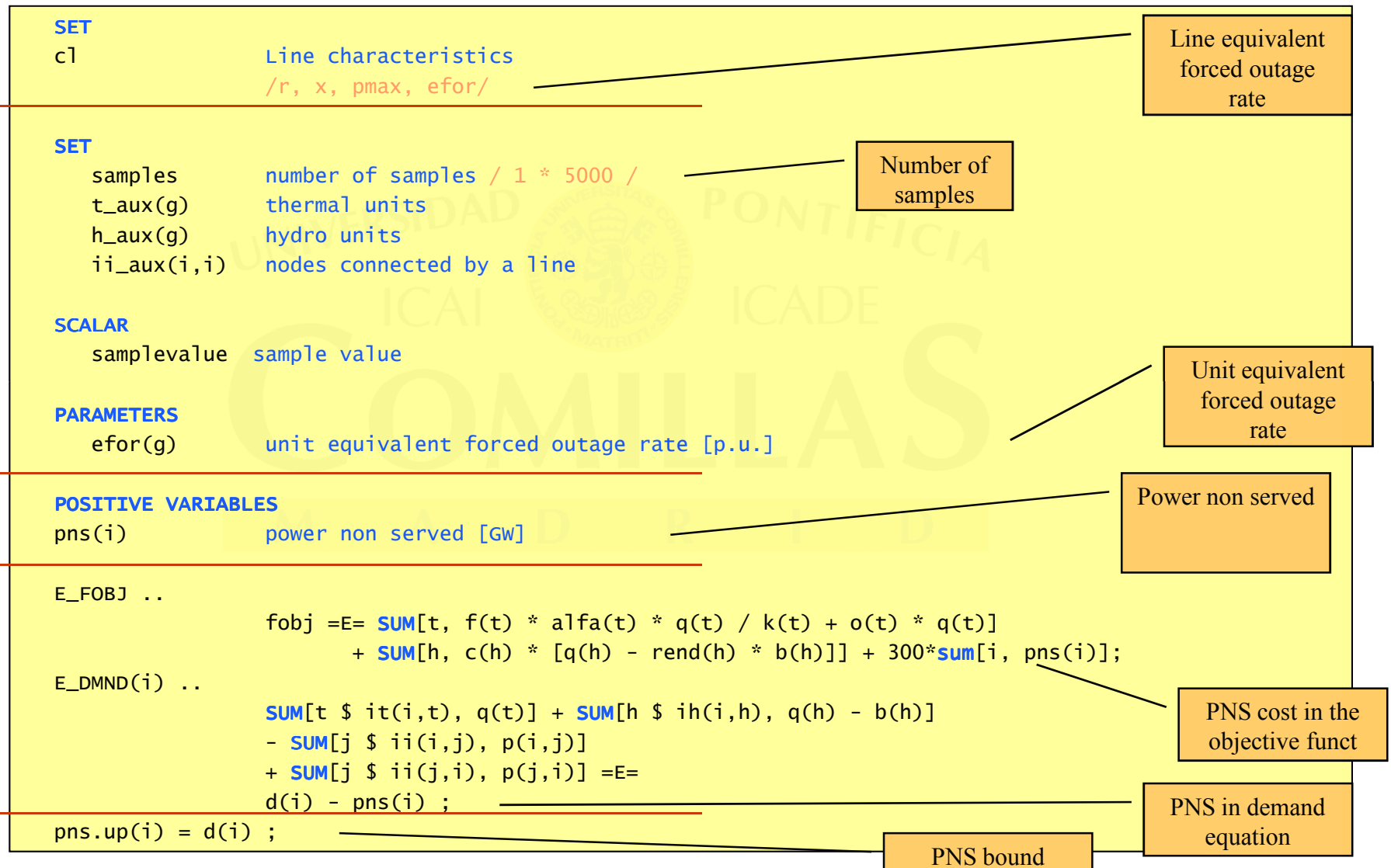


# Stages in Monte Carlo simulation

1. Pseudorandom number generation
2. Random variable generation
3. Simulation or parameter sampling
4. (Variance reduction techniques)
5. Results collection
6. Sampling process stop



# Composite operation model



# Monte Carlo simulation loop

```
* Initialization of auxiliary sets
ii_aux(i,j) = ii(i,j) ;
t_aux(g)    = t(g)    ;
h_aux(g)    = h(g)    ;

* Loop for all the samples
LOOP (samples,
      ii(i,j) = ii_aux(i,j) ;
      t(g)    = t_aux(g)    ;
      h(g)    = h_aux(g)    ;

* Sample of thermal unit availability
LOOP (t_aux(g),
      samplevalue = uniform(0,1) ;
      t(g) $[samplevalue < efor(g)] = no ;
) ;

* Sample of hydro unit availability
LOOP (h_aux(g),
      samplevalue = uniform(0,1) ;
      h(g) $[samplevalue < efor(g)] = no ;
) ;

* Sample of line availability
LOOP (ii_aux(i,j),
      samplevalue = uniform(0,1) ;
      ii(i,j) $[samplevalue < dtl(i,j,'efor')] = no ;
) ;

* Solving the problem
SOLVE MGR USING LP MINIMIZING fobj;

$ INCLUDE MSE_MGR_RESULTADOS.INC
) ;
```

Sample loop

Thermal unit availability

Hydro unit availability

Line availability

DC optimal power flow  
solution



# Monte Carlo simulation (I)

- It is used when the **number of states** of the random parameters is **very huge** (e.g., contingencies)
- Estimate the **mathematical expectation** of operating costs and/or reliability measures
- Simulate is equivalent to integrate or sample in hyperspace of random parameters with a known probability density function
- Determine **sample mean, mean variance, confidence interval**.
- Stop sampling when confidence interval is lower than a certain tolerance.





# Monte Carlo simulation (II)

- **Quadratic behavior** (4 times more samples divides by 2 the confidence interval)
- **Events with a small probability and a huge value** of the objective function cause high variances (it is the usual case of reliability indexes). Therefore, many samples are needed
- **Variance reduction techniques**
  - Common random numbers, antithetic variables, control variable, importance sampling, stratified sampling
  - Allow to reduce the size of the confidence interval of the mean without disturbing its value for a certain number of samples or, alternatively, achieve the desired precision with a lower sampling effort.



# Variance reduction techniques VRT (I)

- Usually, it is impossible to know in advance **the variance reduction to be achieved**, or even if it is going to be reduced. **We have to experiment** considering the real system to analyze.
- You have **to know the model in detail** that reproduces the system behavior.
- The use of VRT can be understood as **a way of taking advantage of information about the implied system**.
- Imply a **computational over-cost** to do certain preliminary samples or auxiliary computations in the same simulation process.



# Variance reduction techniques VRT (II)

- Common random numbers or correlated sampling or comparative simulation or synchronized pairs
  - Do sampling for different system configurations with the same set of random numbers being used each one for the same function in sampling process.
- Antithetic variables
  - It is based on the idea of introducing a negative correlation between two consecutive samples. It consists of the use of complementary random numbers in two consecutive simulations.



# Variance reduction techniques VRT (III)

- **Control variable**

- The basic idea is to use the results of a simpler model to predict or explain part of the variance of the value to estimate. A previous computation of the expected value of the control variable is needed. This computation has to be very quick compared to those of the variable to estimate.

- **Importance sampling**

- The random variable to estimate is replaced by another with the same mean but different variance. The probability density function used in the sampling process is modified to center it around the area of interest. Sampling probable but not interesting events is avoided.



# Variance reduction techniques VRT (IV)

- **Stratified sampling**

- The intuitive idea of this technique is similar to the previous one but in a discrete version. It consists on taking more samples of the random variable in the areas of greater interest. The variance is reduced by concentrating the simulation effort in the more relevant strata.





# Content

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  - Probabilistic operation models
  - Uncertainty modeling
- Some models



# Some IIT transmission network planning models

- Medium term application
  - StarNet/RD for different companies in Dominican Republic
  - SIMUSIS/SIMUMER/SIMUPLUS for REE
- Long term application
  - PERLA/CHOPIN for REE



# StarNet/RD (i)

([www.iit.upcomillas.es/aramos/StarNet.htm](http://www.iit.upcomillas.es/aramos/StarNet.htm))

The screenshot shows a Microsoft Excel spreadsheet titled "StarNet\_Ejemplo". The spreadsheet contains a table with the following data:

	A	B	C	D	E	F	G	H	I	J	K	L
1			<b>StarNet</b>									
2												
3			<i>Disco</i>			<b>c</b>						
4			<i>Directorio Entrada StarNet</i>			<b>c:\usuarios\andres\starnet</b>						
5			<i>Extension del caso</i>			<b>txt</b>						
6			<i>Directorio del caso</i>			<b>c:\usuarios\andres\starnet</b>						
7			<i>Archivo Normal .bat</i>			<b>StarNet.bat</b>						
8			<i>Archivo Runtime .bat</i>			<b>StarNetR.bat</b>						
9												
10												
11												
12												
13												
14												
15												
16												
17												
18												
19												
20												

Below the spreadsheet, a flow diagram shows a box labeled "Exportar caso" with two arrows pointing to two boxes: "Ejecutar modelo. Cargar resultados. GAMS complet" and "Ejecutar Modelo. Cargar resultados. GAMS runtime".





# StarNet/RD (ii)

```

Microsoft Excel - StarNet_Ejemplo
Archivo Edición Ver Insertar Formato Herramientas Datos Ventana ? Adgbe PDF
Escriba una pregunta
A1
A B C D E F G H I J K
1 * sn
2 * activación de la fila correspondiente
3 * NO activa la fila 0
4 * SÍ activa la fila 1
5
6 * nugr
7 * Modelo de explotación
8 * nudo único unico 0
9 * generacion/red SIN pérdidas 1
10 * generacion/red CON pérdidas 2
11
12 * optacpc
13 * Discretización del acoplamiento de los grupos en periodos cronológicos
14 * NO discretización 0
15 * SÍ discretización 1
16
17 * optacpm
18 * Discretización del acoplamiento de los grupos en periodos monótonos
19 * NO discretización 0
20 * SÍ discretización 1
21
22 * gsthdr
23 * Gestion de la hidráulica
24 * INTERperiodo 0
25 * INTRAperiodo 1
26
27 TABLE CASOS (caso,atmd) casos que se ejecutan
28
29 sn nugr optacpc optacpm gsthdr incdem facnod poper
30 caso-0 1 2 1 0 0 0 1 1
31 ;
32
33
34

```



# StarNet/RD (iii)

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
1	SETS																			
2																				
3	P			periodos	/		P001	/												
4	S			subperiodos	/		s1	/												
5	B			bloques de carga	/		b001	/												
6																				
7																				
8	ZN			empresas o zonas																
9	/																			
10	SUR																			
11	/																			
12																				
13	EM empresas						EMPRESA1	/												
14							EMPRESA2	/												
15																				
16	EMCP (em, cp)			pareja empresa zona	/		EMPRESA1.E01	/												
17							EMPRESA2.E02	/												
18																				
19	AR			areas	/		SUR	/												
20																				
21	PS			países	/		RD	/												
22																				
23	PI (ps)			países de interes	/		RD	/												
24																				
25	ARPS (ar, ps)			asignacion de areas a países																
26	/																			
27	SUR						RD													
28	/																			
29																				
30	TN			tension en los nudc	/		138	/												
31	CC			circuitos por linea	/		c1	/												
32																				
33																				
34	TP			tipos de combustibles																
35	/																			
36	COMB1																			
37	/																			
38																				
39																				
40	ND			nudos																
41	/																			
42	NUDO_1																			
43	NUDO_2																			
44	NUDO_3																			
45	NUDO_4																			
46	NUDO_5																			
47	NUDO_6																			
48	/																			
49																				
50	GR			generadores termicos e hidraulicos																
51	/																			



# StarNet/RD (iv)

	A	B	C	D	E	F	G	H	I	J	K	L
1	TABLE	DATDEM	(nd, p,s,b, atd)									
2												
3			b001.dm									
4	NUDO_1	.p001.s1	280.0									
5	NUDO_2	.p001.s1	240.0									
6	NUDO_3	.p001.s1	220.0									
7	NUDO_4	.p001.s1	150.0									
8	NUDO_5	.p001.s1	110.0									
9	NUDO_6	.p001.s1	110.0									
10												
11												
12												
13												
14												
15												
16												
17												
18												
19												
20												
21												
22												
23												
24												
25												



# StarNet/RD (v)

Microsoft Excel - StarNet\_Ejemplo

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Escritura una pregunta

A1 TABLE

1	TABLE	DATGEN	(gr, atg)																	
2																				
3		YN	PMX	PMN	SSAA	CARR														
4	TERM_1_1	0	360.0	180.0	1	0														
5	TERM_1_2	0	100.0	50.0	1	0														
6	TERM_2_1	0	500.0	250.0	1	0														
7	TERM_2_2	1	250.0	125.0	1	0														
8	TERM_3_1	1	320.0	160.0	1	0														
9	TERM_3_2	1	420.0	210.0	1	0														
10	TERM_4_1	1	180.0	90.0	1	0														
11	TERM_4_2	1	160.0	80.0	1	0														
12	TERM_5_1	1	190.0	95.0	1	0														
13	TERM_5_2	1	140.0	70.0	1	0														
14	TERM_6_1	1	220.0	110.0	1	0														
15	TERM_6_2	1	320.0	160.0	1	0														
16	+																			
17		TC1	CSTC1	A	Q	base														
18	TERM_1_1	1	1000	86.000	0	0														
19	TERM_1_2	1	1000	85.000	0	0														
20	TERM_2_1	1	1000	76.000	0	0														
21	TERM_2_2	1	1000	75.000	0	0														
22	TERM_3_1	1	1000	66.000	0	0														
23	TERM_3_2	1	1000	65.000	0	0														
24	TERM_4_1	1	1000	56.000	0	0														
25	TERM_4_2	1	1000	55.000	0	0														
26	TERM_5_1	1	1000	51.000	0	0														
27	TERM_5_2	1	1000	50.000	0	0														
28	TERM_6_1	1	1000	46.000	0	0														
29	TERM_6_2	1	1000	45.000	0	0														
30	+																			
31		E01																		
32	TERM_1_1	100																		
33	TERM_1_2	100																		
34	TERM_2_1	100																		
35	TERM_2_2	100																		
36	TERM_3_1	100																		
37	TERM_3_2	100																		
38	TERM_4_1	100																		
39	TERM_4_2	100																		
40	TERM_5_1	100																		
41	TERM_5_2	100																		
42	TERM_6_1	100																		
43	TERM_6_2	100																		
44	+																			
45		M001																		
46	TERM_1_1	0																		
47	TERM_1_2	0																		
48	TERM_2_1	0																		
49	TERM_2_2	0																		
50	TERM_3_1	0																		
51	TERM_3_2	0																		

Lista

Menu / a\_caso / a\_sets / a\_datdem / a\_datgen / a\_datmrx / a\_dated / a\_durac / a\_param / f\_resumen / f\_despacho /



# StarNet/RD (vi)

	A	B	C	D	E	F	G	H	I	J	K
1	TABLE		DATRED				(ni,nf,cc,atl)				
2							r	x	flmx	status	csl
3	NUDO_1	.	NUDO_2	.	c1		0.00750	0.04500	600.00	1	1
4	NUDO_2	.	NUDO_3	.	c1		0.00750	0.04500	600.00	1	1
5	NUDO_2	.	NUDO_4	.	c1		0.00750	0.04500	600.00	1	1
6	NUDO_3	.	NUDO_5	.	c1		0.00750	0.04500	600.00	1	1
7	NUDO_4	.	NUDO_5	.	c1		0.00750	0.04500	600.00	1	1
8	NUDO_5	.	NUDO_6	.	c1		0.00750	0.04500	600.00	1	1
9											
10											
11											
12											
13											
14											
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27											
28											
29											



# StarNet/RD (vii)

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
1	TABLE	DURAC (p, s, b)													
2															
3		b001													
4	p001.s1	1													
5															
6															
7															
8															
9															
10															
11															
12															
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21															
22															
23															
24															
25															





# StarNet/RD (viii)

	A	B	C	D	E	F	G	H	I	J
1	PARAMETER			DURS (atg)						
2	/									
3	p001			1						
4	/									
5	;									
6	NR ('NUDO_1')	=	YES							
7										
8	INTERC (ps, ps)	=	0							
9										
10	PBM (p)	=	NO							
11	SBM (s)	=	NO							
12	NBM (b)	=	NO							
13										
14	SB (s)	=	NO							
15	NB (b)	=	NO							
16	ST (s)	=	NO							
17	NT (b)	=	NO							
18										
19	PERCR	=	1							
20										
21	CENS	=	300							
22										
23	RT	=	0							
24	PNPT	=	0.085							
25										



# StarNet/RD (ix)

Microsoft Excel - StarNet\_Ejemplo

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Fecha: 03.12.04 Hora: 16:12:58

	A	B	C	D	E	F	G	H	I	J
1	Fecha:	03.12.04	Hora:	16:12:58						
2	DESPACHO POR EMPRESAS [MW]									
3										
4	PERIODO	p001								
5	SUBPERIODO	s1	ENERGIA							
6	BLOQUE	b001	[MWh]							
7										
8	EMPRESA1									
9										
10	TERM_2_2	0	0							
11	TERM_3_1	0	0							
12	TERM_3_2	0	0							
13	TERM_4_1	125.923	125.923							
14	TERM_4_2	160	160							
15	TERM_5_1	190	190							
16	TERM_5_2	140	140							
17	TERM_6_1	220	220							
18	TERM_6_2	320	320							
19										
20	EMPRESA2									
21										
22										
23										
24	PNS	0	0							
25	PINT	0	0							
26	DRRC	0	0							
27	DRTC	0	0							
28										
29	PERDIDAS	45.923	45.923							
30	SSAA	0	0							
31										
32	DEMANDA	1110	1110							
33										
34										
35										
36	Costo Marginal	60.965	60.965							

Menu / a\_caso / a\_sets / a\_datdem / a\_datgen / a\_datmrx / a\_datred / a\_durac / a\_param / f\_resumen / f\_despacho /





# StarNet/RD (x)

Microsoft Excel - StarNet\_Ejemplo

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Fecha: A1

	A	B	C	D	E	F	G	H	I	J	K
1	Fecha:	03.12.04	Hora:	16:12:58							
2		PERIODO	p001	SUBPERIODO	s1	BLOQUE	b001				
3											
4	PLANTA	BARRA	POT MAX	U.BASE	DESPACHO	%DESPACHO	FACT NOD	MULT LAGR		CVP	CVD
5			[MW]	0 no 1 si	[MW]	[%]	[p.u.]	[\$/MWh]		[\$/MWh]	[\$/MWh]
6	TERM_6_2	NUDO_6	320	0	320	100	0.834476	-	-	45	53.926
7	TERM_6_1	NUDO_6	220	0	220	100	0.834476	-	-	46	55.124
8	TERM_5_2	NUDO_5	140	0	140	100	0.885272	-	-	50	56.48
9	TERM_5_1	NUDO_5	190	0	190	100	0.885272	-	-	51	57.609
10	TERM_4_2	NUDO_4	160	0	160	100	0.918564	-	-	55	59.876
11	TERM_4_1	NUDO_4	180	0	125.923	70	0.918564	-	-	56	60.965
12	TERM_3_2	NUDO_3	420	0	0	0	0.939174	-	-	65	69.21
13	TERM_3_1	NUDO_3	320	0	0	0	0.939174	-	-	66	70.274
14	TERM_2_2	NUDO_2	250	0	0	0	0.963743	-	-	75	77.822
15											
16	Costo marginal en NUDO_1	60.965									
17	Reserva Resultante	54.077	Porciento	4.678							
18											
19											
20											
21											
22											
23											
24											
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27											
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29											
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35											
36											

Menu / a\_caso / a\_sets / a\_datdem / a\_datgen / a\_datmxx / a\_datred / a\_durac / a\_param / f\_resumen / f\_despacho /





# CHOPIN

- G. Latorre, J.I. Perez-Arriaga CHOPIN, A HEURISTIC MODEL FOR LONG TERM TRANSMISSION EXPANSION PLANNING IEEE Transactions on Power System, Vol. 9, No. 4, November 1994





# PLAER

- de Dios, R., Sáiz, A., Melsión, J.L. y Bassy, A., "PLAER. Strategic Transmission Network Planning". 11TH Power System Computation Conference, August 1993





# PERLA

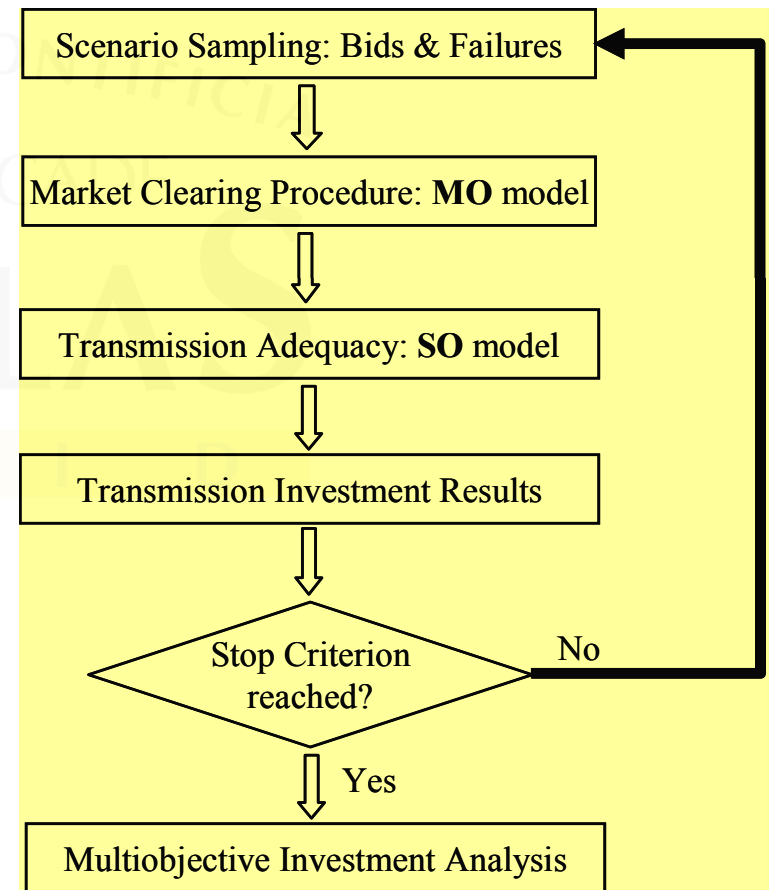
- J.F. Alonso, A. Sáiz, L. Martín G. Latorre, A. Ramos, I.J. Pérez-Arriaga *PERLA: An Optimization Model for Long Term Expansion Planning of Electric Power Transmission Networks* IIT-91-009 January 1991 (<http://www.iit.upcomillas.es/aramos/papers/COIMBR A.pdf>)

COMILLAS  
M A D R I D



# SIMUPLUS (i)

- Determine **incremental investment needs** in transmission network for the **medium term** in electricity markets



P. Sánchez-Martín, A. Ramos, J.F. Alonso  
*Probabilistic mid-term transmission planning in a liberalized market* IEEE Transactions on Power Systems 20 (4): 2135-2142 Nov 2005

([http://www.iit.upcomillas.es/aramos/papers/TP\\_WRS-00679-2004.pdf](http://www.iit.upcomillas.es/aramos/papers/TP_WRS-00679-2004.pdf))



# SIMUPLUS (ii)

1. Monte Carlo sampling:
  - Demand bids and generation offers
  - Units and circuits availability
  - Hydro and wind generation
2. Single node market clearing
  - Losses included as additional demand
3. Network constraint evaluation penalizing deviations with respect to market clearing
  - DC load flow, flow limits, losses
  - N-1 contingencies
4. Determine sensitivities (derivative of the objective function with respect to investment):
  - Improvement in existing circuits
  - New circuit expansion





## SIMUPLUS (iii)

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5. Investment multi-attribute analysis
  - Weigh sensitivities average, confidence interval, validity range, investment needs, environmental impact, etc.
  - Investment selection
6. Repeat all the process

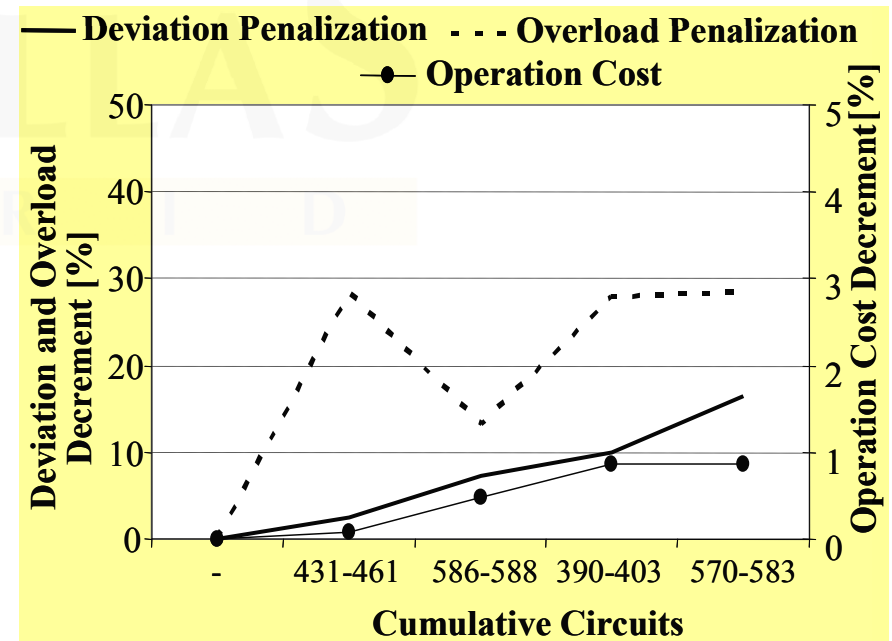


# SIMUPLUS (iv)

Spanish Iterative Investment Ranking

Stage	Candidates	Sensitivity mean [M\$/M\$]	Confidence interval [%]	Validity range [MW]	Multi-attribute value
<i>No circuit is added (initial stage)</i>					
1	431-461	-5.622	8.6	296	1.505
	390-403	-3.365	7.9	119	0.767
	570-583	-1.254	63.4	131	0.727
<i>Circuit 431-461 is added</i>					
2	586-588	-3.275	57.5	138	1.162
	390-403	-3.352	7.9	107	0.941
	570-583	-1.849	56.8	128	0.897
<i>Circuits 431-461 and 586-588 are added</i>					
3	390-403	-3.633	6.9	157	1.468
	570-583	-0.289	39.1	138	0.894
	424-520	-2.841	7.9	6	0.638
<i>Circuits 431-461, 586-588 and 390-403 are added</i>					
4	570-583	-0.587	51.4	129	1.434
	424-520	-2.930	7.8	5	0.821
	500-567	-1.784	10.1	30	0.745
<i>Circuits 431-461, 586-588, 390-403 and 570-583 are added</i>					
5	457-498	-0.495	19.8	83	1.293
	424-520	-3.027	7.6	7	0.933
	500-567	-1.665	10.9	21	0.774
<i>No more circuits are added</i>					

- 623 nodes and 1021 circuits, 165 thermal units and 76 hydro units. 12 network expansion alternatives. Sampling of 100 scenarios in each stage and obtain the 3 best alternatives.







# Summary

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- Where to use a composite reliability model
- Some characteristics to be considered into this model
- Mathematical techniques used to solve the model
- Some real applications





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